Monetary policy and endogenous financial crises

Frédéric Boissay (Bank for International Settlements)

Fabrice Collard (Toulouse School of Economics)

Jordi Galí (CREI and Universitat Pompeu Fabra)

Cristina Manea (Bank for International Settlements)

AEA — January 2023

The views expressed here are our own and may not reflect those of the BIS

What is the link between monetary policy and financial instability?

• Positive approach:

- What are the channels through which monetary policy affects financial stability?
- Is there a trade-off between price and financial stability?
- To what extent may monetary policy itself brew financial vulnerabilities?
- Normative approach
 - Should monetary policy (MP) account for financial stability (FS) risks? Conventional ("No") versus more recent ("yes") view
 - → Needed: models where MP affects the incidence and severity of crises

NK model with endogenous and microfounded financial crises

- Textbook New Keynesian (NK) model, with capital accumulation and sticky prices
 - + Idiosyncratic productivity shocks → capital reallocation among firms via a credit market
 - + Financial frictions ightarrow credit market prone to endogenous collapse when borrowers search for yield
 - + Global solution o capture nonlinearities and dynamics far away from steady state
- MP is the "only game in town" (e.g. no macroprudential policy)

Main findings

- 1. Monetary policy affects financial stability in the short run, via aggregate demand and in the medium run, via capital accumulation
- 2. MP as a backstop is effective to address both financial and price instability. Normalisation path depends on the cause of financial stress
- 3. MP can lead to a crisis if the policy rate remains too low for too long and then increases abruptly
- 4. Reacting to both output and inflation improves FS and welfare upon strict inflation targeting

Contribution to the literature

- We study how MP affects FS in a NK model with endogenous microfounded crises
- Monetary policy and financial stability (reduced form models of endogenous crises)

Woodford (2012), Filardo and Rungcharoentkitkul (2016), Svensson (2017), Gourio, Kashyap, Sim (2018), Ajello, Laubach, Lopez–Salido, Nakata (2019), Cairo and Sim (2018), Borio, Disyatat and Rungcharoentkitkul (2019)

- Micro-founded models of endogenous financial crises
 - Boissay, Collard, Smets (2016), Benigno and Fornaro (2018), Gertler, Kiyotaki, Prestipino (2019)
- ullet Our approach: fragility of financial markets (eq institutions) and search–for–yield behaviours (eq collateral constraints)

An extended New-Keynesian Model

Model- Agents

- Central bank: sets nominal interest rate
- Household: representative, works, consumes, saves (nominal bonds, firm equity)
- Retailers: monopolistic, diversify intermediate goods, sticky prices
- Intermediate goods firms: competitive, issue equity, invest, produce with labor and capital
 - + Idiosyncratic productivity shocks → capital reallocation among firms via a credit market

Central bank

• Sets nominal interest rate i_t on risk–free public bond B_t according to the following policy rule:

$$1+i_t=rac{1}{eta}(1+\pi_t)^{\phi_\pi}\left(rac{Y_t}{ar{Y}}
ight)^{\phi_y}$$

• We experiment with different specifications, including Taylor (1993)'s rule (TR93) and SIT

Households

• The representative household consumes a basket of goods C_t , works N_t , invests in public bonds B_t and in intermediate goods firm $j \in [0, 1]$'s equity $P_t Q_t(j)$

$$\max_{C_t, N_t, B_t, Q_t(j)} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{C_t^{1-\sigma}}{1-\sigma} - \chi \frac{N_t^{1+\varphi}}{1+\varphi} \right]$$

s.t.
$$P_tC_t + B_t + P_t \int_0^1 Q_t(j)dj \le W_tN_t + (1+i_{t-1})B_{t-1} + P_t \int_0^1 D_t(j)dj + \mathcal{X}_t$$

◆ Optimality conditions

Retailers

 Monopolistic retailer i ∈ [0,1] produces a differentiated final good using intermediate goods and sets its price subject to quadratic adjustment costs

$$\max_{P_t(i),Y_t(i)} \mathbb{E}_0 \sum_{t=0}^{\infty} \Lambda_{0,t} \left[\frac{P_t(i)}{P_t} Y_t(i) - \frac{(1-\tau)p_t}{P_t} Y_t(i) - \frac{\varsigma}{2} \left(\frac{P_t(i)}{P_{t-1}(i)} - 1 \right)^2 Y_t \right]$$
s.t.
$$Y_t(i) = \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} (C_t + I_t) \text{ where } I_t \equiv K_{t+1} - (1-\delta)K_t$$

• Markup $\mathcal{M}_t \equiv \frac{P_t}{(1-\tau)p_t}$ will be important for the effect of MP on FS

