# Online Appendix for The Out-of-State Tuition Distortion 

Brian Knight and Nathan Schiff*

July 2nd, 2018

## 1 Theory Proofs and Extensions

### 1.1 Derivation of $\frac{\partial r_{W}}{\partial n}$ and $\frac{\partial r_{E}}{\partial n}$

We derive expressions for the change in resident tuition given a uniform increase in non-resident tuition. Note that, for state $W$, the budget constraint $f_{W} r_{W}+\left(1-f_{W}\right) n_{W}=m$ can be re-written as:

$$
P_{W}\left(r_{W}, n_{E}\right)\left[r_{W}-m\right]+\left[1-P_{E}\left(r_{E}, n_{W}\right)\right]\left[n_{W}-m\right]=0
$$

Then, considering a change in $n_{E}$, we have that:

$$
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial P_{W}}{\partial n_{E}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m\right]=0
$$

Similarly, considering a change in $n_{W}$, we have that:

$$
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{W}}+\frac{\partial P_{E}}{\partial n_{W}}\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
$$

Now, direct effects are given by $\frac{\partial P_{E}}{\partial r_{E}}=-\rho P_{E}\left(1-P_{E}\right)$ and cross-effects are given by $\frac{\partial P_{E}}{\partial n_{W}}=\rho P_{E}\left(1-P_{E}\right)$. Thus, $\frac{\partial P_{E}}{\partial r_{E}}=-\frac{\partial P_{E}}{\partial n_{W}}$, and, plugging this into the expressions above, we have:

$$
\begin{gathered}
\left(\frac{\partial P_{W}}{\partial r_{W}}\left(\frac{\partial r_{W}}{\partial n_{E}}-1\right)\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m\right]=0 \\
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}}\left(\frac{\partial r_{E}}{\partial n_{W}}-1\right)\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
\end{gathered}
$$

Adding these two conditions together, we have:

$$
\left(\frac{\partial P_{W}}{\partial r_{W}}\left(\frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial r_{W}}{\partial n_{W}}-1\right)\right)\left[r_{W}-m\right]+P_{W}\left(\frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial r_{W}}{\partial n_{W}}\right)-\frac{\partial P_{E}}{\partial r_{E}}\left(\frac{\partial r_{E}}{\partial n_{W}}+\frac{\partial r_{E}}{\partial n_{E}}-1\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
$$

[^0]Letting $\frac{\partial r_{W}}{\partial n}=\frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial r_{W}}{\partial n_{W}}$ and $\frac{\partial r_{E}}{\partial n}=\frac{\partial r_{E}}{\partial n_{E}}+\frac{\partial r_{E}}{\partial n_{W}}$, we have

$$
\left(\frac{\partial P_{W}}{\partial r_{W}}\left(\frac{\partial r_{W}}{\partial n}-1\right)\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n}-\frac{\partial P_{E}}{\partial r_{E}}\left(\frac{\partial r_{E}}{\partial n}-1\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
$$

Now, by symmetry, for the case of state E, we have:

$$
\left(\frac{\partial P_{E}}{\partial r_{E}}\left(\frac{\partial r_{E}}{\partial n}-1\right)\right)\left[r_{E}-m\right]+P_{E} \frac{\partial r_{E}}{\partial n}-\frac{\partial P_{W}}{\partial r_{W}}\left(\frac{\partial r_{W}}{\partial n}-1\right)\left[n_{E}-m\right]+\left(1-P_{W}\right)=0
$$

In the symmetric case, these simplify to:

$$
\left(\frac{\partial P}{\partial r}\left(\frac{\partial r}{\partial n}-1\right)\right)[r-n]+P \frac{\partial r}{\partial n}+(1-P)=0
$$

Solving, we have that:

$$
\frac{\partial r}{\partial n}=\frac{-(1-P)-\frac{\partial P}{\partial r}(n-r)}{P-\frac{\partial P}{\partial r}(n-r)}
$$

