Identity-Based Elections

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Abstract

It is hypothesized that Bayesian individuals choose their news media with the goal of preserving their political identity and that this will have electoral implications. They are also exposed to outside information shocks, which they try to counteract. When those information shocks are unbiased, substantial political advantage may accrue to a political camp if its members are less exposed to them, which may be sufficient to swing an election regardless of the state of the world. The same result occurs if those individuals incorrectly believe that the information shock is imprecise or biased against them. Propaganda, i.e. biased official media, is beneficial to autocratic regimes only if other media sources are censored or if citizens are unaware of its bias.

JEL codes: D72, D83, D90
Keywords: Behavioral Voters, Belief-based Utility, Information Aggregation

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1 Introduction

“More often than not, citizens do not choose which party to support based on policy opinion; they alter their policy opinion according to which party they support.” Lilliana Mason (2018)

In the era of the Internet, people can choose from a plethora of possible news sources. Although traditional mainstream news sources continue to exist, many new ones have emerged in just the past two decades. Figure 1, which is taken from Benkler et al. (2017), maps the sharing on Twitter of 1.25 million news articles from 25,000 outlets. This richness of the media landscape has allowed people to more precisely tailor their media choices to their preferences. However, the incredible diversity of viewpoints on offer, combined with new technologies, has also facilitated the formation of “echo chambers” or “filter bubbles” which insulate people from possibly contrary perspectives offered by traditional media outlets.

Figure 1: Pattern of news sharing on Twitter

At the same time, trust in traditional media has declined markedly over the past two decades. This distrust has developed along radically different paths on each side of the political spectrum, particularly during the last five years in the U.S. As can be seen in figure 2 below, the level of trust in mainstream media differs dramatically between Republicans and Democrats.
Indeed, based on Pew Foundation opinion polls reported in Jurkowitz et al. (2020), “one of the clearest differences between Americans on opposing sides of the political aisle is that large portions of Democrats express trust in a far greater number of news sources.”

These two phenomena — the emergence of a dense array of media outlets and partisan distrust of mainstream media — are likely to be having an impact on the formation and updating of political beliefs, and as a consequence, may be influencing voter decisions. But can this new information environment generate aggregate beliefs biased enough to swing an election?

In the U.S., the influence of the above-mentioned phenomena on electoral outcomes is compounded by the particularly polarized landscape, in which traditional ideological, religious, and racial affiliations are being replaced by overlapping meta-identities that align almost entirely along party lines. Citizens have become less responsive to new information.

1For instance, as noted in Benkler et al. (2017) and illustrated in figure 1, during the 2016 US presidential campaign, “Pro-Clinton audiences were highly attentive to traditional media outlets, which continued to be the most prominent outlets across the public sphere, alongside more left-oriented online sites. But pro-Trump audiences paid the majority of their attention to polarized outlets that have developed recently, many of them only since the 2008 election season. [...] Breitbart News became the center of a distinct right-wing media ecosystem, surrounded by Fox News, the Daily Caller, the Gateway Pundit, the Washington Examiner, Infowars, Conservative Treehouse, and Truthfeed. Lee (2010) finds that trust in media is negatively correlated with conservatism and Republican-leaning views. Pennycook & Rand (2019) note that Democrats trust mainstream news more than Republicans, with the difference ranging between 11.5 and 14.7 percent. According to Jones (2004), “…only 16.5 percent of Democrats (including Democratic-leaning independents) can be classified as media skeptics compared with nearly 40 percent of Republicans and Republican-leaning independents.”
tion about national issues, as if political affiliations determine what information people absorb, rather than the other way around (see, for instance, Mason (2018) and Kahan (2017)).

Given this situation, we propose a model in which media choices are driven by political identity, which is a broader, though at the same time weaker, concept of political partisanship. In other words, voters try to preserve their political identity but may not always succeed in doing so. Media choice is modeled in an environment where the agent may also be exposed to information shocks from outside her chosen set of media outlets. We assume that an individual chooses specific media to follow, but is to some extent also exposed to the outside world, namely the broader media environment which she does not explicitly choose. We refer to the latter as Outside media and the former, namely, media that individuals choose, in full awareness of their bias, as Inside media.

We study a variety of situations by making various assumptions about the Outside media. In the context of a liberal democracy, such as the U.S., individually chosen outlets often have some political bias, while the outside mainstream media landscape, on the whole, is generally considered to be vibrant and free of systematic bias. Thus, in our benchmark case, we assume that Outside information which individuals are involuntarily exposed to originates from a relatively unbiased source. However their exposure to Outside media, or their beliefs regarding bias or degree of precision may vary. By contrast, in an illiberal democracy, the media landscape is influenced by the regime, such that the structure generating Outside information is assumed to be biased. In our benchmark case, we consider environments in which this bias and the degree of precision is common knowledge. But we also show that the model easily extends to “motivated reasoning” environments in which some or all citizens hold incorrect beliefs about the bias or precision of the Outside media.

The core setup of the model is decision-theoretic and fairly straightforward. Individuals receive two pieces of news: one from the exogenous Outside media (the shock) and one from the Inside media, i.e., media endogenously chosen by the citizen. In liberal democracies such as the US, the different levels of exposure to Outside information means that it is noisier for some individuals than for others and therefore affects their beliefs to a lesser extent. We take this heterogeneous level of exposure to be exogenous and determined by basic long-term preferences, such as, urban (more exposed) versus rural (less exposed) lifestyle choices. The Inside media source is by contrast a choice made in a

\[\text{It is difficult to define mainstream media in the current rapidly evolving media environment. Broadly speaking, we use the term to refer to traditional corporate legacy outlets which employ standard fact-checking processes and try to responsibly synthesize and diffuse the best information available.}\]
self-serving behavioral way, as explained below. Crucially, individuals are fully rational in the way they process information, in that they update their beliefs based on the two signals. They then choose between the candidates according to their rational posterior beliefs. In sum, the election aggregates all votes, each of which is based on two conditionally independent signals about the candidates. Our goal is to determine whether information aggregation fails in such elections, and if so, why.

The model’s key behavioral assumption does not relate to information processing, but rather the preferences that drive the choice of Inside media. How we model the media is also a key innovation. Each Inside media choice is a particular known signal structure (under commitment). We assume that an individual identifies with a particular party, either on the Left or the Right, and wishes to preserve their political identity. They choose Inside media in order to maximize the likelihood that once they have consumed all the available information, they will conclude that the party they already identify with better matches the state of the world. In other words, individuals make their media choice in order to shield themselves from news that is potentially unfavorable to their political identity.

Equivalently, one can think of agents as having two selves — an emotional self (heart) and a rational self (mind). The heart chooses Inside media in order to preserve the individual’s political identity, whereas the mind processes all the information it receives rationally and votes for the party it believes to be superior. The objective of the heart could alternatively be to persuade the mind to vote for the heart’s preferred party, while the mind simply prefers to vote for the correct party. Under our baseline preferences, agents do not want to determine the true state of the world, rather they wish to conclude that the true state more likely matches their heart’s disposition. This is a rational choice model in which rationality is the constraint and the objective is the value of the posterior. That is, there is motivated information acquisition, but no motivated reasoning. One can think of our agents as partisan voters, albeit in a weak sense: they want to vote for their preferred party but they may not succeed in doing so because of their rational side.

Our goal is to propose an innovative model of electoral outcomes based on what we believe are timely and often neglected features of modern society. This involves a novel way of thinking about elections in the current environment in which political identity has become dominant and media choices are plentiful and polarized. This model is broad

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3 Inside media choice can be viewed as a long-term loyalty to particular outlets rather than one that is instrumental to voting in a specific election (such that the utility is not derived from the voting itself but rather purely from ex-post beliefs). Alternatively, the choice of Inside media can be thought of as being made instrumentally in the context of a particular election, in which case we can think of agents as deriving explicit utility from being able to vote sincerely for the party they are aligned with.
enough that it can be used to study winning margins and information aggregation in a variety of contexts that assume heterogeneity in several dimensions, i.e. distribution of identities, priors, exposure or trust in mainstream/Outside media, misspecified beliefs, and alternative forms of democracy.

In what follows, we will present some specific and very simple applications. For example, in order to highlight the electoral consequences of variation in exposure to mainstream media along partisan lines, we present our benchmark results for a setup in which the two sides are perfectly symmetric, except in the extent to which they are exposed to information from mainstream media. Thus, the type of media they actively choose (i.e., Inside media) can vary dramatically, which may result in a substantial electoral advantage for the side less exposed to mainstream media. In the following example, we examine this possibility, assuming that each citizen votes for the party she rationally believes to be superior.

**Illustrative example:** Assume a symmetric benchmark in which an equal proportion of countably infinite voters have partisan affiliations, referred to as left (L) and right (R). There are two equally likely states of the world (ω ∈ {L, R}), differentiated by which of the two candidates is superior. The only asymmetry between the two sides is that the left is more exposed to Outside media than the right. Assume, for instance, that the left-wing individuals receive i.i.d. symmetric binary signals from the Outside media with precision $t_L = 0.75$, while right-wing individuals receive noisier Outside signals, with precision of only $t_R = 0.51$. As a baseline, we consider electoral outcomes in the absence of Inside media — that is, when the agent is only exposed to an Outside signal. The winning margin and winning probability for the R-side are then as follows:

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<th>Ex-Ante</th>
<th>ω = R</th>
<th>ω = L</th>
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<tbody>
<tr>
<td>R Win Margin</td>
<td>0%</td>
<td>+26%</td>
<td>-26%</td>
</tr>
<tr>
<td>R Win Prob</td>
<td>50%</td>
<td>100%</td>
<td>0%</td>
</tr>
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Thus, asymmetric exposure to mainstream media generates symmetric electoral outcomes. In this baseline case, the superior candidate is always elected, i.e., information is perfectly aggregated. No personal media choice is made by citizens, and thus political identity, whether R or L, plays no role.