◆ Optimality conditions

Intermediate goods firms

- ullet Continuum of 1-period firms indexed by $j \in [0,1]$
- End of t-1: Firms are similar and <u>all</u> get start-up equity funding $P_{t-1}Q_{t-1}$ and purchase capital $K_t = Q_{t-1}$

Intermediate goods firms

- Continuum of 1-period firms indexed by $j \in [0,1]$
- End of t-1: Firms are similar and <u>all</u> get start-up equity funding $P_{t-1}Q_{t-1}$ and purchase capital $K_t=Q_{t-1}$
- **Beginning of** t: firm j has access to production technology

$$Y_t(j) = A_t(\omega_t(j)K_t(j))^{\alpha}N_t(j)^{1-\alpha}, \quad \text{where } \omega_t(j) = \left\{ egin{array}{ll} 0 & ext{with probability } \mu
ightarrow ext{Unproductive} \ 1 & ext{with probability } 1-\mu
ightarrow ext{Productive} \end{array}
ight.$$

Intermediate goods firms

$$\max_{N_t(j),K_t(j)} D_t(j) = \frac{p_t}{P_t} A_t(\omega_t(j)K_t(j))^{\alpha} N_t(j)^{1-\alpha} - \frac{W_t}{P_t} N_t(j) + (1-\delta)K_t(j) - (1+r_t^c)(K_t(j)-K_t)$$

Defining $r_t^k = \frac{p_t}{P_t} \frac{\alpha Y_t(j)}{K_t(j)} - \delta = \frac{p_t}{P_t} \frac{\alpha Y_t}{K_t} - \delta$ we obtain:

• Choices of an unproductive firm j with $\omega_t(j) = 0$:

$$\max_{\mathcal{K}_t(j)} r_t^q(j) \equiv rac{D_t(j)}{\mathcal{K}_t} - 1 = r_t^c - (r_t^c + \delta) rac{\mathcal{K}_t(j)}{\mathcal{K}_t}$$

• Choices of a productive firm j with $\omega_t(j) = 1$:

$$\max_{\mathcal{K}_t(j)} r_t^q(j) \equiv \frac{D_t(j)}{\mathcal{K}_t} - 1 = r_t^c + \left(r_t^k - r_t^c\right) \frac{\mathcal{K}_t(j)}{\mathcal{K}_t}$$

► Reallocation role

- Upon observing $\omega_t(j)$, firm j adjusts its capital from K_t to $K_t(j) \in \{K_t^u, K_t^p\}$:
 - (i) Unproductive firms sell their capital K_t and lend the proceeds on the credit market: $K_t^u=0$
 - (ii) Productive firms borrow and use the funds to buy $K_t^p K_t > 0$ units of capital
- ullet Credit market helps reallocate capital: $\mu K_t = (1-\mu)(K_t^p K_t) \Rightarrow$ textbook NK model

► Financial frictions

- Asymmetric Information: $\omega_t(j)$ is private information
- Limited Commitment: firm *j* may borrow, purchase capital goods, and abscond with them in search for yield
- \Rightarrow Borrowing limit is the same for all firms, and credit market is fragile

◆ Limited commitment only

▶ Financial fragility

• Incentive Compatibility Constraint:

An unproductive firm has two options:

- 1. Behave: sell its capital to lend the proceeds at equilibrium loan rate $r_t^c \rightarrow (1+r_t^c)K_t$
- 2. **Misbehave:** borrow to buy more capital $K_t^p K_t$ (i.e. mimic productive firms) and abscond $\rightarrow (1 \delta)K_t^p$

- ► Financial fragility
- Incentive Compatibility Constraint:

Unproductive firms lend iff the equilibrium loan rate r_t^c is high enough

$$\rightarrow \left\{ \begin{array}{l} (1+r_t^c)K_t \geqslant (1-\delta)K_t^p \\ \text{where } r_t^c \text{ satisfies } \mu K_t = (1-\mu)(K_t^p - K_t) \end{array} \Leftrightarrow r_t^c \geqslant \overline{r}^k \equiv \frac{\mu - \delta}{1-\mu} \right.$$

▶ Financial fragility

• Incentive Compatibility Constraint:

Unproductive firms lend iff the equilibrium loan rate r_t^c is high enough

$$\rightarrow \left\{ \begin{array}{c} (1+r_t^c)K_t \geqslant (1-\delta)K_t^\rho \\ \text{where } r_t^c \text{ satisfies } \mu K_t = (1-\mu)(K_t^\rho - K_t) \end{array} \Leftrightarrow r_t^c \geqslant \overline{r}^k \equiv \frac{\mu - \delta}{1-\mu} \right.$$