### 1.2 Proof of Proposition 1

Using some results from the prior section, we have that:

$$
\begin{gathered}
\left(\frac{\partial P_{W}}{\partial r_{W}}\left(\frac{\partial r_{W}}{\partial n_{E}}-1\right)\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m\right]=0 \\
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}}\left(\frac{\partial r_{E}}{\partial n_{W}}-1\right)\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
\end{gathered}
$$

When $r_{W}=n_{W}=m$, these simplify to:

$$
\begin{gathered}
\frac{\partial r_{W}}{\partial n_{E}}=0 \\
\frac{\partial r_{W}}{\partial n_{W}}=\frac{-\left(1-P_{E}\right)}{P_{W}}
\end{gathered}
$$

For the case of the budget of state $E$, we have that, by symmetry:

$$
\begin{gathered}
\frac{\partial r_{E}}{\partial n_{W}}=0 \\
\frac{\partial r_{E}}{\partial n_{E}}=\frac{-\left(1-P_{W}\right)}{P_{E}}
\end{gathered}
$$

Recall the original formula for the change in welfare:

$$
0.5\left[\left\{-P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(1-P_{E}\right)-P_{E} \frac{\partial r_{E}}{\partial n_{W}}\right\} \Delta n_{W}+\left\{-P_{E} \frac{\partial r_{E}}{\partial n_{E}}-\left(1-P_{W}\right)-P_{W} \frac{\partial r_{W}}{\partial n_{E}}\right\} \Delta n_{E}\right]
$$

Plugging in the above expressions, we have that there is no welfare gain when considering changes in nonresident tuition when $r_{W}=n_{W}=m$ and $r_{E}=n_{E}=m$. Thus, non-discriminatory policies are optimal.

### 1.3 Proof of Proposition 2

In the symmetric case, we have that $\frac{\partial P}{\partial n}=\rho P(1-P)$ and thus $n-m=1 / \rho P$. Further, using the budget constraint, one can show that $P=(n-m) /(n-r)$. Combining these, we have that:

$$
r=n-\rho(n-m)^{2}
$$

Further, note that $P=\exp (-\rho r) /[\exp (-\rho r)+\exp (-\rho n-\rho \delta)]$, which can be re-written as $r=n+\delta-$ $(1 / \rho) \ln [P /(1-P)]$. Next, note that $n-m=(1 / \rho P)$ and thus $P /(1-P)=1 /[\rho(n-m)-1]$. Combining these two expressions, we have that:

$$
r=n+\delta+(1 / \rho) \ln [\rho(n-m)-1]
$$

The first expression for $r$ is quadratic in $n$, with a peak at $n=m+(0.5 / \rho)$, at which point $r=m+(0.25 / \rho)$. Beyond this peak, the expression in decreasing in $n$. The second expression for $r$ equals negative infinity when $n=m+(0.5 / \rho)$ and is strictly increasing in $n$. Moreover, when $n=m+(2 / \rho), r=m+(2 / \rho)+\delta$. This is greater than $m+(0.25 / \rho)$, and hence there is a single crossing between $n=m+(0.5 / \rho)$ and $n=$ $m+(2 / \rho)$. At this single crossing, we have that $r<m<n$.

To show the comparative static, combining the two expressions above, note that $n$ can be implicitly defined by:

$$
-\rho^{2}(n-m)^{2}=\rho \delta+\ln [\rho(n-m)-1]
$$

Considering a change in $\rho$, we have that:

$$
-2 \rho(n-m)^{2}-2 \rho^{2}(n-m) \frac{\partial n}{\partial \rho}=\delta+\frac{(n-m)+\rho \frac{\partial n}{\partial \rho}}{\rho(n-m)-1}
$$

Re-arranging, we have that

$$
\left(-2 \rho(n-m)^{2}-\delta\right)[\rho(n-m)-1]-2 \rho^{2}(n-m) \frac{\partial n}{\partial \rho}[\rho(n-m)-1]=(n-m)+\rho \frac{\partial n}{\partial \rho}
$$

Finally, solving, we have,

$$
\frac{\partial n}{\partial \rho}=\frac{\left(-2 \rho(n-m)^{2}-\delta\right)[\rho(n-m)-1]-(n-m)}{\rho+2 \rho^{2}(n-m)[\rho(n-m)-1]}
$$

Thus, since $\rho(n-m)-1>0$ and $n>m$, we have that the numerator is negative and the denominator is positive. Thus, $\frac{\partial n}{\partial \rho}<0$.