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4The main results are qualitatively unchanged even if we assume that an individual votes for the party she is culturally affiliated with only if she believes it is the superior party and abstains otherwise. In this case, all winning margins will simply be halved. We assume infinite population size, and therefore being pivotal is not a concern for voters.
Now suppose that individuals can also optimally select Inside media sources. In this case, their voting decision is made after having rationally updated their beliefs based on two signals, rather than one. If the media is chosen in order to maximize the chance of preserving their political identity, then the outcome of the election is no longer symmetric. In fact, it may be drastically skewed. In this example, the winning margin and winning probability of the R-side are as follows:

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<thead>
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<th>Ex-Ante</th>
<th>$\omega = R$</th>
<th>$\omega = L$</th>
</tr>
</thead>
<tbody>
<tr>
<td>R Win Margin</td>
<td>+29%</td>
<td>+56%</td>
<td>+2%</td>
</tr>
<tr>
<td>R Win Prob</td>
<td>100%</td>
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In this case, the R-side has not only an ex-ante winning margin advantage, but surprisingly, also an ex-post advantage. In other words, the R-side wins the election in either state of the world in this example and information is not aggregated, despite the fact that individuals vote solely on the basis of the information they have received and which was used to rationally update their beliefs.

Identity-R agents are less exposed to the information shock and optimally choose a qualitatively different Inside media source than Identity-L agents who must contend with a more precise information shock. Importantly, in a world without a rich set of signal structures (Inside media) to choose from — even if partisan biases still drive media choice — we would not see such stark aggregate electoral bias as in the example above. Since this result is not knife-edge, party R would win regardless of the state of the world even if there were slightly more identity-L agents than identity-R, or when the prior leans towards the L side.

**Structure of the paper.** In Subsection 1.1, we note how our paper builds on and contributes to various strands of literature. We develop the building blocks of our model in Section 2 by solving the problem of a single agent. This allows us to highlight some novel aspects of the model, namely the preferences and the conceptualization of media.

The influence of individual media choices aggregated to determine electoral outcomes constitutes the core of the analysis. In Section 3, we illustrate the flexibility and strength of this model by considering electoral outcomes in several distinct contexts. In Subsection 3.1, we suppose that the two political sides are exposed unequally to the information shock. Here, we build on the example above in showing that the region of information aggregation failure is a salient subset of parameters. Further, we show that the result of information aggregation failure is robust to considering non-common priors, gain from


learning the truth, correlated signals, etc.

We consider media distrust in Subsection 3.2. It is modeled as a cognitive bias, in that the Outside signal is unbiased and moderately precise, but citizens on one side (mistakenly) believe either that it is *imprecise* (Subsection 3.2.1) or that it is *biased against their side* (Subsection 3.2.2). This is of particular interest since it may apply to some liberal democracies, such as the US (see figure 2). In this subsection, we show that significant political advantage accrues to the side that (wrongly) believes that the mainstream media, as a whole, is either imprecise or biased against them. This result is robust to our interpretation of distrust and may provide one rationale behind the fomenting of distrust in mainstream media by some politicians.

Our modeling strategy, which is based on the dichotomy between Inside media and Outside media, can also be used to explore other important questions. We initially assume that the Outside media is unbiased, but allowing it to be biased makes it possible to consider government propaganda. In Subsection 3.3, we, therefore, imagine a propaganda regime. In Subsection 3.3.1, we study a media censorship regime, where the biased Outside media is the only media available. Here, propaganda can benefit the government. However, as we show in Subsection 3.3.2, if citizens are able to consume chosen Inside media, then propaganda is not just ineffective, it may backfire completely in favor of the anti-government side. This reversal is striking and occurs because individuals from both political camps choose qualitatively different Inside media. Further, in Subsection 3.3.3, we show that if citizens are unaware of the bias in the Outside signal, then propaganda may benefit the government. This provides a rationale for why authoritarian governments invest so much in their propaganda machine. Propaganda may succeed if the electorate remains unaware of government influence on the media, or when it is paired with censorship.

The nature of partisanship we consider in this model, i.e., political identity preservation, is fundamentally different from earlier conceptualizations of partisanship. Thus, instead of a bias in the utility function, location of ideal points, or behavioral types, we study an agent who is partisan in the beliefs she *wants* to hold. She would like to believe that her party is the better party. We highlight this contribution of the paper in Subsection 3.4. Section 4 concludes. All the proofs are detailed in the Appendix.

1.1 Related Literature

Given the novelty of the model we consider, our analysis does not fit neatly into one subliterature. Rather, it lies at the intersection of various strands of literature. Below, we
provide an overview of the papers and topics we build on and contribute to.

**Information biases and politics.** Biases in the processing of information influence electoral outcomes in [Levy & Razin (2015)](#) and [Ortoleva & Snowberg (2015)](#). The source of bias in both their models is correlation neglect, according to which individuals underestimate the correlation between their information sources. Although we also use a simple decision-theoretic problem aggregated to derive expected electoral outcomes, the behavioral bias in our benchmark case is not cognitive but rather it resides in the preferences that drive information acquisition. Specifically, agents rationally update using all the information they receive.

**Belief-based utility.** The tradition of models with agents deriving utility from their beliefs goes back to [Akerlof & Dickens (1982)](#) who incorporate beliefs explicitly in the decision maker’s utility function. In their framework, beliefs are a choice variable, whereas, in our case, beliefs are a stochastic outcome of choosing a particular signal structure. This growing literature includes [Caplin & Leahy (2001)](#) and [Brunnermeier & Parker (2005)](#), in which belief-based utility drives agents’ actions. [Bénabou & Tirole (2016)](#) provide a survey of the main findings that emerge from economic models of motivated beliefs.

Though cast in a different context, our model has a similar flavor to the [Köszegi (2006)](#) model of overconfidence, in which agents are unbiased in their beliefs (since they start from a correct prior and update rationally) but end up with a systematic bias in their choice due to the bias in their information collection process. Intuitively, agents derive intrinsic utility from believing that “something” is the case (specifically, that they have superior ability in some task, as in Köszegi’s case, or that their party is superior, as in our case), and therefore they tend to collect information that preserves those beliefs as often as possible.

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For a survey of the recent literature on the electoral outcomes under these and similar cognitive biases, see [Levy & Razin (2019)](#). This literature continues to grow (see, for example, [Little et al. (2020)](#) on motivated reasoning cognitive bias). [Gentzkow et al. (2021)](#) find that small ideological differences in the extent of trust in information sources and in beliefs about the state of the world can result in a polarized electorate.

Motivated reasoning to preserve political identity is similar in spirit to minimizing cognitive dissonance, the electoral implications of which are considered in [Acharya et al. (2018)](#). The objective of preserving one’s political identity is also consistent with findings in a large strand of the psychology literature, which primarily looks at cognitive biases (unlike our model). [Sherman & Cohen (2006)](#) note that biases in the assimilation of information can be generated from the motivation to maintain and protect political identity. Motivated reasoning as a way of preserving political identity is also noted by [Kahan (2017)](#) and [Kahan & Braman (2006)](#). Furthermore, the ability to explicitly deliberate does not mitigate this phenomenon according to [Kahan (2012)](#) who finds that cognitive reflection exacerbates ideologically motivated reasoning. [Kaanders et al. (2022)](#) conduct an experiment with active information sampling and find that individuals are more likely to choose information that allows them to preserve their beliefs, which is consistent with
Information aggregation. Like Feddersen & Pesendorfer (1996) and Feddersen & Pesendorfer (1997) and the rich literature in their wake, our goal is to understand the aggregation of information held by differently informed voters. We propose a broader notion of partisanship which blurs the dichotomy between partisan voters (who vote in one way regardless of their beliefs or the state of the world) and non-partisans (who just want the correct electoral outcome) which is typical of previous models. In our model, all voters are partisans, albeit in a weaker sense; that is, they have an allegiance to a specific candidate, but (depending on the realization of the state, their prior, and their exposure to the outside world) they may or may not succeed in convincing themselves to vote for her. While aggregate welfare measures are tricky given our preferences, the question of correct information aggregation in elections is well-posed since all information received is processed in a purely Bayesian manner by all voters.

Bayesian Persuasion. As in recent work on this topic, we apply Bayesian persuasion techniques to political economy. Our focus is on conditionally aggregating individual decisions in a large population of individuals. In order to do so, we adapt and distill results developed by Kolotilin (2018) who builds on Kamenica & Gentzkow (2011). Kolotilin requires the sender to choose an information structure while being uncertain about the receiver’s type. This is similar to our agent’s problem of choosing an information structure while bracing for an Outside signal. Lipnowski & Mathevet (2018) consider an information design problem with a benevolent sender who chooses a signal structure for a receiver with psychological preferences, an approach with similarities to our model of information choice by agents who derive belief-based utility.

Media and politics. Our model assumes that citizens can choose their Inside media from a dense distribution of sources, spanning all possible biases. The innovation lies in the fact that media are passive and non-strategic information senders with commitment, i.e., bias is known, and media consumption is demand-driven only. Motivated by the fast-changing media landscape, there is a burgeoning literature that examines media bias —

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7 The literature on potential failure of information aggregation is vast and includes Razin (2003), Callander (2008), Acharya (2016), Ekmekci & Lauermann (2020), and Barelli et al. (2022).

8 There has recently been a great deal of effort in applying information design to political environments including Edmond (2013), Cotton & Li (2018), Gratton & Lee (2022), Luo & Rozenas (2022), Innocenti (2022), Heese et al. (2019), and Prato & Turner (2022).

9 Kolotilin et al. (2017) establish the equivalence of implementation by persuasion mechanisms, which can condition the signal structure on the type of the receiver, and implementation by experiments, which are unconditional on the receiver’s type.
albeit usually from the supply side — in which media behave strategically. This includes Gentzkow & Shapiro (2006), Mullainathan & Shleifer (2005), Bernhardt et al. (2008), Chan & Suen (2008), Hu et al. (2019), Gitmez & Molavi (2022), and Perego & Yuksel (2022). In a similar vein, politicians can also influence the media or manipulate the information available to voters, as in for instance Gehlbach & Sonin (2014), Aköz & Arbatlı (2016), Alonso & Cámara (2016), and Kolotilin et al. (2022).

Our theoretical results are consistent with a number of empirical studies, such as DellaVigna & Kaplan (2007) and Martin & Yurukoglu (2017) which show that the introduction of new (and largely conservative) media outlets has resulted in a persistent and significant increase in Republican vote share. The absence of a systemic partisan bias in recognizing fake news, as shown by Angelucci & Prat (2021), indicates the absence of systemic partisan cognitive differences. Broockman & Kalla (2022) find that the political views of partisans are malleable, indicating that while voters have partisan preferences, they update beliefs based on the information they receive. An overview of the recent literature on populism and identity politics is provided by Guriev & Papaioannou (2022).