• Participation Constraint:

Productive firms borrow iff r_t^c is lower than their return on capital r_t^k

$$r_t^c \leqslant r_t^k \equiv \frac{\rho_t}{P_t} \frac{\alpha Y_t^p}{K_t^p} - \delta = \frac{\rho_t}{P_t} \frac{\alpha Y_t}{K_t} - \delta$$

▶ Financial fragility

• Incentive Compatibility Constraint:

Unproductive firms lend iff the equilibrium loan rate r_t^c is high enough

$$\rightarrow \left\{ \begin{array}{c} (1+r_t^c)K_t \geqslant (1-\delta)K_t^\rho \\ \text{where } r_t^c \text{ satisfies } \mu K_t = (1-\mu)(K_t^\rho - K_t) \end{array} \Leftrightarrow r_t^c \geqslant \overline{r}^k \equiv \frac{\mu - \delta}{1-\mu} \right.$$

• Participation Constraint:

Productive firms borrow iff r_t^c is lower than their return on capital r_t^k

$$r_t^c \leqslant r_t^k \equiv \frac{p_t}{P_t} \frac{\alpha Y_t^p}{K_t^p} - \delta = \frac{p_t}{P_t} \frac{\alpha Y_t}{K_t} - \delta$$

ullet Trade is possible iff the marginal return on capital $r_t^k \geq ar{r}^k$

◆ Credit market equilibrium

MP affects financial fragility in the short and medium run

• Condition for a crisis

$$\frac{\alpha Y_t}{\mathcal{M}_t K_t} \leqslant \frac{(1-\tau)(1-\delta)\mu}{(1-\mu)}$$

MP affects financial fragility in the short and medium run

• Condition for a crisis

$$\frac{\alpha \frac{\mathsf{Y}_t}{\mathcal{M}_t K_t}}{\mathcal{M}_t K_t} \leqslant \frac{(1-\tau)(1-\delta)\mu}{(1-\mu)}$$

• Short-run: through macro-economic stabilization \rightarrow Y- and \mathcal{M} -channels

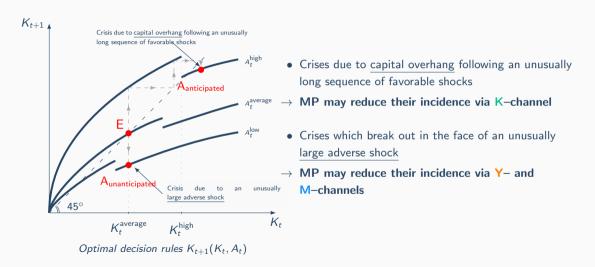
MP affects financial fragility in the short and medium run

• Condition for a crisis

$$\frac{\alpha \frac{\mathsf{Y}_t}{\mathcal{M}_t \mathsf{K}_t}}{\mathcal{M}_t \mathsf{K}_t} \leqslant \frac{(1-\tau)(1-\delta)\mu}{(1-\mu)}$$

- Short-run: through macro-economic stabilization \rightarrow Y- and \mathcal{M} -channels
- **Medium-run:** through capital accumulation → K–channel

Two polar types of crisis



Overview of the model

$$1 = \mathbb{E}_t igg[oldsymbol{\Lambda}_{t,t+1} ig(1 + \mathit{r}_{t+1} ig) igg]$$

3.
$$\frac{W_t}{R} = \chi N_t^{\varphi} C_t^{\sigma}$$

5.
$$\frac{W_t}{P_t} = \frac{\epsilon}{\epsilon - 1} \frac{(1 - \alpha)Y_t}{\mathcal{M}_t N_t}$$

7.
$$1 + i_t = \frac{1}{\beta} (1 + \pi_t)^{\phi_{\pi}} \left(\frac{Y_t}{Y} \right)^{\phi_y}$$

9.
$$\Lambda_{t,t+1} \equiv \beta \frac{C_{t+1}^{-\sigma}}{C_t^{-\sigma}}$$

11.
$$Y_t = A_t \left(\frac{\omega_t}{K_t} \right)^{\alpha} N_t^{1-\alpha}$$

13.
$$(1+\pi_t)\pi_t = \mathbb{E}_t\left(\Lambda_{t,t+1}\frac{Y_{t+1}}{Y_t}(1+\pi_{t+1})\pi_{t+1}\right) - \frac{\epsilon-1}{\varrho}\left(1-\frac{\epsilon}{\epsilon-1}\cdot\frac{1}{\mathcal{M}_t}\right)$$

$$2. \quad 1 = \mathbb{E}_t \bigg[\Lambda_{t,t+1} (1 + r_{t+1}^k) \bigg]$$

4.
$$K_{t+1} = I_t + (1 - \delta)K_t$$

6.
$$r_t^k + \delta = \frac{\epsilon}{\epsilon - 1} \frac{\alpha Y_t}{\mathcal{M}_t K_t}$$