### 1.4 Theoretical Extension: Fixed Costs

We next extend the theoretical model to include fixed costs. In particular, continue to assume that educating a student requires a constant expenditure, or marginal cost, equal to $m$, but that institutions also incur a fixed cost equal to $F$. Then, college $W$ faces the following budget constraint:

$$
P_{W} r_{W}+\left(1-P_{E}\right) n_{W}=\left(P_{W}+1-P_{E}\right) m+F
$$

Then, re-deriving $\frac{\partial r_{W}}{\partial n}$ and $\frac{\partial r_{E}}{\partial n}$ in the first appendix, we have that the budget constraint can be re-written as:

$$
P_{W}\left(r_{W}, n_{E}\right)\left[r_{W}-m\right]+\left[1-P_{E}\left(r_{E}, n_{W}\right)\right]\left[n_{W}-m\right]=F
$$

Then, considering a changes in $n_{E}$ and $n_{W}$ we have that the key conditions are unchanged:

$$
\begin{gathered}
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial P_{W}}{\partial n_{E}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m\right]=0 \\
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{W}}+\frac{\partial P_{E}}{\partial n_{W}}\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)=0
\end{gathered}
$$

Thus, the key conclusions from the welfare analysis remain unchanged.
We next consider tuition policies set under decentralization with fixed costs. In the symmetric case, Nash equilibrium out-of-state tuition continues to be characterized by:

$$
n=m+\frac{(1-P)}{\partial P / \partial n}
$$

Using the institutional budget constraint under symmetry $[\operatorname{Pr}+(1-P) n=m+F]$ and using the fact that $\partial P / \partial n=\rho P(1-P)$, this can be re-written as:

$$
P(n-r)=-F+\frac{1}{\rho P}
$$

Thus, non-resident tuition continues to be higher than resident tuition so long as fixed costs are sufficiently small (i.e., $F<(1 / \rho P)$ ).

### 1.5 Theoretical Extension: Increasing marginal costs

We next extend the theoretical model to increasing marginal costs. In particular, assume that marginal costs are quadratic in enrollment, with the parameter $\beta$ capturing the degree of convexity. That is, college $W$ faces the following budget constraint:

$$
P_{W} r_{W}+\left(1-P_{E}\right) n_{W}=\left(P_{W}+1-P_{E}\right) m+\beta\left(P_{W}+1-P_{E}\right)^{2}
$$

Then, re-deriving $\frac{\partial r_{W}}{\partial n}$ and $\frac{\partial r_{E}}{\partial n}$ in the first appendix, we have that the budget constraint can be re-written as:

$$
P_{W}\left(r_{W}, n_{E}\right)\left[r_{W}-m\right]+\left[1-P_{E}\left(r_{E}, n_{W}\right)\right]\left[n_{W}-m\right]=\beta\left[P_{W}\left(r_{W}, n_{E}\right)+\left(1-P_{E}\left(r_{E}, n_{W}\right)\right)\right]^{2}
$$

Then, considering a changes in $n_{E}$ and $n_{W}$ we have that the key conditions are given by:

$$
\begin{aligned}
&\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial P_{W}}{\partial n_{E}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m\right]= \\
& 2 \beta\left[P_{W}\left(r_{W}, n_{E}\right)+\left(1-P_{E}\left(r_{E}, n_{W}\right)\right)\right]\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial P_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\right) \\
&\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{W}}+\frac{\partial P_{E}}{\partial n_{W}}\right)\left[n_{W}-m\right]+\left(1-P_{E}\right)= \\
& 2 \beta\left[P_{W}\left(r_{W}, n_{E}\right)+\left(1-P_{E}\left(r_{E}, n_{W}\right)\right)\right]\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{W}}-\frac{\partial P_{E}}{\partial n_{W}}\right)
\end{aligned}
$$