2 The single agent model

Suppose there are two states of the world (R and L), which indicate which of the political parties (R or L) is superior. An agent is either identity-R or identity-L, which indicates her political affiliation. We begin by considering the problem for a single identity-R agent. The problem and solution for an identity-L agent are analogous.

Preferences. The identity-R agent identifies with party R. She gains utility if she is able to believe that party R is at least as good as party L. In this model, this is equivalent to a posterior belief that the state of the world is R with a probability of at least one-half. Specifically, her utility equals one (\(U_R = 1\)) if her posterior belief is weakly favorable to her party (\(P[\omega = R|\text{signals}] \geq 0.5\)) and zero otherwise.

Timing. The agent is born with some priors regarding the state of the world. First, she chooses the information source from which she would like to receive a signal. Next,

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10 Polarization can even occur without media bias or political control of media, through the selective sharing of information by voters (with misspecified learning) amongst themselves, as seen in Bowen et al. (2023).

11 There is a vast literature on the importance of political identity for individuals. See, for instance, Mason (2018). The notion of political identity preservation is closely related to ego utility which is studied in Köszegi (2006).
the state of the world is realized. She then receives two signals that update her beliefs. One is from the chosen source (Inside media), and the other is an information shock that she is exposed to (Outside media). Finally, she forms Bayesian posteriors and realizes utility. Her problem is to select the structure of the chosen source so as to maximize the chances of preserving her political identity given her prior and anticipating her exposure to an informational shock. Her desire to preserve her political identity influences the way she acquires information and, as shown in Section 3, leads to interesting aggregate electoral outcomes.

An alternative but equivalent setup supposes that an identity-$R$ agent has two selves: a sender and a receiver. The sender-self selects the chosen media. The receiver-self observes the signal generated by the chosen media as well as an information shock. She then votes sincerely. The objective of the sender-self is to maximize the likelihood that the receiver-self votes for party $R$. For simplicity of illustration, we formulate the individual’s problem such that she realizes belief-based utility.

The agent’s objective can be expressed as:

$$E[U_R] = P[P[\omega = R|S, s] \geq 0.5]$$  \hfill (1)

where $S$ is the signal generated by the chosen media (Inside signal structure), while $s$ is the information shock (a signal generated by the Outside signal structure). The agent’s problem is to choose an Inside signal structure that maximizes equation 1.

**Conceptualization of media.** The conceptualization of an individual’s information environment is a novel aspect of our paper and is a key contribution. In a rich media landscape, an individual can choose from outlets with a wide range of political slants. The Inside signal structure is a finite set of signals ($S = \{S_1, S_2, ..., S_n\}$) that are correlated with the state of the world. No restrictions are imposed on the agent’s choice of the Inside signal structure except that it must abide by the Martingale property, namely the expected posterior must equal the prior. We interpret this choice of signal structure as the combination of news outlets from which the agent chooses to receive information.

The diverse set of signal structures represents the rich media landscape in which voters

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12 Kaanders et al. (2022) show that information sampling can be motivated by a desire to preserve beliefs. That political identity preservation can motivate reasoning is documented in Kahan & Braman (2006) and Kahan (2017), among others.

13 Since we allow for a rich structure, the possibility that the agent consumes news from several different outlets is subsumed within our model. Any distribution of posteriors generated by multiple Inside signals can be generated by an appropriately designed single signal structure.
currently gather information. Furthermore, an agent can choose a news media (a signal structure), but not the programming (the realization of a signal).

We also allow for the possibility that individuals might not be able to completely isolate themselves from sources they haven’t chosen. The identity-\(R\) agent is involuntarily exposed to an information shock (Outside signal) with the following structure:

\[
P[s = l|\omega = L] = P[s = r|\omega = R] = t_R
\]

where \(t_R \in [0.5, 1]\) is the precision of the Outside signal. We interpret the structure of the information shock as reflecting the nature of the media environment as a whole. This structure is one we would expect in a liberal democracy in which each individual outlet may have a political slant but the media, as a whole, is vibrant and free. In other words, the Outside signal structure in a liberal democracy is unbiased. The model is nonetheless amenable to more general structures of the information shock.\(^{14}\)

The individual holds beliefs over the structure from which the information shock is generated and selects her chosen media accordingly. In the next subsection, we study the individual’s strategic choice of the Inside signal structure in order to possibly counteract the information shock generated by the Outside signal structure.

### 2.1 Solution of the individual’s decision problem

The solution of the individual’s problem is simply a distillation of the techniques developed in Kamenica & Gentzkow (2011) and Kolotilin (2018). We first calculate the agent’s expected utility as a function of her interim priors, namely after she has received the Inside signal but before she has received the information shock (the Outside signal). We denote this interim posterior as \(P[\omega = R|s_i]\). We will obtain the agent’s optimal signal structure choice as a function of the precision of her information shock.

In figure 3, we plot an identity-\(R\) agent’s expected utility (which is the likelihood of preserving her political identity) as a function of her interim posterior for an Outside signal structure, such that the precision of the Outside signal \((t_R)\) is 0.75. For values of the interim posterior between 0 and 0.25, regardless of the realization of the Outside signal,\(^{13}\)

\(^{14}\)The model provides the flexibility to consider environments in which the media, as a whole, is biased or believed to be biased. We interpret that bias by means of an Outside signal structure in which \(P[s_R = l|\omega = L] \neq P[s_R = r|\omega = R]\). An incorrect belief regarding the bias of the Outside signal is interpreted as a form of distrust in the media (see Subsection 3.2.1). We believe that a biased Outside signal can occur when one political side can influence the mainstream media as a whole. We study that scenario in Subsection 3.3. @HH: I want to remove this footnote. It seems repetitive now that we describe the structure before the lit section. What do you think?
the agent is unable to preserve her political identity. If the agent has an interim posterior equal to 0.25, and if she receives a favorable Outside signal, then her posterior expectation that the state of the world is $R$ is equal to 0.5, and she is just able to preserve her political identity. For values of interim posteriors between 0.25 and 0.75, she can preserve her political identity if she receives a favorable Outside signal, $s = r$. The likelihood that she receives a favorable Outside signal increases with her expectation that the state of the world is $\omega = R$. Finally, if the agent’s interim posterior is at least 0.75, then she is able to preserve her political identity regardless of the Outside signal.

**Partisanship and political identity preservation: an aside.** An agent in our model would exhibit partisan behavior if she were born with priors that allowed her to preserve her political identity regardless of any information shock. In that case, she would optimally choose an uninformative Inside signal structure and if there were an election, she would always vote for her preferred party. However, for intermediate priors and in the presence of information shocks, agents need to persuade themselves in order to preserve their political identity. While they choose media optimally in order to maximize their likelihood of preservation of political identity, they cannot always achieve that objective. The concept of political identity preservation that we develop is, therefore, both weaker and broader than partisanship and constitutes a novel contribution to the literature.

**A sufficient set of signals.** For parsimony, we assume that the agent is born with a prior that the two states of the world are equally likely ($\mathbb{P}[\omega = R] := w = 0.5$). As we show in
Appendix A, three interim posteriors are key to solving the agent’s problem. The first is an interim posterior such that the agent is just able to preserve her political identity in the event of an unfavorable Outside signal ($P[\omega = R|S_i] = 0.75$ in figure 3). We refer to an Inside signal that generates such an interim posterior as a Good ($G$) signal. The second is an interim posterior that allows the agent to just preserve her political identity only if she receives a favorable Outside signal ($P[\omega = R|S_i] = 0.25$ in figure 3). We refer to an Inside signal that generates such an interim posterior as a Bad ($B$) signal. The third is an interim posterior such that the agent is certain that the state does not match her political identity ($P[\omega = R|S_i] = 0$). We refer to an Inside signal that generates such an interim posterior as a Terrible ($T$) signal. Any signals other than the three described above — Good, Bad, and Terrible — are suboptimal. Furthermore, we show that two signal structures, $GT$ and $GB$, are sufficient to solve the agent’s problem.

In figures 4(a) and 4(b), we plot the agent’s expected utility as a function of her interim posterior after observing the Inside signal and before observing the Outside signal. For lower values of precision, as in figure 4(a), the concave closure of the expected utility function is such that it would be optimal for the agent to choose a signal structure that mixes between $G$ and $T$, namely $GT$. On the other hand, if the Outside signal is more precise, as in figure 4(b), then the concave closure of the expected utility is such that the optimal signal structure is $GB$. This can also be seen in 5, which shows that an agent who faces a less (more) precise Outside signal expects greater utility from choosing a $GT$ ($GB$) signal structure.
Interpreting the signal structures. Note that the $GT$ signal structure is one-sided, in the sense that only signal $G$ is realized in the favorable state of the world. Therefore, on observing a signal $T$, the agent is certain that the state of the world is unfavorable. We interpret the agent’s choice of $GT$ as the choice of media with a strong political bias.\textsuperscript{15} Favorable news is routinely reported by these outlets and is not very informative for Bayesian agents. When these outlets report unfavorable news, it is highly informative for Bayesian agents and will convince them that the state of the world is not favorable to their side.

On the other hand, $GB$ is two-sided in that either $G$ or $B$ can be realized in either state of the world, according to a predetermined probability distribution. This is akin to the agent consuming more balanced media because it provides her with a mix of positive and negative news in either state of the world.\textsuperscript{16} The probability of realization of each signal ($G$ or $B$) depends on the state of the world.

The fact that a negative signal is sent by the $GB$ Inside media in either state of the world makes it less informative, allowing a critique to not be irredeemably bad. Specifically, a favorable Outside signal can counteract an unfavorable Inside signal making the Outside news potentially crucial in the preservation of the individual’s political identity. In contrast, with the more slanted $GT$ Inside signal structure, the preservation of political identity does not depend on the realization of Outside news.

It is important to note that the nature of the media outlets endogenously chosen by the agent (her Inside signal structure) depends on her beliefs about the media environment as a whole. If she believes that the media environment is imprecise or biased against her,
then she will choose to consume news from a more politically biased media outlet

**Robustness checks.** In Appendix [A.3](#), we show that the nature of this problem and the optimal signal structures are robust to a small amount of uncertainty or noise in the threshold of belief required for political identity preservation. This kind of robustness is also noted in [Kamenica & Gentzkow (2011)](#), whose key results and structure of the solution hold in the presence of noise which makes the receiver’s belief threshold for choosing the sender-preferred action stochastic.