8.
$$Y_t = C_t + I_t$$

10.
$$1+r_t=\frac{1+i_{t-1}}{1+\pi_t}$$

12.
$$\omega_t = \begin{cases} 1 & \text{if } r_t^k \ge \frac{\mu - \delta}{1 - \mu} \\ 1 - \mu & \text{otherwise} \end{cases}$$

Anatomy of financial crises

Quantitative analysis

- Quarterly parametrization. The only non–standard parameter is the share of unproductive firms. $\mu = 2.42\%$ to have the economy spend 8% of the time in crisis (with TR93 as baseline)
- Global solution and simulation of the (nonlinear) model over one million periods
- Study the dynamics 20 quarters around the beginning of a crisis. Baseline analysis with technology shocks only. Conclusions hold with both technology and demand shocks

Parametrisation

Parameter	Target			
Preferences				
β	4% annual real interest rate			
σ	Logarithmic utility on consumption			
φ	Inverse Frish elasticity equals 2			
χ	Steady state hours equal 1			
Technology	and price setting			
α	64% labor share			
δ	6% annual capital depreciation rate			
ρ	Same slope of the Phillips curve as with Calvo price setting			
ϵ	11% markup rate	10.000		
Aggregate 7	TFP shocks			
ρ_a	Persistence			
σ_{a}	Standard deviation of innovations (in %)	0.700		
Interest rate	e rule			
ϕ_{π}	Standard quarterly Taylor rule			
ϕ_y				
Proportion	of unproductive firms			
μ	The economy spends 8% of the time in a crisis	2.42%		

◀ TFP and Demand shocks

Average crisis dynamics and crisis variety

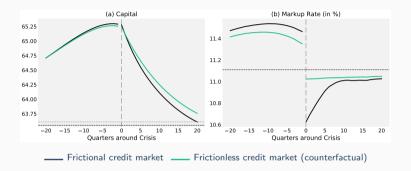


- Parameterized so that the economy spends 8% of the time in crises under the Taylor rule (TR93)
- → Most crises break out on the back of an investment boom
- → Few crises follow severe adverse TFP shocks

◆ Paths TFP shocks ◆ Paths TFP and demand shocks ◆ Paths demand shocks

"Precautionary savings" and "markup" externalities

► The case for policy intervention



- The household accumulates precautionary savings in anticipation of revenue losses
- Retailers frontload price increases in anticipation of inflationary pressures
- \Rightarrow Individual "hedging" behaviors precipitate the crisis via K– and M–channels

The price versus financial stability trade-off

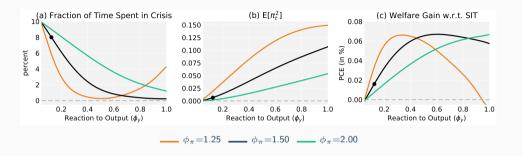
Responding to output lowers the crisis probability but increases price volatility

Rule	Crisis time (%)	Output loss (%)	$\mathbb{E}(\pi_t^2)$
SIT	9.85	-5.78	0.0000
TR93	8.00	-4.94	0.0064

◆ Full table ◆ AD shocks ◆ Output loss during GFC

Financial stability-price stability tradeoff

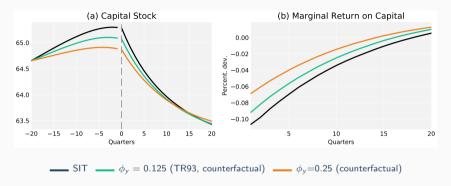
► Conventional parameter space



- One may reduce the time spent in crisis by responding systematically to output fluctuations alongside inflation...
- ullet ... but beyond a certain point, too much price volatility (\mathcal{M} -channel) can be detrimental to financial stability

Why is there fewer crises under TR93?