In the symmetric case $\left(P_{E}=P_{W}\right)$, these can be written as:

$$
\begin{gathered}
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{E}}+\frac{\partial P_{W}}{\partial n_{E}}\right)\left[r_{W}-m-2 \beta\right]+P_{W} \frac{\partial r_{W}}{\partial n_{E}}-\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{E}}\left[n_{W}-m-2 \beta\right]=0 \\
\left(\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\right)\left[r_{W}-m-2 \beta\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}-\left(\frac{\partial P_{E}}{\partial r_{E}} \frac{\partial r_{E}}{\partial n_{W}}+\frac{\partial P_{E}}{\partial n_{W}}\right)\left[n_{W}-m-2 \beta\right]+\left(1-P_{E}\right)=0
\end{gathered}
$$

Thus, all of the previous results in the symmetric case follow, with $m$ replaced by $m+2 \beta$. Since the key results do not depend upon $m$, they thus do not depend upon $\beta$.

Under decentralization, the relevant version of equation (14) in the symmetric case ( $P_{W}=P_{E}$ ) is given by:

$$
\frac{\partial P_{W}}{\partial r_{W}} \frac{\partial r_{W}}{\partial n_{W}}\left[r_{W}-m-2 \beta\right]+P_{W} \frac{\partial r_{W}}{\partial n_{W}}+\left(1-P_{E}\right)-\frac{\partial P_{E}}{\partial n_{W}}\left[n_{W}-m-2 \beta\right]=0
$$

Since $\frac{\partial r_{W}}{\partial n_{W}}=0$ in equilibrium, we have that non-resident tuition can be characterized by:

$$
n=m+2 \beta+\frac{(1-P)}{\partial P / \partial n}
$$

Moreover, the budget constraint under symmetry is equal to:

$$
P(r-m)+(1-P)(n-m)=\beta
$$

Thus, under non-distortionary tuition, we have that $n=r=m+\beta$. Since $n>m+\beta$, it is the case that $n>r$.

### 1.6 Theoretical Extension: State subsidies

Assume that colleges receive a subsidy for each resident student from the state government equal to $\sigma_{c}$. These subsidies are financed via non-distortionary taxes that must be paid by families regardless of college choice. These subsidies are assumed to be exogenous and thus do not respond to changes in tuition policy. In this case, the inclusive value for a resident from state $W$ is given by:

$$
V_{W}\left(r_{W}, n_{E}\right)=(1 / \rho) \ln \left[\exp \left(\alpha \rho q_{W}-\rho r_{W}\right)+\exp \left(\alpha \rho q_{E}-\rho n_{E}-\rho \delta\right)\right]-P_{W} \sigma_{W}
$$

where the new term represents welfare costs associated with taxes required to finance subsidies and depend upon the likelihood of all residents attending in-state colleges.

Also, the college budget constraint for college $W$ is adjusted as follows:

$$
f_{W}\left(r_{W}+\sigma_{W}\right)+\left(1-f_{W}\right) n_{W}=m
$$

In the symmetric case, we have that the change in welfare is given by:

$$
\Delta n\left[-P \frac{\partial r}{\partial n}-(1-P)-\sigma \frac{\partial P}{\partial r} \frac{\partial r}{\partial n}-\sigma \frac{\partial P}{\partial n}\right]
$$

where the two new terms represents the change in taxes required to fund the appropriations due to a response in in-state enrollment probabilities. Under symmetry, we have that $\frac{\partial P}{\partial n}=-\frac{\partial P}{\partial r}$, and the expression can be written more compactly as:

$$
\Delta n\left[-P \frac{\partial r}{\partial n}-(1-P)-\sigma \frac{\partial P}{\partial r}\left(\frac{\partial r}{\partial n}-1\right)\right]
$$

The required change in resident tuition in this case can be written as:

$$
\frac{\partial r}{\partial n}=\frac{-(1-P)-\frac{\partial P}{\partial r}(n-r-\sigma)}{P-\frac{\partial P}{\partial r}(n-r-\sigma)}
$$