In Appendix [A.4](#) we show that all the results are robust to an additive function according to which the agent has a relatively small gain from voting for the correct party. This is because, for low values of gain from being correct, the set of signal structures that solve the agent’s problem remains the same as in the benchmark. If there is a region of information aggregation failure present in the benchmark, then it does not disappear when we include a small gain from voting for the correct party, although the region might shrink in size.

We further show in Appendix [A.5](#) that the results remain unchanged if the agent gains linearly from holding posteriors favorable to her party, in addition to the gain from political identity preservation. This is because the choice of an Inside signal structure is invariant to the gain from favorable posteriors, and all electoral outcomes are determined by that choice. This robustness holds for all levels of that gain in the utility function.

Therefore, the results are robust to small changes to the shape of the utility function such as noise, a preference for being correct, or holding more favorable beliefs. The key driver of the results is a sharp change in the agent’s utility when her beliefs cross a predetermined threshold which is in the vicinity of one-half.

### 3 The model: Electoral outcomes

In the previous section, we considered an identity-\(R\) agent’s decision-theoretic problem (the identity-\(L\) agent’s problem is specified and solved analogously). In order to study information aggregation in elections, which is our main focus, we assume that there are countably infinite agents who vote for the party they believe to be superior after they form posterior beliefs.\(^{18}\)

\(^{17}\)In Appendix [A](#) we consider a general model and calculate the optimal signal structure choice for all binary Outside signal structures, which includes biased signal structures. In Subsections [3.2.2](#) and [3.3](#) agents who believe that the outside signal is biased against them choose a one-sided signal structure.

\(^{18}\)Ties are broken in favor of the party matching the agent’s identity. Since there are infinite voters, pivotality is not a concern. Furthermore, we have thus far assumed that the agents vote for the party they
Since we are aggregating individual decisions, we can consider any distribution of voter characteristics. These include identity (R or L), priors, exposure to the information shock, access to inside media, and possibly incorrect beliefs about the information shock, among other things. We can also consider asymmetries in the news environment such as a bias in the process that generates the information shock.

In each case, we can compare the electoral outcomes in our model with those in a benchmark case in which agents are not motivated by identity preservation, or in which an Inside signal is not available. Focusing on electoral outcomes allows us to not only illustrate whether information is aggregated correctly but also to highlight the margin of victory. While this workhorse model is capable of analyzing any distribution of voter characteristics and symmetric or asymmetric environments, the environments we choose to consider are the most salient and interesting.

In Subsection 3.1, we consider the baseline model in which voters of both identities are unequally exposed to information shocks. In Subsection 3.2, we conceptualize asymmetric trust in the media in two ways: media distrust may imply an incorrect belief that the mainstream media is less precise than it truly is (Subsection 3.2.1) or an incorrect belief that the mainstream media is biased against the agent’s preferred party (Subsection 3.2.2). Note that in subsections 3.1 and 3.2, the analysis involves an asymmetry in the distribution of voter characteristics.

The model also allows us to tackle questions related to propagandized media. In Subsection 3.3, we consider a mainstream media environment that is biased in favor of one political party. In this case, voter characteristics are symmetrically distributed and an asymmetry appears as a bias in the Outside signal structure.

Given the ubiquitousness of partisanship and the widespread availability of a vibrant set of news media, there may be other applications of the model that are worthy of future research.

In each application, we study the role of a particular asymmetry between the two political sides. To highlight the impact of that asymmetry in each environment, we suppose that the countably infinite agents are either identity-R or identity-L in equal proportion. We also assume that all agents share a common and symmetric prior regarding the state of the world ($P[\omega = R] := w = 0.5$).
3.1 Asymmetric exposure to information shocks

What happens if voters of one political side are systematically less exposed to information shocks than the other side? In what follows, we suppose that identity-\( R \) agents contend with a less precise information shock than identity-\( L \) agents. We considered this question in the example that was discussed in the introduction; a more detailed illustration of the solution and the mechanisms is presented here.

Each agent receives an Outside signal \((s \in \{r,l\})\). The Outside signal for identity-\( L \) agents has the following structure:

\[
P[s = l | \omega = L] = P[s = r | \omega = R] = t
\]

where \( t \in [0.5, 1] \) is the precision of the Outside signal.

For identity-\( R \) agents, the Outside signal has the following structure:

\[
P[s = l | \omega = L] = P[s = r | \omega = R] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \leq t
\]

where \( t \in [0.5, 1] \) is the precision of the Outside signal for identity-\( L \) agents and \( \tau \in [0, 1] \) is the relative exposure of identity-\( R \) agents to the Outside signal.\(^{19}\)

One way to interpret precision and exposure in the context of the Outside signal is as attention. Attention, or lack thereof, might be a feature of the media landscape or one’s social circle, which will determine the intensity, frequency, or clarity with which agents receive the signal from outside their chosen media diet. For instance, in the U.S., an asymmetry in information insularity between the two political parties may be due to the rural-urban sorting between Republicans and Democrats. An alternative interpretation of attention would be that signal precision and exposure capture the openness of an agent to receiving a signal from outside her chosen Inside media. This openness, or lack thereof, may be due to the agent’s preference or beliefs regarding the trustworthiness of the Outside information, which may lead her to actively avoid exposure to mainstream media. The asymmetry in exposure can therefore be thought of as reflecting either the media landscape, or the agent’s preferences or beliefs, or some combination thereof.\(^{20}\)

\(^{19}\)One can interpret \((1 - \tau)\) as the extent of noise mixed in with the outside information shock for identity-\( R \) agents. Equal exposure to outside information shocks can be considered by setting \( \tau = 1 \). When \( \tau = 0 \), identity-\( R \) agents receive an outside information shock that is pure noise. An alternative isomorphic setup would simply specify different levels of precision for the Outside signal received by agents of both identities, such that the Outside signal’s precision for an identity-\( R \) agent is lower than that for an identity-\( L \) agent.

\(^{20}\)Note that in this subsection, identity-\( R \) agents receive a less precise Outside signal than identity-\( L \) agents. In Subsection 3.2.1 we consider a variant of the model in which identity-\( R \) agents receive the same
We assume that both the Inside signal and the Outside signal are realized independently for all agents, conditional on the state of the world. This can occur in a media-rich environment where different media choices might have the same signal structure but different realizations of the signal. Under independent realization of signals, there is no aggregate uncertainty in outcomes. Introducing correlation is straightforward, and the results have a similar flavor, albeit with aggregate uncertainty about electoral outcomes. See Appendix B.2 for details.

Individuals in this environment have access to a wide array of news and opinion outlets that allow them to consume a specific diet of chosen media. We are interested in their choice of Inside media as a function of their exposure to Outside media and its effect on electoral outcomes.

Example. In the example appearing in the introduction, we set \( t_R = 0.51 \) and \( t_L = 0.75 \), which is equivalent to setting \( t = 0.75 \) and \( \tau = 0.04 \). For these parameter values, we find that introducing the ability to choose one’s media transforms a fully symmetric election into one with failure of information aggregation, where party \( R \) wins the election in both states of the world. This result is obtained despite agents being rational in their information processing.

Table 1: Results with and without Inside media

<table>
<thead>
<tr>
<th>Parameters: ( t = 0.75, \tau = 0.04 )</th>
<th>Without Inside media</th>
<th>With Inside media</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Ex-Ante ( \omega = R )</td>
<td>( \omega = L )</td>
</tr>
<tr>
<td>R Win Margin</td>
<td>0%</td>
<td>+26%</td>
</tr>
<tr>
<td>R Win Prob</td>
<td>50%</td>
<td>100%</td>
</tr>
</tbody>
</table>

Table 1 shows that without Inside media, asymmetric exposure to mainstream media does not provide the \( R \)-side with any advantage in winning margin or winning probability. The correct side wins in both states of the world. When the state of the world is \( R \), then 51% of identity-\( R \) agents and 75% of identity-\( L \) agents receive an Outside signal indicating that the state of the world is more likely to be \( R \), and they vote for party \( R \), which implies that the \( R \)-side wins with a margin of 26%. Because the Outside signal is unbiased, party \( L \) wins with the same margin in state \( L \).

\( ^{21} \) In this subsection, both agents receive unbiased Outside signals that are not fully informative, and we suppose that identity-\( R \) agents receive noisier Outside signals than identity-\( L \) agents. The reverse case yields analogous results.

\( ^{21} \) In this subsection, both agents receive unbiased Outside signals that are not fully informative, and we suppose that identity-\( R \) agents receive noisier Outside signals than identity-\( L \) agents. The reverse case yields analogous results.
The mechanism. The introduction of the Inside signal in the second row of table 1 results in an information aggregation failure that allows party $R$ to win regardless of the state of the world. This result is not ex-ante obvious.

Figure 6(a) plots the expected utility (which is equivalent to the likelihood of political identity preservation) for an agent choosing $GT$ and $GB$ signal structures as a function of the precision of the Outside signal ($t_\mathcal{R} = \tau t + \frac{(1-\tau)}{2}$). We see that a $GT$ signal structure results in higher utility if the perceived precision of the Outside signal is sufficiently low. For higher values of perceived precision, a $GB$ signal is optimal. The intuition behind this result follows directly from figure 4(a) and 4(b). When the perceived precision of the Outside signal is low, it is easier to counteract an unfavorable Outside signal and a $GT$ signal structure is preferable. For high levels of precision, a $GB$ signal structure is preferable because it allows her to rely on a favorable realization of the Outside signal to preserve her political identity since even an unfavorable realization of her Inside signal can be overcome by that. Under the parameter values described above ($t = 0.75$ and $\tau = 0.04$), an identity-$R$ agent chooses a $GT$ signal structure, whereas an identity-$L$ agent chooses a $GB$ signal structure.