► A counterfactual experiment

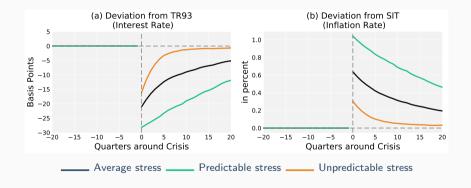


- Medium run: capital builds up more slowly under TR93 than under SIT
- Short run: TR93 cushions better the fall in r_t^k in the face of adverse shocks

IRFs

Two Policy Experiments

MP as backstop policy and MP normalisation path

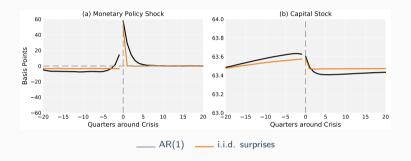


Backstop policies increase welfare

Rule	ϕ_y	Welfare loss (%)	BP time (%)	Length (quarter)	$\mathbb{E}(\pi_t^2)$
SIT	_	0.0013	15.16	8.84	0.0019
Taylor rules $(\phi_\pi=1.5)$	0.025 0.050	0.0012 0.0013	17.99 16.30	9.17 8.70	0.0011 0.0017
	0.125 0.250	0.0019 0.0044	11.81 6.30	7.45 5.93	0.0063 0.0196
	0.500 0.750	0.0117 0.0196	1.38 0.37	4.43 5.11	0.0196 0.0821

- Mix of SIT and backstop ("Fed put") reduces the welfare loss to 0.0012% (from 0.1114%)
- The financial sector is more fragile when backstopped though, which forces the central bank to intervene 15% of the time

Discretionarily keeping rates too low for too long may lead to a crisis



- ullet Discretionary deviations from TR93 ightarrow simulate the model with MP shocks only
- Crises occur after a "Great Deviation" (Taylor (2011))

Takeaways

Takeaways

- NK model with micro-founded endogenous financial crises:
 - → Monetary policy affects financial stability via Y–M–K channels
 - → Backstop policy effective but normalisation path depends on the nature of the stress
 - → Discretionary loose MP followed by abrupt reversal may lead to crisis
 - ightarrow Systematic response to output (eq SIT) improves both financial stability and welfare
- More in the paper on: the externalities that warrant MP bias toward FS, differentiated effects of supply and demand shock on financial stability
- <u>Still work-in-progress</u>: Calvo-type rigidities (better measure of welfare cost of price volatility)
- Future extensions (distinct papers): ZLB, macroprudential policy



Representative household

The representative household consumes a basket of goods C_t , works N_t , invests in public bonds B_t and in intermediate goods firm $j \in [0,1]$'s equity $P_tQ_t(j)$

$$\begin{split} \max_{C_t, N_t, B_t, Q_t(j)} & \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left[\frac{C_t^{1-\sigma}}{1-\sigma} - \chi \frac{N_t^{1+\varphi}}{1+\varphi} \right] \\ \text{s.t. } & \int_0^1 P_t(i) C_t(i) di + B_t + P_t \int_0^1 Q_t(j) dj \leq W_t N_t + (1+i_{t-1}) B_{t-1} + P_t \int_0^1 D_t(j) dj + \mathcal{X}_t \\ \end{split}$$

$$\begin{aligned} W_{t}/P_{t} &= \chi C_{t}^{\sigma} N_{t}^{\varphi} \\ C_{t}(i) &= (P_{t}(i)/P_{t})^{-\epsilon} C_{t} \\ 1 &= \beta (1+i_{t}) \mathbb{E}_{t} \left\{ (C_{t+1}/C_{t})^{-\sigma} (1/(1+\pi_{t+1})) \right\} \\ 1 &= \beta \mathbb{E}_{t} \left\{ (C_{t+1}/C_{t})^{-\sigma} (1+r_{t+1}^{q}(j)) \right\} \quad \forall j \in [0,1] \end{aligned}$$

where
$$C_t \equiv \left[\int_0^1 C_t(i)^{1-\frac{1}{\epsilon}} di\right]^{\frac{\epsilon}{\epsilon-1}}$$
, $\pi_{t+1} \equiv \frac{P_{t+1}}{P_t} - 1$ and $1 + r_{t+1}^q(j) \equiv \frac{D_{t+1}(j)}{Q_t(j)}$

Retailers

Monopolistic retailer $i \in [0,1]$ produces a differentiated final good using intermediate goods and sets its price subject to quadratic adjustment costs

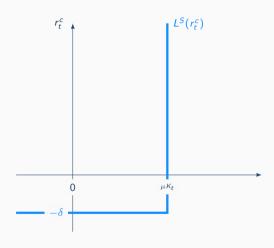
$$\begin{split} \max_{P_t(i),Y_t(i)} \mathbb{E}_0 \sum_{t=0}^{\infty} \Lambda_{0,t} \left[\frac{P_t(i)}{P_t} Y_t(i) - \frac{(1-\tau)p_t}{P_t} Y_t(i) - \frac{\varsigma}{2} \left(\frac{P_t(i)}{P_{t-1}(i)} - 1 \right)^2 Y_t \right] \\ \text{s.t. } Y_t(i) = \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} (C_t + I_t) \quad \text{where } I_t \equiv K_{t+1} - (1-\delta)K_t \end{split}$$