When $n=r+\sigma$, we have that the required change in tuition equals $-(1-P) / P$, and the welfare gain takes the simple form:

$$
\Delta n\left[\frac{\partial P}{\partial r} \frac{\sigma}{P}\right]
$$

Since $\frac{\partial P}{\partial r}<0$, we have that reductions in non-resident tuition from $n=r+\sigma$ lead to an increase in welfare.
With portable subsidies, all residents receive subsidies, regardless of which institution they attend, and taxes simply equal the subsidy. Assume that in-state students pay $r_{c}$ and the institution receives a subsidy equal to $\sigma_{c}$. For out-of-state students, assume that colleges charge a higher tuition equal to $n_{c}>r_{c}$ but that students can use their portable subsidy to help to cover their tuition. Thus, the net payment, for example, for students from $W$ attending college $E$ equals $n_{E}-\sigma_{W}$. In this case, the inclusive value for a resident from state $W$ equals:

$$
V_{W}\left(r_{W}, n_{E}\right)=(1 / \rho) \ln \left[\exp \left(\alpha \rho q_{W}-\rho r_{W}\right)+\exp \left(\alpha \rho q_{E}-\rho\left(n_{E}-\sigma_{W}\right)-\rho \delta\right)\right]-\sigma_{W}
$$

Moreover, the college budget constraint is given by:

$$
f_{W}\left(r_{W}+\sigma_{W}\right)+\left(1-f_{W}\right) n_{W}=m
$$

In the symmetric case, we have that the key welfare expressions can be written as:

$$
\begin{gathered}
\Delta n\left[-P \frac{\partial r}{\partial n}-(1-P)\right] \\
\frac{\partial r}{\partial n}=\frac{-(1-P)-\frac{\partial P}{\partial r}(n-r-\sigma)}{P-\frac{\partial P}{\partial r}(n-r-\sigma)}
\end{gathered}
$$

Thus, when $n=r+\sigma$, we have that the required change in tuition again equals $-(1-P) / P$. Given this, there is no welfare gain when reducing non-resident tuition from this higher level.

### 1.7 Theoretical Extension: More Than Two States

We next extend the model from two states to $S$ states, indexed by $s$. Let $P_{s}(t)$ denote the likelihood that a student from state $s$ attends institution $t$. Then, in-state attendance probabilities are given by:

$$
P_{s}(s)=\frac{\exp \left(\alpha \rho q_{s}-\rho r_{s}\right)}{\exp \left(\alpha \rho q_{s}-\rho r_{s}\right)+\sum_{t \neq s} \exp \left(\alpha \rho q_{t}-\rho n_{t}-\rho \delta\right)}
$$

Likewise, attendance at an out-of-state institution $t \neq s$ occurs with the following probability:

$$
P_{s}(t)=\frac{\exp \left(\alpha \rho q_{t}-\rho r_{t}-\delta\right)}{\exp \left(\alpha \rho q_{t}-\rho r_{t}-\delta\right)+\exp \left(\alpha \rho q_{s}-\rho r_{s}\right)+\sum_{r \neq s, r \neq t} \exp \left(\alpha \rho q_{r}-\rho n_{r}-\rho \delta\right)}
$$

Then, the change in welfare given a uniform increase in non-resident tuition equals:

$$
(1 / S) \Delta n\left[\sum_{s}-P_{s}(s) \frac{\partial r_{s}}{\partial n}-\sum_{t \neq s}\left(1-P_{s}(t)\right)\right]
$$

Under symmetry, this reduces to:

$$
\Delta n\left[-P \frac{\partial r}{\partial n}-(1-P)\right]
$$

where $P$ represents the likelihood of in-state attendance and $1-P$ represents the likelihood of out-of-state attendance, aggregated over all out-of-state institutions. Moreover, it remains the case that:

$$
\frac{\partial r}{\partial n}=\frac{-(1-P)-\frac{\partial P}{\partial r}(n-r)}{P-\frac{\partial P}{\partial r}(n-r)}
$$

Thus, the welfare calculations are unchanged with more than two states, under the interpretation that $1-P$ is the out-of-state attendance probability, aggregated over all possible out-of-state institutions.