Figure 6: The mechanism

When the state of the world is $R$, all identity-$R$ agents are able to preserve their political identity because of their choice of a $GT$ signal structure. Therefore, all identity-$R$ agents vote for party $R$ in state $R$. This is illustrated in figure 6(b) with the dotted red line which shows that the expected utility of an agent who chooses a $GT$ signal structure

\footnote{In Appendix B.1 we show that the $GT$ signal structure is optimal for identity-$R$ agents if and only if $\tau \cdot t + (1-\tau) \cdot \frac{1}{2} \leq \frac{1}{\sqrt{2}}$. Because identity-$L$ agents receive an Outside signal with a perceived precision $t$, they choose a $GT$ signal structure for all values of $t \leq \frac{1}{\sqrt{2}}$ and a $GB$ signal otherwise.}
equals 1 in the favorable state of the world. As denoted by the dashed blue line, a GB signal structure in the unfavorable state of the world allows identity-L agents to preserve their political identity and vote for party L with a probability of 44%. Therefore, party R wins in state R.

When the state of the world is L, the likelihood of political identity preservation by identity-R agents is denoted by the red arrow on the dashed red line, while the corresponding likelihood for identity-L agents is denoted by the blue arrow on the dotted blue line. Given the parameter values in table[1] 96% of identity-R agents vote for party R while 94% of identity-L agents vote for party L. Therefore, party R wins even in state L.

This kind of information misaggregation occurs when identity-R agents receive a very imprecise Outside signal, while identity-L agents must contend with a moderately precise Outside signal. This configuration is particularly salient because it corresponds to identity-R agents being relatively closed to Outside information while identity-L agents are relatively open, which might be the result of a rural-urban divide between the parties or an asymmetry between the parties in terms of trust placed in the mainstream media.

**Discussion.** Every agent individually maximizes her likelihood of political identity preservation, but, for some parameters, this implies that party L loses regardless of the state of the world. If instead, identity-L agents choose GT as their Inside signal structure, then party L can win in the correct state — implying that an ex-ante suboptimal individual choice can allow for ex-post optimal policy choice. In other words, party L would benefit if it could convince its electorate to consume more politically biased news. In the U.S. context, this would occur if the Democratic party notes that Republicans consume more biased news, realizes that they could benefit electorally if Democrats also do so, and successfully influences their news consumption patterns. We believe that, in line with the structure of the model, it is more likely that individual news consumption is driven by individual preferences, rather than by mandates from political parties, or by strategic considerations as to which media is being consumed by members of the opposing political camp.

It is important to note that information aggregation failure occurs for low values of exposure (τ) and intermediate values of Outside signal precision (t). If the Outside signal were less precise, for instance, if t = 0.7, then agents of both identities would choose a GT signal structure, and the correct party would always win. On the other hand, if the Outside signal were very precise, then again, the correct party would always win. If the

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23In aggregate, if each agent maximizes her likelihood of political identity preservation, then (L and R) is maximizing their expected vote share.
state of the world is $L$, then identity-$L$ agents are more likely to receive a *Good* signal and vote for party $L$ in state $L$ relative to the outcomes in table 1. Similarly, identity-$R$ agents are more likely to receive a *Terrible* signal and vote for party $L$. Party $L$, therefore, receives more votes than party $R$ in state $L$.

Figure 7: Signal choices and results with asymmetric exposure

(a) Common priors

(b) Non-common priors: $w_R = 0.6, w_L = 0.4$

In figure 7(a), we consider all values of signal precision ($t$) and exposure ($\tau$). In the red-shaded area, agents of both identities choose a $GT$ signal structure, while in the blue-shaded area, they choose a $GB$ signal structure. In the purple-shaded region, identity-$R$ agents choose a $GT$ signal structure, while identity-$L$ agents choose a $GB$ signal structure. There is no region where identity-$R$ agents choose a $GB$ signal structure and identity-$L$ agents choose a $GT$ signal structure. As claimed in proposition 1 below, there is a region within the purple-shaded region where information aggregation fails, such that identity-$R$ individuals choose a $GT$ signal structure while identity-$L$ agents choose a $GB$ signal structure.

**Proposition 1** In the environment specified in Subsection 3.1, the correct candidate wins except in a region with intermediate Outside signal precision and low exposure among identity-$R$ agents. In the region of information misaggregation, identity-$R$ agents choose a $GT$ signal structure while identity-$L$ agents choose a $GB$ signal structure.

We show in Appendix B.1 that the result in the above example is not knife-edge and that the voting margins are continuous in $\tau$ and $t$ in the neighborhood of $\tau = 0.04$ and $t = 0.75$. In figure 7(a), it can be seen that the light-purple-shaded area, which denotes the region of information aggregation failure, exists for low values of media exposure on the Right ($\tau$) and moderate values of Outside media precision ($t$).
When agents of both identities choose a $GT$ signal structure for their respective Inside media and if the state of the world is $R$, then all identity-$R$ agents and some identity-$L$ agents vote for party $R$. If the state of the world is $L$, then all identity-$L$ agents and some identity-$R$ agents vote for party $L$. In this case, information aggregation failure is not possible. We show in Appendix B.1 that the party that matches the state of the world wins for all values of $\tau$ and $t$, such that a $GB$ signal structure is optimal for both identities. Furthermore, the parameter space is such that there is no situation in which identity-$R$ agents choose a $GB$ signal structure and identity-$L$ agents choose a $GT$ signal structure.

Party $R$ achieves an ex-ante winning margin advantage as a result of the lower exposure of identity-$R$ citizens. This is a straightforward implication of the fact that it is easier for identity-$R$ citizens to preserve their political identity because they are contending with a less precise Outside signal than identity-$L$ citizens. It is, however, striking that the political advantage enjoyed by party $R$ can be so substantial for some parameters that it can win regardless of the state of the world. Furthermore, while the region of information aggregation failure in figure 7(a) appears to be small, those parameter values may be particularly relevant in the case of the U.S. The intermediate values of Outside media precision at which information misaggregation takes place are high enough that identity-$L$ agents choose a two-sided $GB$ Inside signal structure, but not high enough that party $L$ wins in state $L$.

**Correlated signals.** In this model, we have assumed that the Inside and Outside signals realize independently of each other and for each individual. We saw in the example above that party $R$ can win for sure in either state of the world. Because the winning margin of party $R$ is positive (specifically, bounded away from zero), we know that the result of information aggregation failure is robust to some, possibly small, degree of correlation of the two signals.

In Appendix B.2, we detail the implications of three cases of correlated signals. We fix parameter values to be the same as studied in the key example above. That is, there is an equal proportion of infinite identity-$R$ and identity-$L$ agents. Identity-$R$ agents receive a less precise Outside signal than identity-$L$ agents ($t_R = 0.51$ and $t_L = 0.75$). The common prior belief is that each state of the world is equally likely.

First, we consider the case that the Outside signal realization is fully correlated across agents of the same identity. Second, we suppose that Inside signal realization is fully correlated in the same way. Finally, we study the situation where both signals are fully correlated in the way they realize for all agents of the same identity. In each scenario, since
the Outside signals realize independently of the Inside signal, the optimal signal structure choice for agents remains the same as in the baseline model. This implies that the expected winning margin advantage for party $R$ remains the same ex-ante ($+29\%$) and conditional on the state being $R$ ($+56\%$) or $L$ ($+2\%$). The aggregate implications of this expected winning margin advantage vary according to the kind of correlation we consider. In each case, party $R$ wins with a higher probability than party $L$. Therefore, while correlation introduces some aggregate uncertainty, the flavor of the key results remains largely unchanged.

**Non-common priors.** In addition to having a political affiliation, it may be that agents hold more favorable priors towards their party, and we can very simply extend the baseline model to consider the implication of such non-common priors. Suppose that an identity-$R$ agent holds a prior $P_R[\omega = R] := w_R$, which is higher than that of an identity-$L$ agent ($P_L[\omega = R] := w_L$).

Figure 7(b) considers the case in which $w_R = 0.6$ and $w_L = 0.4$ and shows that the region of information aggregation failure, where party $R$ wins regardless of the state of the world, is much larger with non-common priors than with common and symmetric ones ($P[\omega = R] := w = 0.5$).\(^{24}\)

In this case, if the precision of the Outside signal ($t_R = \tau t + \frac{(1-\tau)}{2}$) for an identity-$R$ agent is less than 0.6, then she can preserve her political identity regardless of the realization of the Outside signal by simply choosing a non-informative Inside signal structure. This is akin to a citizen consuming news commentary from an outlet with a political bias that does not claim to be providing journalistic facts. For higher levels of perceived precision of the Outside signal, the identity-$R$ agent would choose a $GT$ or $GB$ signal structure as before. Holding favorable priors means that identity-$R$ individuals preserve their political identity more often.

Similarly, identity-$L$ citizens are able to preserve their political identity more often when they hold priors favorable to their party. However, because they face a more informative Outside signal, the advantage gained from their priors is limited. If the precision of the Outside signal is low enough for identity-$L$ agents to always preserve their political identity, then identity-$R$ agents would also be able to do the same. Furthermore, in the presence of non-common priors, for some parameter values, identity-$R$ agents always preserve their political identity by choosing a non-informative Inside signal structure, while identity-$L$ agents choose a $GB$ signal structure that allows them to preserve their political identity with a probability not equal to one. Naturally, non-common priors would

\(^{24}\)The calculations are presented in Appendix B.3.
expand the parameter space within which we observe information misaggregation.

The assumption of agents sharing common priors reduces the region of information misaggregation, which is a key result of the model. In that sense, we have tied our own hands by assuming that agents share common priors.

3.2 Asymmetric media distrust

Figure 2 illustrates the markedly different levels of trust in the mainstream media by voters on either end of the political spectrum. In the polling data for years following 2016, around fifteen percent of Republicans have expressed a great deal or fair amount of trust in mass media. The corresponding proportion for Democrats has hovered around seventy percent. In this subsection, we consider two models of asymmetric media distrust. In Subsection 3.2.1, we build a model in which identity-\( R \) agents incorrectly believe that the Outside signal is less precise than it really is, while in Subsection 3.2.2, we consider a model in which identity-\( R \) voters incorrectly believe that the Outside signal is biased against their side. The mechanism underlying the results is similar to the one presented earlier in Subsection 3.1.

3.2.1 Distrust in mainstream media precision

In this subsection, we interpret distrust as reflecting an agent’s perception of the quality of mainstream media, namely the source of the information shock. As noted earlier, agents’ beliefs regarding the Outside signal structure are based on their beliefs regarding the mainstream media landscape as a whole. If some agents incorrectly believe that mainstream media reporting is imprecise, then they will believe that the precision of the mainstream media is lower than it really is.