→ Price setting behavior

$$(1+\pi_t)\pi_t = \mathbb{E}_t\left\{\mathsf{\Lambda}_{t,t+1}\frac{\mathsf{Y}_{t+1}}{\mathsf{Y}_t}(1+\pi_{t+1})\pi_{t+1}\right\} - \frac{\epsilon-1}{\varsigma}\left(1-\frac{\mathcal{M}}{\mathcal{M}_t}\right)$$

where $\mathcal{M}_t = \frac{P_t}{(1-\tau)p_t}$ denotes the markup rate and $\mathcal{M} \equiv \frac{\epsilon}{\epsilon-1}$ its steady state. Markup \mathcal{M}_t will be important for the effect of MP on FS

▶ Frictionless case

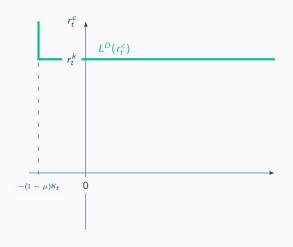


Unproductive firms' net loan supply

$$L^{\mathcal{S}}(r_t^b) = \begin{cases} \mu \mathcal{K}_t & \text{for } r_t^c > -\delta \\ (-\infty, \mu \mathcal{K}_t] & \text{for } r_t^c = -\delta \\ -\infty & \text{for } r_t^c < -\delta \end{cases}$$



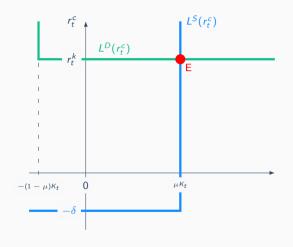
► Frictionless case



Productive firms' net loan demand

$$L^{D}(r_{t}^{b}) = \begin{cases} -(1-\mu)K_{t} & \text{for } r_{t}^{c} > r_{t}^{k} \\ [-(1-\mu)K_{t}, +\infty) & \text{for } r_{t}^{c} = r_{t}^{k} \\ +\infty & \text{for } r_{t}^{c} < r_{t}^{k} \end{cases}$$

▶ Frictionless case

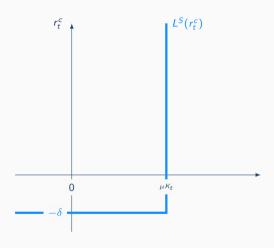


• In E, $r_t^k = r_t^c$ and capital is perfectly reallocated to productive firms:

$$\mu K_t = (1 - \mu)(K_t^p - K_t)$$

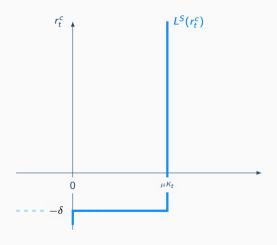
 Model boils down to the textbook NK model with one representative firm

▶ Frictional case



• Unproductive firms' net loan supply...

► Frictional case

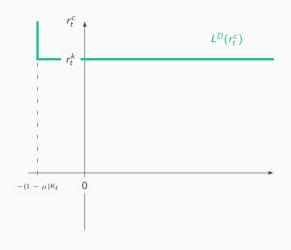


Unproductive firms' net loan supply...

... now with IC constraint

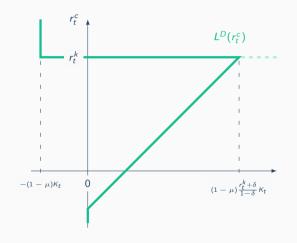
$$L^{S}(r_{t}^{b}) = \begin{cases} \mu K_{t} & \text{for } r_{t}^{c} > -\delta \\ [0, \mu K_{t}] & \text{for } r_{t}^{c} = -\delta \\ 0 & \text{for } r_{t}^{c} < -\delta \end{cases}$$

▶ Frictional case



• Productive firms' net loan demand...

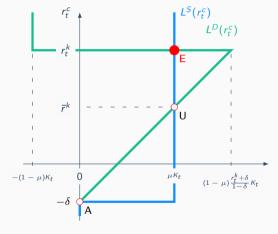
► Frictional case



Productive firms' net loan demand...
 ... now with IC constraint

$$L^D(r_t^b) = \begin{cases} -(1-\mu)K_t & \text{for } r_t^c > r_t^k \\ \left[-(1-\mu)K_t, (1-\mu)\frac{r_t^k + \delta}{1-\delta}K_t \right] & \text{for } r_t^c = r_t^k \\ (1-\mu)\max\{\frac{r_t^c + \delta}{1-\delta}, 0\}K_t & \text{for } r_t^c < r_t^k \end{cases}$$