Turning to decentralization, we have that state $s$ again chooses non-resident tuition to minimize resident tuition. That is, $\partial r_{s} / \partial n_{s}=0$. The institution budget constraint for college $s$ in this case is given by:

$$
P_{s}(s)\left(r_{s}-m\right)+\sum_{t \neq s} P_{t}(s)\left(n_{s}-m\right)=0
$$

Taking the derivative with respect to non-resident tuition $\left(n_{s}\right)$, we have that:

$$
\frac{\partial P_{s}}{\partial r_{s}} \frac{\partial r_{s}}{\partial n_{s}}\left[r_{s}-m\right]+P_{s} \frac{\partial r_{s}}{\partial n_{s}}+\sum_{t \neq s} P_{t}(s)+\sum_{t \neq s} \frac{\partial P_{t}(s)}{\partial n_{s}}\left[n_{s}-m\right]=0
$$

Since $\frac{\partial r_{s}}{\partial n_{s}}=0$ in equilibrium and using the fact that $\frac{\partial P_{t}(s)}{\partial n_{s}}=-\rho P_{t}(s)\left[1-P_{t}(s)\right]$, we have that:

$$
\sum_{t \neq s} P_{t}(s)=\sum_{t \neq s} \rho P_{t}(s)\left[1-P_{t}(s)\right]\left[n_{s}-m\right]
$$

In the symmetric case, we have that $P_{t}(s)=(1-P) /(S-1)$ for $t \neq s$, where $P$ is the probability of in-state attendance. Then, this can be written as:

$$
(1-P)=\frac{\rho(1-P)(S+P-2)(n-m)}{S-1}
$$

Solving for non-resident tuition, we have that:

$$
n=m+\frac{1}{\rho} \frac{S-1}{(S+P-2)}
$$

Since $P \leq 1$, we have that $n \geq m+1 / \rho$, and, moreover, non-resident tuition converges to $m+1 / \rho$ as the number of states grows large.

To further investigate how tuition policies change with the number of states, we next calibrate the model to match current tuition and in-state attendance probabilities. To do so, we first invert the above non-resident pricing rule to solve for $\rho$ as follows:

$$
\rho=\frac{1}{n-m} \frac{S-1}{(S+P-2)}
$$

We use in-state attendance probabilities of $P=0.75$. Tuition is taken from the overall averages in Table 1 of the main document, yielding $n=15.511$ and $r=6.358$. This implies that $m=8.646$. Finally, using $S=50$, we have that $\rho=0.1464$. With this estimate of $\rho$, we then choose $\delta$ to match $P=0.75$. This yields $\delta=24.947$.

With these parameters in hand, we can then estimate how pricing changes given a change in the number of states. As shown in Table 1 below, increasing the number of states beyond 50 does yield a reduction in non-resident tuition, falling from 15.512 to 15.503 for 90 states. This decrease is quite small however, and, as noted above, non-resident tuition is bounded from below by $m+1 / \rho$, which equals 15.477 . Thus, there is little scope in the model for reducing non-resident tuition via an increase in the number of states. In addition, while non-resident tuition does fall as the number of states increases, the gap between non-resident and resident tuition actually rises. This reflects the fact that the choice set also increases for students, yielding an increase in non-resident attendance, allowing universities to reduce in-state tuition. Likewise, as the number states decreases below 50, non-resident tuition increases but so does resident tuition, leading to a reduction in the gap between non-resident and resident tuition.