We suppose that identity-\( L \) agents hold correct beliefs regarding the Outside signal and perceive the following structure:

\[
P[s = l | \omega = L] = P[s = r | \omega = R] = t
\]

where \( t \in [0.5, 1] \) is the true precision of the Outside signal. On the other hand, identity-\( R \) agents incorrectly believe that the Outside signal has the following structure:

\[
P[s = l | \omega = L] = P[s = r | \omega = R] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2}
\]

where \( \tau \in [0, 1] \) is the extent of an identity-\( R \) agent’s trust in the Outside signal.
The choice of signal structures by agents of either identity is the same as in Subsection 3.1. Again, we find there to be misaggregation of information within the region where identity-\( R \) agents choose a \( GT \) signal structure and identity-\( L \) agents choose a \( GB \) signal structure. Because identity-\( L \) agents are correct about the process generating the Outside signal and because the Outside signal does not impact the likelihood of political identity preservation for identity-\( R \) agents, the region of misaggregation of information (where party \( R \) wins regardless of the state of the world) is identical to the region presented in figure 7(a). In sum, the results are identical whether we consider the asymmetry to be in exposure to Outside media or distrust in the quality of Outside media.

3.2.2 Distrust in mainstream media unbiasedness

What happens if there is no systematic bias present yet some individuals believe there is? This obviously reflects distrust in the unbiasedness of the mainstream media. Therefore, we now suppose that identity-\( R \) agents believe the mainstream media to be biased when actually it is not.

Suppose the Outside signal structure is unbiased and has a precision of \( t \in [0.5, 1] \). Then, identity-\( L \) agents correctly believe that the Outside signal structure follows:

\[
P[s = l|\omega = L] = P[s = r|\omega = R] = t
\]

Identity-\( R \) agents hold an incorrect belief and perceive the media to be biased when it is not. Thus, they believe that the Outside signal structure follows:

\[
P[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot 1, \quad P[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
\]

where \( \tau \in [0, 1] \) is an identity-\( R \) agent's belief in the extent of the Outside signal's unbiasedness.

Figure 8 shows the Inside signal structure choices for agents of each identity as well as the region of information aggregation failure. In this region, identity-\( R \) agents perceive the media to be highly biased, and the Outside signal is at least moderately precise. The perception of bias in the Outside signal structure makes a favorable Outside signal more informative for identity-\( R \) agents and an unfavorable Outside signal less so. This allows identity-\( R \) voters to preserve their political identity with greater likelihood. Therefore, asymmetry in the perception of bias by the mainstream gives party \( R \) an advantage that allows it to win regardless of the state of the world for a subset of parameters (the calculations are provided in Appendix B.5).
Proposition 2 In the environment specified in Subsection 3.2.2, the correct candidate wins except in a region where the Outside signal has intermediate precision and low perceived unbiasedness. In the region of information misaggregation, identity-R agents choose a GT signal structure while identity-L agents choose a GB signal structure.

Thus, creating the perception that the mainstream media produces propaganda is a strong political tool that can allow the incorrect party to win. One implication is that party R benefits if it can convince identity-R voters that the mainstream media is biased in favor of party L. As noted in the introduction, President Trump railed against the mainstream media, accusing it of being biased. Our model suggests that if identity-R voters believe that the mainstream media is biased in favor of party L, then that will influence the Inside media choices of identity-R voters. This gives party R a major electoral advantage and, for a substantial subset of parameters, party R will be able to win regardless of the state of the world.

In this subsection, we considered an interpretation of media distrust in which some agents incorrectly believe that the media is biased and found that there exists a substantial region of information aggregation. In Subsection 3.2.1 we interpreted distrust in the mainstream media as an incorrect belief held by identity-R citizens regarding the Outside signal’s precision and found a comparable result. In view of the similarities in the regions of information misaggregation in figure 8 and 7(a), it is apparent that the phenomenon of an electoral benefit accruing to the side with greater distrust of mainstream media is robust to our interpretation of mistrust.
3.3 Propaganda

A telltale sign of a decaying democracy is the state’s use of the mainstream media for propaganda purposes. We define propaganda as a bias in the information shock process that stems from asymmetry in the realization of news that is favorable or unfavorable to the political parties, depending on the state of the world. We are specifically interested in the impact of propaganda on the agents’ choice of Inside-media as well as its effect on electoral outcomes. In particular, the model allows us to explore whether an agent’s ability to choose Inside media, can counteract propaganda, and furthermore, whether that ability can lead to information aggregation failure if the agent incorrectly believes that the mainstream media is biased.

Suppose that the Outside signal is biased in favor of party $L$ such that the signal $l$ is realized more often. Specifically, the Outside signal structure follows:

$$
\mathbb{P}[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot 1, \quad \mathbb{P}[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
$$

where $t \in [0.5, 1]$ is the precision of the Outside signal, and $\tau \in [0, 1]$ is the extent of unbiasedness in state-influenced media. The higher $\tau$ is, the less biased is the signal. This bias is commonly known by all agents and is the true process that generates the Outside signal.\(^{25}\)

Such a signal structure for the Outside media can exist when the state exerts control over mainstream media outlets. Suppose, for instance, that a strongman leader can force the mainstream media to frequently run positive stories, but cannot prevent the occasional negative story. In such an environment, he may also be able to censor media outlets in order to prevent agents from receiving an Inside signal. In the next two subsections, we therefore consider the implications of propaganda with and without censorship.

3.3.1 With censorship

Suppose that no agents, regardless of their identity, have access to any information other than their prior and the information shock. This scenario may be interpreted either as a situation in which the ruling party shuts down all media other than the propagandized state-controlled media or as a sparse media environment such as that which existed prior to the internet. We define this as the benchmark with censorship, which will serve to highlight the role played by the ability to choose Inside media.

---

\(^{25}\)The extent of unbiasedness, denoted by $\tau$, is analogous to the probability with which a signal is credible, denoted by $\chi$, in Lipnowski et al. (2019). A similar notion of partial commitment is analyzed theoretically and experimentally in Fréchette et al. (2019).
It is straightforward to show that because the agents share common and symmetric priors, and because the Outside signal is informative, the realization of the Outside signal determines whether the agent is able to preserve her political identity. The condition for party $L$ to win in state $L$ is simply that the Outside signal $l$ be realized more often than the signal $r$, which, in fact, always holds (the details of this claim and the ones that follow are presented in Appendix B.6).

If the state of the world is $R$, then the Outside signal $l$ is realized more often if $\tau t < 0.5$. If this condition holds, then there is information misaggregation, and party $L$ wins regardless of the realization of the state of the world. This region is illustrated in figure 9(a).

Figure 9: Propaganda with and without censorship

If the ruler of an illiberal democracy can influence the mainstream media and also prevent citizens from independently accessing information, then she can ensure electoral victory regardless of the state of the world for a large subset of the parameter space. Censorship along with propaganda is, therefore, a powerful combination of tools in an illiberal democracy.

3.3.2 Without censorship

Now suppose that agents can select an Inside signal structure. Being rational, they perceive an information shock that is favorable to the propagandizing side (party $L$) to be less informative than a shock unfavorable to it. Recall that a Good signal from the Inside signal structure is designed to just counteract an unfavorable information shock (Outside signal). For identity-$R$ agents, an unfavorable Outside signal is relatively easy to counter-
act because it is less effective. For identity-\(L\) agents, it is more difficult to counteract. As can be seen in figure 9(b), there is a large subset of parameters within which identity-\(R\) agents optimally choose a \(GT\) signal structure while identity-\(L\) agents choose a \(GB\) signal structure. The region of information misaggregation lies within this subset of parameter values.

In the region of information misaggregation, party \(R\) wins regardless of the state of the world. The intuition behind this result is that if the state of the world is \(R\), then party \(R\) must win because all identity-\(R\) agents and some identity-\(L\) agents vote for party \(R\). The fact that an Outside signal unfavorable to party \(L\) is very informative implies that if the state of the world is \(L\), then that an insufficient proportion of identity-\(L\) agents preserve their political identity and vote for party \(L\). For propaganda to backfire, it must be that the Outside media is sufficiently biased and that the precision of the Outside signal is strong enough to push identity-\(L\) agents to choose a \(GB\) signal structure as their Inside media. However, if the precision of the Outside signal is high, then party \(L\) will win in state \(L\), and no misaggregation of information is present.

Table 2: Results with and without censorship

<table>
<thead>
<tr>
<th>Parameters: (t = 0.6, \tau = 0.3)</th>
<th>With censorship</th>
<th>Without censorship</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Ex-Ante)</td>
<td>(\omega = R)</td>
<td>(\omega = L)</td>
</tr>
<tr>
<td>L Win Margin</td>
<td>+70%</td>
<td>+64%</td>
</tr>
<tr>
<td>L Win Prob</td>
<td>100%</td>
<td>100%</td>
</tr>
</tbody>
</table>

Table 2 presents the case of \(t = 0.6\) and \(\tau = 0.3\) (see Appendix B.6 and B.7 for the calculations). These parameter values correspond to a situation where the Outside signal is fairly precise, and the party-\(L\)–influenced media is known to be particularly biased. It can be seen that under censorship, party \(L\) always wins, and with high margins (reminiscent of the electoral results seen in some Eastern European “democracies” that were controlled by strongmen). On the other hand, in the absence censorship, party \(L\) loses in both states of the world. Therefore, for a substantial subset of parameters, there is a reversal of electoral outcomes when censorship is disallowed. Suppose that party \(L\) cannot perfectly target propaganda and that there is a possibility of mistakes such that there is a positive probability for all levels of bias and precision. Then, party \(L\) must also institute censorship in order to benefit from propaganda. Otherwise, with a positive probability, propaganda backfires.

\footnote{\cite{Li et al.} find that a truthful alternative media can counteract propaganda, a result that is similar in spirit to ours.}
Proposition 3  In the environment specified in Subsection 3.3.2, the correct candidate wins except in a region with low-to-intermediate precision and a highly biased Outside signal. In the region of information misaggregation, identity-R agents choose a GT signal structure, while identity-L agents choose a GB signal structure.

The calculations and the proof can be found in Appendix B.7.