► Frictional case

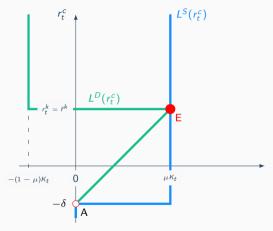


 Equilibrium E is the same as in the frictionless case and textbook model:

$$\mu K_t = (1 - \mu)(K_t^p - K_t)$$

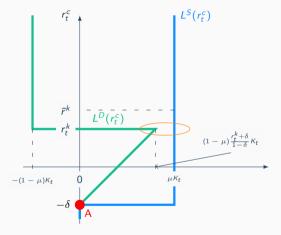
- $\bullet\,$ Aggregate outcome is the same in E and U
- Absence of coordination failure rules out equilibrium A

▶ Frictional case



\(\bar{r}^k\) is the minimum loan rate that ensures that all unproductive firms lend (i.e. there is no rationing)

► Frictional case



- \(\bar{r}^k \) is the minimum loan rate that ensures that
 \(\bar{all} \) unproductive firms lend (i.e. there is no rationing)
- When $r_t^k < \bar{r}^k$, there is excess supply and every unproductive firm left out has an incentive to borrow and abscond
- In this case, A (autarky) is the unique equilibrium

Perfect Information Case

- ► Incentive Compatibility Constraint
- Unproductive firms do not get any loan
- Productive firm js' borrowing limit is given by the incentive compatibility constraint

$$(1 - \delta)K_t(j) \le (1 + r_t^q(j))K_t = (1 + r_t^c)K_t + (r_t^k - r_t^c)K_t(j)$$

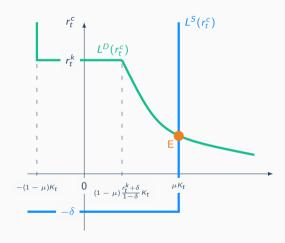
$$\Leftrightarrow K_t(j) - K_t \le \frac{r_t^k + \delta}{1 - \delta + r_t^c - r_t^k}K_t$$

$$\Rightarrow L^D(r_t^c) \equiv (1 - \mu)(K_t(j) - K_t) = (1 - \mu)\frac{r_t^k + \delta}{1 - \delta + r_t^c - r_t^k}K_t \quad \text{if } r_t^k \ge r_t^c$$

ullet Aggregate loan demand monotonically decreases with r_t^c

Perfect Information Case

▶ Credit Market Equilibrium (given r_t^k)



Aggregate outcome — Crisis versus normal times

• Crisis times: unproductive firms keep capital idle and capital mis-allocation lowers TFP

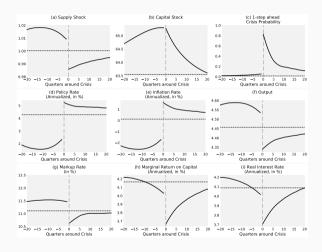
$$Y_t = A_t \left((1 - \mu) K_t \right)^{\alpha} N_t^{1 - \alpha}$$

• Normal times: capital is perfectly reallocated (as in the credit-frictionless economy)

$$Y_t = A_t K_t^{\alpha} N_t^{1-\alpha}$$

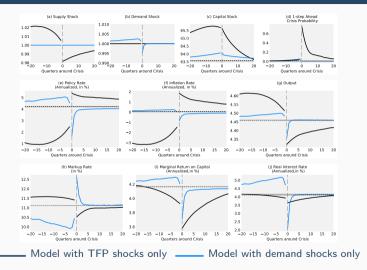
Anatomy of the average crisis

► Technology shocks



Anatomy of the average crisis

► Technology versus demand shocks



Should the central bank deviate from SIT to foster FS?

	ϕ_y	Welfare Loss CEV (%)	Frictional credit market				
Rule			Welfare Loss CEV (%)	Crisis time (%)	Length (quarter)	Output loss (%)	$\mathbb{E}(\pi_t^2)$
SIT	_	0	0.1114	9.85	5.91	-5.78	0.0000
	0.025	0.0000	0.1198	10.47	5.94	-5.75	0.0004
	0.050	0.0001	0.1137	9.87	5.80	-5.53	0.0012
or rules	0.125	0.0009	0.0964	[8.00]	5.31	-4.94	0.0064
= 1.5)	0.250	0.0037	0.0706	5.00	4.58	-4.24	0.0200
Taylor $(\phi_{\pi} =$	0.500	0.0116	0.0466	1.39	3.64	-3.16	0.0516
	0.750	0.0197	0.0467	0.45	4.49	-2.45	0.0817

Should the central bank deviate from SIT to foster FS?