Table 1: Competition and Tuition Policies

| Number of <br> states <br> $(\mathrm{S})$ | Out-of-state <br> tuition <br> $(\mathrm{n})$ | In-state tuition <br> $(\mathrm{r})$ | In-state <br> attendance <br> $(\mathrm{P})$ |
| :---: | :---: | :---: | :---: |
| 10 | 15.533 | 8.097 | 0.926 |
| 20 | 15.525 | 7.588 | 0.867 |
| 30 | 15.520 | 7.132 | 0.819 |
| 40 | 15.515 | 6.728 | 0.782 |
| 50 | 15.512 | 6.362 | 0.750 |
| 60 | 15.509 | 6.027 | 0.724 |
| 70 | 15.507 | 5.718 | 0.701 |
| 80 | 15.505 | 5.431 | 0.681 |
| 90 | 15.503 | 5.163 | 0.663 |

## 2 Additional Empirical Results

### 2.1 Student Payments: Private Institutions

In parallel to Section VI.A of the main document, we present in Table 2 below results on student payments to private institutions using NPSAS data. As shown, residents pay a bit less, around $\$ 260$, in tuition payments than non-residents. This difference, however, is small when compared to the sample average of over $\$ 20,000$ in tuition payments. The gap is larger for net payments, with residents paying roughly $\$ 2,800$ less than residents. This implies that residents receive around $\$ 2,500$ more in grants than non-residents at private universities. To further explore the source of this difference, we next decompose total grants into their four components: federal grants, state grants, institution grants, and other grants. As shown, the bulk of the difference is explained by state grants. This finding is consistent with several state aid programs that generate financial differences between residents and non-residents at private institutions. For example, the Cal Grant Program is a state-funded program that provides aid to California residents attending California institutions,
both public and private. ${ }^{1}$ Likewise, the Hope scholarship in Georgia is available to state residents attending either public or private institutions in the state of Georgia. Finally, we note that these differences in payments between residents and non-residents are smaller than those documented for public institutions.

Table 2: Student payments in NPSAS data: private

|  | $(1)$ <br> Tuition/ <br> fees paid | $(2)$ <br> Net tuition/ <br> fees paid | $(3)$ <br> Federal <br> grants | $(4)$ <br> State grants | $(5)$ <br> Institution <br> grants | Other <br> grants |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| in-state | $-0.259^{* *}$ | $-2.847^{* * *}$ | $0.634^{* * *}$ | $1.761^{* * *}$ | -0.086 | $0.278^{* * *}$ |
|  | $(0.113)$ | $(0.213)$ | $(0.041)$ | $(0.039)$ | $(0.142)$ | $(0.063)$ |
| LHS | 21.435 | 9.63 | 1.636 | 1.195 | 7.721 | 1.253 |
| mean |  |  |  |  |  | 0.356 |
| $R^{2}$ | 0.587 | 0.318 | 0.164 | 0.283 | 0.110 |  |

All specifications include institution-by-year, state-of-residence-by-year, and cohort FE.
Net tuition and fees paid is net of all grants received by the student.
All dollar values are in thousands of 2011 dollars.
The sample consists of 32,130 full-time students attending four-year private institutions.

* $\mathrm{p}<0.1^{* *} \mathrm{p}<0.05^{* * *} \mathrm{p}<0.01$


### 2.2 Analysis of Private Institution Acceptance Decisions

In parallel to Section VI.E of the main document, Table 3 below presents results on private institution acceptance decisions using ELS data. As shown, private institutions are also more likely to admit residents, when compared to non-residents. The difference is only statistically significant, however, when including applicant fixed effects. In addition, the magnitude of any differences is smaller than the corresponding differences for public institutions.

Table 3: Analysis of Private Institution Acceptance Decisions

|  | $(1)$ | $(2)$ |
| :---: | :---: | :---: |
|  | Accept | Accept |
| in-state | 0.021 | $0.040^{* *}$ |
|  | $(0.017)$ | $(0.020)$ |
| sat | $0.001^{* * *}$ |  |
|  | $(0.000)$ |  |
| gpa | $0.146^{* * *}$ |  |
|  | $(0.017)$ | 0.821 |
| $R^{2}$ | 0.245 | yes |
| student FE | no |  |

Linear probability models of acceptance decisions with institution FE
Sample consists of 5,960 students reporting SAT and GPA scores
Four-year institutions with at least 10 appearances in student application sets