Proposition 3 states that without censorship, propaganda is not simply weak, it actually backfires. Propaganda, by its very nature, implies that news favorable to the propagandizing party is discounted by Bayesian agents and does not affect their posteriors to a substantial degree. News unfavorable to the propagandizing party is particularly informative because it is so rare. If individuals can independently access information, then identity-R agents need very little of it to counteract the propaganda in favor of party L. On the other hand, identity-L agents need a much stronger signal to counteract unfavorable news from the biased media. For all parameters, party R wins in the state of the world it is meant to (state R), and for a substantial parameter space, also in state L.

3.3.3 Propaganda that individuals are oblivious to

We now consider an even less desirable situation in which the mainstream media is biased in favor of party L but individuals are convinced that it is unbiased. We first consider the case in which individuals of both identities are oblivious to the bias in the information shock process. Later on, we will also consider cases in which only identity-R or only identity-L individuals are oblivious to the bias. In each of these cases, at least some citizens choose their Inside signal structure under incorrect beliefs. The mainstream media, which is biased toward party L, generates a signal favorable to party L more often than one favorable to party R.

The true process that generates the Outside signal is biased in favor of party L and takes the following form:

\[
P[s = l | \omega = L] = \tau \cdot t + (1 - \tau) \cdot 1, \quad P[s = r | \omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
\]

where \( t \in [0.5, 1] \) is the precision of the Outside signal and \( \tau \in [0, 1] \) is the Outside signal’s true level of unbiasedness. In the first case we consider, agents of both identities incorrectly believe that \( \tau = 1 \).

As can be seen in figure 10(a), agents of both identities choose a GB signal structure for their Inside media in the region of information aggregation failure (see Appendix B.8 for the detailed calculations).
Although the agents are Bayesian, they update incorrectly and choose their Inside signal structure sub-optimally. Identity-$R$ agents update excessively upon receiving an unfavorable Outside signal, and cushion themselves against the Outside signal by choosing an overly informative Inside signal structure. They thus preserve their political identity less often than they could have. Similarly, identity-$L$ citizens update too little upon receiving unfavorable outside information, which works to their benefit. As we show in proposition 4 for low values of Outside media unbiasedness ($\tau$) and moderate-to-high values of Outside media precision ($t$), party $L$ enjoys such a large advantage that it can win regardless of the realized state of the world.

**Proposition 4** In the environment specified in Subsection 3.3.3 the correct candidate wins, except in a region with an intermediate-precision and highly biased Outside signal. In the region of information misaggregation, agents of both identities choose a GB signal structure.

The proof and detailed calculations are to be found in Appendix B.8. The existence of such a region of information aggregation failure can explain why propagandizing news outlets go to great lengths to portray themselves as accurate and balanced.

**Censorship:** We consider the implications of censorship in an environment where the Outside media is biased but citizens wrongly believe it is not. Party $L$ wins regardless of the state of the world if the Outside signal favorable to party $L$ is generated more often in both. As in Subsection 3.3.1 this condition holds if $\tau t < 0.5$. The electoral results
are therefore also identical and are illustrated in figure 9(a). The only difference with Subsection 3.3.1 lies in the intensity of an individual’s belief in the party they vote for.

**L agents are oblivious:** So far in this subsection, we have considered the case in which voters of both identities are oblivious to the bias in the Outside signal. Now, suppose that only identity-\(L\) agents believe that the Outside signal is unbiased, while identity-\(R\) citizens know that it is. Identity-\(L\) agents update less than they should when faced with an unfavorable Outside signal, and their Inside signal structure choice is the same as in figure 10(a). Identity-\(R\) agents choose their Inside signal structure as shown in figure 9(b). The correct side always wins under this specification, which for party \(L\) is an improvement over the backfiring of propaganda we saw in Subsection 3.3.2.

**R agents are oblivious:** Now suppose that only Identity-\(R\) agents are unaware of the bias in the Outside signal. Identity-\(L\) agents know that the Outside signal structure is biased in favor of Party \(L\) and choose their Inside signal structure correctly as shown in figure 9(b). Identity-\(R\) agents hold incorrect beliefs and choose their Inside signal structure as in figure 10(a).

As shown in figure 10(b), the region where party \(L\) wins regardless of the state of the world expands if only identity-\(R\) agents — rather than both identities — are oblivious to the bias in the Outside signal.

Summarizing Subsection 3.3, we have demonstrated that propaganda backfires in the presence of a rich media landscape. Bayesian citizens largely discard information shocks favorable to the propagandizing side and update their beliefs to a much greater extent upon receiving unfavorable information shocks. A rich media landscape allows citizens on the non-propagandizing side to preserve their political identity more effectively than those on the propagandizing side. Censorship allows the propagandizing side to benefit from the propaganda. Alternatively, the propagandizing side benefits if citizens, particularly those on the opposing side, are unaware of the mainstream media’s bias. In many illiberal democracies, the ruling party usually invests heavily in propaganda. According to our model, that effort should be complemented by censorship or attempting to an attempt to legitimize the propagandized news.

Ravi is here
3.4 Discussion: Belief-based partisanship

We have introduced a novel formalization of partisanship, according to which citizens would like to believe that their preferred party is the better one, but they must contend with outside information. While they choose Inside media to maximize the likelihood of preserving their political identity, they might not always be successful in doing so. In particular, if they are plugged into the news media and receive a highly precise information shock, then it is unlikely that they will manage to preserve their political identity in the state of the world that favors the other party.

Figure 11: Information aggregation failure and belief-based partisanship

This notion of partisanship introduces a novel mechanism for preserving and expressing one’s political identity. It is simultaneously weaker and broader than a behavioral partisanship that induces voters to simply vote for their preferred party. We now analyze the influence of belief-based partisanship by varying the proportion of the population that identifies with party $R$ under two sets of conditions.

In figure 11 (a), we consider asymmetric exposure to the information shock by building on the exposition in Subsection 3.1. Specifically, the precision of the information shock is $t = 0.75$, which is the same as in the example considered earlier. The y-axis measures the exposure of identity-$R$ citizens to the information shock ($\tau$), while the x-axis measures the proportion of the population that identifies with party $R$. It can be seen that when there are sufficiently few identity-$R$ voters, party $L$ always wins. Conversely, when there are enough identity-$R$ voters, party $R$ always wins. The region of information aggregation failure — in which party $R$ always wins — tends to shrink as the exposure of $R$ citizens to the outside signal increases. There is, however, a threshold value of exposure
at which identity-\(R\) citizens switch from a \(GT\) signal structure to a \(GB\) signal structure (at approximately \(\tau = 0.83\)). At that point, there is a discontinuous expansion of the region of information aggregation failure.

Figure 11 (b), illustrates the subtlety of this formalization of partisanship even more strikingly. Unlike behavioral partisans, belief-based partisans must contend with Outside information, and they must convince themselves to vote for their preferred party. In the state of the world that favors the other party, this becomes more difficult as the precision of the information shock increases. In the graph, we suppose that citizens of both identities contend with an information shock of equal precision. Precision appears on the y-axis and as before, the x-axis is the proportion of the population that identifies with party \(R\). When the precision of the information shock is high, the correct party wins in both states of the world even when the population is divided very unequally between the political identities.

4 Conclusion and Further Research

Supporting a party has become nowadays similar to supporting a sports team: emotional attachment and the desire to believe your team is the best come first and the urge to learn the truth often comes second. In the context of liberal democracies, researchers are faced with the task of explaining recent electoral outcomes such as the election of (and then the very close defeats of) Trump, Bolsonaro, or even the Brexit vote, and whether the current emotional partisanship and the rich media environment played a key role in such elections. In non-liberal democracies, such as Russia, Syria, and Hungary, where the regime fully controls the official media message, the government also engages in a costly and extensive crackdown (whether explicitly or implicitly) on non-government media. This suggests that such media may effectively counteract government propaganda, namely that propaganda alone is not effective enough to persuade the country’s citizens.

To shed light on the above phenomena, we have explored how instrumental media choice driven by political identity can affect aggregate electoral results in the current rich media environment. In the core setup, bias is assumed to exist in the preferences that drive media choice but it is not cognitive. Specifically, individuals rationally update using all the information they receive and vote according to that information. We later added cognitive biases and analyse their effects on electoral outcomes.

For liberal democracies, such as the U.S., our benchmark assumes symmetry between the two sides, where the asymmetry exists only in the exposure to Outside media (perhaps reflecting the urban-rural divide), or in the bias of Outside media. In those contexts,
we showed that media choice driven by political identity preservation motives can swing electoral outcomes. When information aggregation failure occurs, one candidate wins in all states of the world, even when she is the worse candidate, or in other words, even when average/expected rational beliefs following any media signal — chosen or not — are unfavorable to her. A key determinant of this failure of information aggregation is that one side has low exposure to mainstream media or low trust in it, while the other has a moderate level of exposure/trust. In this region, the introduction of a rich media environment can provide a winning margin advantage to the side less exposed to mainstream media, even to the point that it can swing elections in all states of the world. This misaggregation region (characterized by low and moderate exposure on the Right and Left sides of the political spectrum, respectively) seems particularly salient in democracies such as the U.S., perhaps explaining why some parties have an incentive to encourage distrust in the mainstream media. If we add cognitive biases, such as biased priors, this misaggregation region becomes even larger.

In the case of illiberal democracies, we found that for government propaganda to work, it is crucial that individuals be unaware of it. In other words, individuals must also have a cognitive bias. If they are aware of the bias in the Outside signal structure, then the presence of a free media undermines government propaganda spectacularly. Indeed, propaganda may backfire entirely, allowing the non-propagandizing side to win regardless of the state of the world. This may explain why it is not sufficient for authoritarian governments to control the official media message and promote government propaganda if citizens are aware of this. For such governments to maintain power, they must limit the free media and dissenting news outlets in order that possibly inconvenient truths are suppressed.

In our setup, news consumption is demand-driven and therefore media outlets are passive signal providers. More work needs to be done on the supply side of news, in particular on the supply of misinformation and how effective this might be in aggregate. Interestingly, misinformation is often aimed at counteracting actual news. For instance, in the aftermath of an attack by a right-wing extremist on Paul Pelosi, the husband of the Speaker of the House, which happened 10 days before the U.S. midterm elections in 2022, some partisan activists and media outlets immediately counteracted the news reports by circulating unfounded claims casting doubt on the official version what had happened.