	ϕ_y	Welfare Loss CEV (%)	Frictional credit market				
Rule			Welfare Loss CEV (%)	Crisis time (%)	Length (quarter)	Output loss (%)	$\mathbb{E}(\pi_t^2)$
SIT	_	0	0.1114	9.85	5.91	-5.78	0.0000
	0.025	0.0000	0.1198	10.47	5.94	-5.75	0.0004
	0.050	0.0001	0.1137	9.87	5.80	-5.53	0.0012
or rules $= 1.5$	0.125	0.0009	0.0964	[8.00]	5.31	-4.94	0.0064
	0.250	0.0037	0.0706	5.00	4.58	-4.24	0.0200
Taylor $(\phi_{\pi} =$	0.500	0.0116	0.0466	1.39	3.64	-3.16	0.0516
	0.750	0.0197	0.0467	0.45	4.49	-2.45	0.0817

AS and AD shocks

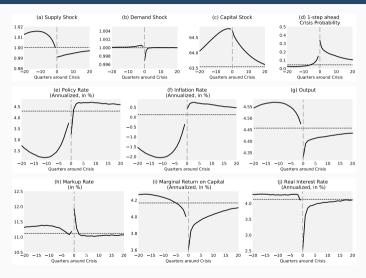
▶ Parametrization

Parameter Target	Value					
Aggregate risk-premium shocks						
ρ_z As in Smets and Wouters (2007)	0.220					
σ_z	0.230					
Proportion of unproductive firms						
μ $$ $$ The economy spends 8% of the time in a crisis	2.39%					

◆ Back to parametrization

AS and AD shocks

► Anatomy of the average crisis



With AS and AD shocks

▶ Crisis statistics

	Crisis time (%)	Output loss (%)
Economy with both shocks	[8.00]	-3.20
Economy with TFP shocks only	3.42	-4.76
Economy with demand shocks only	0.00	-2.90

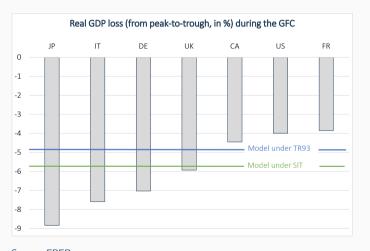
AS and AD shocks

▶ Welfare

	ϕ_y	Frictionless Welfare loss CEV ^{FB} (%)	Frictional credit market				
Rule			Welfare loss CEV ^{FB} (%)	Crisis time (%)	Length (quarter)	Output loss (%)	$\mathbb{E}(\pi_t^2)$
SIT	_	0	0.1114	9.85	5.91	-5.78	0.0000
	0.025 0.050	0.0116 0.0093	0.1566 0.1396	13.11 11.74	1.75 1.77	-4.06 -3.77	0.0006 0.0014
	0.125	0.0062 0.0064	0.0980 0.0583	[8.00] 3.93	1.78 1.75	-3.20 -2.71	0.0065
Taylor	0.500	0.0126 0.0203	0.0298 0.0337	0.46 0.04	1.46 1.18	-2.10 -1.53	0.0524

Peak-to-trough GDP fall during the GFC

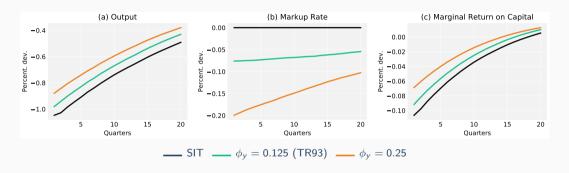
▶ A success of the model



Source: FRED

Short Run Effects

► Impulse Response Function to a Negative TFP shock

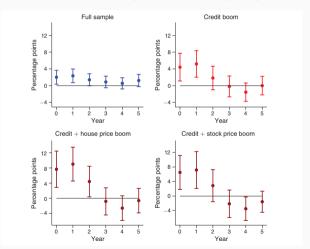


◆ Back to counterfactuals and IRFs

Schularick at al (2021)

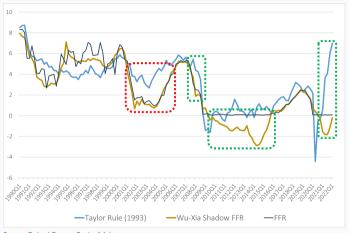
► Leaning against the wind and crisis risk

Effect on annual crisis probability of an unexpected 1 pp policy rate hike



"Based on the near-universe of advanced economy financial cycles since the nineteenth century, we show that discretionary leaning against the wind policies during credit and asset price booms are more likely to trigger crises than prevent them".

Deviation from Taylor (1993) rule and shadow policy rate



Source: Federal Reserve Bank of Atlanta

MP has likely prevented a financial crisis during the Covid-19 pandemic