* $\mathrm{p}<0.1^{* *} \mathrm{p}<0.05^{* * *} \mathrm{p}<0.01$

[^1]
### 2.3 Additional Robustness Checks of Main Specification

Table 4: Alternative Border-Side Widths

| Table 4: Alternative Border-Side Widths |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10km border-sides |  |  |  | 30km border-sides |  |  |
|  | Enroll | Enroll percent | Ln Enroll | Enroll | Enroll percent | Ln Enroll |  |
| in-state | $32.997^{* * *}$ | $0.796^{* * *}$ | $1.455^{* * *}$ | $78.606^{* * *}$ | $0.822^{* * *}$ | $1.913^{* * *}$ |  |
|  | $(3.168)$ | $(0.008)$ | $(0.050)$ | $(6.935)$ | $(0.007)$ | $(0.053)$ |  |
| Observations | 16422 | 11820 | 16422 | 17286 | 14336 | 17286 |  |
| $R^{2}$ | 0.439 | 0.870 | 0.732 | 0.457 | 0.906 | 0.768 |  |
| \#Clusters | 2790 | 2288 | 2790 | 2882 | 2622 | 2882 |  |

Columns 1-3 at border-side level for 10 km border-sides, cols $4-6$ use 30 km border-sides.
All specifications include university-year FE and border-side-year FE.
Sample is public universities, 1997-2011, excluding two-year colleges.
Standard errors clustered at university-border-side level

* $\mathrm{p}<0.1^{* *} \mathrm{p}<0.05^{* * *} \mathrm{p}<0.01$

Table 5: Excluding Border Institutions

|  | $(1)$ <br> Enroll | $(2)$ <br> Enroll percent | $(3)$ <br> Ln Enroll |
| :--- | :---: | :---: | :---: |
| in-state | $46.736^{* * *}$ | $0.814^{* * *}$ | $1.652^{* * *}$ |
|  | $(5.397)$ | $(0.008)$ | $(0.050)$ |
| Observations | 16092 | 12536 | 16092 |
| $R^{2}$ | 0.462 | 0.892 | 0.779 |
| \#Clusters | 2682 | 2308 | 2682 |

Regressions run at border-side level, 20km border-sides.
Sample is public universities only, 1997-2011;
two-year colleges are excluded.
Sample also drops universities within 30km of border.
All specifications include univ-year and border_side-year FE.
Standard errors clustered at university-border-side level.

* $\mathrm{p}<0.1^{* *} \mathrm{p}<0.05^{* * *} \mathrm{p}<0.01$


### 2.4 Confidence Intervals for Welfare Analysis

The statistic for the required increase in resident tuition equals:

$$
S(\rho)=\frac{-(1-P)+\rho(n-r) P(1-P)}{P+\rho(n-r) P(1-P)}
$$

This can be written as

$$
S(\rho)=\frac{g(\rho)}{h(\rho)}
$$

To apply the Delta method, we require $S^{\prime}(\rho)$. Applying the quotient rule, we have that:

$$
S^{\prime}(\rho)=\frac{g^{\prime}(\rho) h(\rho)-g(\rho) h^{\prime}(\rho)}{h(\rho)^{2}}
$$

Using the fact that $g^{\prime}(\rho)=h^{\prime}(\rho)=(n-r) P(1-P)$ and that $h(\rho)-g(\rho)=1$, this can be re-written as:

$$
S^{\prime}(\rho)=\frac{(n-r) P(1-P)}{h(\rho)^{2}}
$$

Then, using the delta method, the standard error for the required change in resident tuition equals $\sigma(\rho)\left|S^{\prime}(\rho)\right|$.
Following similar logic the standard error for the change in welfare for resident students equals $P \sigma(\rho)\left|S^{\prime}(\rho)\right|$ and this is also the standard error for the change in combined welfare.

### 2.5 Illustration of Identification Strategy



Figure 1: Border-Sides and Distance Bins Diagram


[^0]:    *Knight: Brown University, 64 Waterman Street, Providence, RI 02906, brian_knight @brown.edu. Schiff: Shanghai University of Finance and Economics, 777 GuoDing Road, Shanghai, China, nschiff@gmail.com.

[^1]:    ${ }^{1}$ For further details, see http://www.csac.ca.gov/doc.asp?id=568 (accessed October 16, 2015).