Misinformation has become ingrained and the reflexive response to anything that might

---

27Such claims were often homophobic or they alleged an inside job. Similar conspiracies minimized, denied, or invented a different story for what happened during the Jan. 6, 2021 attack on the Capitol and the Sandy Hook School shooting on Dec. 14, 2012.
cast a negative light on one side or the other is to deflect it with fictional claims in an attempt to muddy the waters and deflect accusations. Such claims evidently are more likely to be believed by voters with a certain desire to preserve their political identity.

References


41
A Solution for the general model

Suppose that an agent believes (whether correctly or incorrectly) that

\[ P[s = l | \omega = L] = k, \quad P[s = r | \omega = R] = m \]

The agent’s expected utility still follows equation and the signal structure must satisfy the Martingale constraint.

The agent’s interim posteriors on observing the Outside signal and before observing the signal from the chosen signal structure are such that:

\[ P[\omega = L | s = l] = \frac{k}{1 + k - m}, \quad P[\omega = L | s = r] = \frac{1 - k}{1 + m - k} \]
The $G$, $B$, and $T$ signals are described Section 2. An identity-$R$ agent is able to preserve her political identity as long has her posterior upon observing both signals is such that 

$$ P[\omega = R|s, S] \geq 0.5. $$

Therefore, the $G$, $B$, and $T$ signals must be such that:

$$ P[\omega = R|S = G] = \frac{k}{1 + k - m}, $$

$$ P[\omega = R|S = B] = \frac{1 - k}{1 + m - k}, $$

$$ P[\omega = R|S = T] = 0. $$

**Claim 1** It is sufficient to consider three signals used in two possible signal structures when solving the agent's problem described above.

**Proof.** The proof follows directly from Kolotilin (2018) and Kamenica & Gentzkow (2011). We use the linear optimization technique of comparing marginal utility to price ratios (MU-Price ratios) for the different signals. In figure 3, the MU-Price ratio of a signal is represented by the slope of the line from the origin to the point on the expected utility curve that corresponds to the interim posterior generated by that signal. In that sense, this technique is equivalent to finding the optimal signal structure using the concave closure of the expected utility function.

**Lemma 2** Any signal $M_i$ that generates a posterior $P[\omega = R|M_i] \in (\frac{k}{1 + k - m}, 1]$ is sub-optimal when compared to a signal $M_G$ where $M_G$ is such that $P[\omega = R|M_G] = \frac{k}{1 + k - m}$.

**Proof.** Regardless of whether the agent observes $M_i$ or $M_G$, her expected utility will be the same. This is because the agent is able to preserve her political identity regardless of the realization of the Outside signal.

However, it is more costly (according to the Martingale constraint) to generate the signal $M_i$. Therefore, the MU-Price ratio of generating $M_i$ is less than that for generating $M_G$. This implies that any signal structure where $P[M_i] > 0$ will have a lower ex-ante expected utility than a signal structure that assigns $P[M_i] = 0$ and adds $P[\omega = R|M_i]P[M_i]$ to the probability that $M_G$ is generated. Therefore, no $M_i$ such that $P[\omega = R|M_i] \in (\frac{k}{1 + k - m}, 1]$ will be chosen by the agent. Equivalently, $M_i$ is sub-optimal when compared to $M_G$. ■

**Lemma 3** Any signal $M_i$ that generates a posterior $P[\omega = R|M_i] \in (\frac{1 - k}{1 + m - k}, \frac{k}{1 + k - m})$ is sub-optimal when compared to a signal $M_B$ where $M_B$ is such that $P[\omega = R|M_B] = \frac{1 - k}{1 + m - k}$. 

43
Proof. For $M_i$, the ex-ante expected utility of the agent is given by:

$$\mathbb{P}\left[\mathbb{P}[\omega = R|M_i, s] \geq 0.5\right] = m\mathbb{P}[\omega = R|M_i] + (1-k)(1 - \mathbb{P}[\omega = R|M_i])$$

$$= 1 - k + \mathbb{P}[\omega = R|M_i](m + k - 1)$$

This implies that the MU-Price ratio is:

$$\frac{(m + k - 1)}{\mathbb{P}[\omega = R|M_i]}$$

For $M_B$, the ex-ante expected utility is:

$$\mathbb{P}\left[\mathbb{P}[\omega = R|M_B, s] \geq 0.5\right] = m\left(\frac{1-k}{1+m-k}\right) + (1-k)(1 - \left(\frac{1-k}{1+m-k}\right)) = 2m\left(\frac{1-k}{1+m-k}\right)$$

This means that the MU-Price ratio is:

$$2m = (m + k - 1) \times \left(\frac{1-k}{1+m-k}\right)$$

Since $\mathbb{P}[\omega = R|M_i] > \frac{1-k}{1+m-k}$, the MU-Price ratio for generating a signal structure posterior $M_i$ is lower than for $M_B$. Therefore, no $M_i \in \left(\frac{1-k}{1+m-k}, \frac{k}{1+k-m}\right)$ will be chosen by the agent. Equivalently, $M_i$ would be sub-optimal when compared to $M_B$. ■

Lemma 4 Any signal $M_i$ that generates a posterior $\mathbb{P}[\omega = R|M_i] \in (0, \frac{1-k}{1+m-k})$ is sub-optimal when compared to a signal $M_T$ where $M_T$ is such that $\mathbb{P}[\omega = R|M_T] = 0$.

Proof. For $M_i$, the ex-ante expected utility is zero. This is because regardless of the realization of the Outside signal, the agent is never able to preserve her political identity, and the same is true for $M_T$. However, $M_i > 0$, which implies that the cost for generating $M_i$ is higher than that for generating $M_T$. Therefore, no $M_i \in (0, \frac{1-k}{1+m-k})$ will be chosen by the agent. Equivalently, $M_i$ is sub-optimal when compared to $M_T$. ■

The agent requires only three signals to solve her problem. In fact, any signal that generates a posterior different from them would be sub-optimal. $M_G$, which generates a posterior $\mathbb{P}[\omega = R|M_G] = \frac{k}{1+k-m}$, is abbreviated to $G$. $M_B$, which generates a posterior $\mathbb{P}[\omega = R|M_B] = \frac{k}{1+m-k}$, is abbreviated to $B$. Finally, $M_T$, which generates a posterior $\mathbb{P}[\omega = R|M_T] = 0$, is abbreviated to $T$.

A signal structure is a combination of signal realizations, and the three possible signals
are $G$, $B$, and $T$. Therefore, the possible signal structures are $GT$, $GB$, and $GBT$. 

We argue that while $GBT$ is feasible according to the budget constraint, and might even be an optimal choice for some parameters, it can be ignored, since whenever it is optimal, a simpler signal structure ($GB$ or $GT$) is as well. In other words, this signal structure never offers strictly greater expected utility (than the max of $GB$, and $GT$), and is therefore not required to solve the agent’s problem. Either the MU-Price ratio of $G$ is higher than that of $B$ in which case $GT$ should be implemented, rather than $GBT$; or the MU-Price ratio of $B$ is higher than that of $G$ in which case $GB$ should be implemented, rather than $GBT$; or, the MU-Price ratios of $G$ and $B$ are equal, in which case either $GB$ or $GT$ provides the agent with the same expected utility as $GBT$, and therefore, $GBT$ can be ignored.

Therefore, $GT$ and $GB$ alone are sufficient to solve the agent’s problem. 

A.1 The identity-$R$ agent’s problem

Recall that:

$$\mathbb{P}[s = l | \omega = L] = k, \quad \mathbb{P}[s = r | \omega = R] = m$$

This is a linear optimization problem, and therefore, the agent chooses to employ the signals with the highest MU-Price ratio.

For signal $G$, the MU is 1. This is because regardless of the Outside signal, the agent is able to preserve her political identity. For signal $B$, the MU is equal to the likelihood that the Outside signal is favorable ($r$, for an identity-$R$ agent) given that $B$ is realized, i.e. $2m \left( \frac{1 - k}{1 + m - k} \right)$. Finally, for $T$, the agent is never able to preserve her political identity, and therefore the MU is 0.

The price of each of these signals is determined according to the coefficient corresponding to it in the Martingale constraint, i.e. $\left( \frac{k}{1 + k - m} \right) \cdot P_G + \left( \frac{1 - k}{1 + m - k} \right) \cdot P_B + 0 \cdot P_T = 0.5$. This price is simply the intermediate posterior generated by the signal.

The MU-Price ratio is $\frac{1}{k} \frac{1}{1 + k - m}$ for signal $G$, $\frac{2m}{\left( \frac{1 - k}{1 + m - k} \right)} = 2m$ for signal $B$, and undefined for signal $T$.

The signal structure $GT$ is optimal when MU-Price ratio for signal $G$ is at least as large as that for signal $B$, which simplifies to $1 + k - m - 2km \geq 0$. If $1 + k - m - 2km \leq 0$, then signal structure $GB$ is optimal. This is equivalent to saying that the concave closure of the

\footnote{There are a number of signal structures that are ruled out because they violate the Martingale constraint, specifically, $G$, $B$, $T$, and $BT$. While we assume that the agents share a common symmetric prior belief that $\mathbb{P}[\omega = R] = 0.5$, this result is robust to values of $\mathbb{P}[\omega = R]$ such that $\frac{1 - k}{1 + m - k} < \mathbb{P}[\omega = R] < \frac{k}{1 + k - m}$.}
expected utility curve shown in figure 4 has a kink if and only if \(1 + k - m - 2km < 0\). If it does, then a GB signal provides the agent with a higher expected utility than a GT signal.

We can now calculate the probability of realization of different signals, the utility achieved, and the likelihood of voting for the preferred party under the signal structures GT and GB.

The probabilities of realizing the different signals will help us calculate expected utilities as well as the outcome of the election.

**Signal structure GT:** Unconditional on the state, the likelihood that the signal \(G\) is realized is \(P_G = \frac{1 + k - m}{2k}\), which is also the agent’s ex-ante expected utility.

Conditional on the state being \(\omega = R\), the signal \(G\) is always realized and therefore the agent’s expected utility is \(E[U_{R|GT\cap \omega = R}] = P[G|\omega = R] = 1\).

Conditional on the state being \(\omega = L\), the likelihood that signal \(G\) is realized is \(1 - \frac{m}{k}\). Whenever signal \(G\) is realized, the agent is able to preserve her political identity. Therefore, this also equals the agent’s expected utility \(E[U_{R|G\cap \omega = L}]\).

**Signal structure GB:** This signal structure is somewhat more complicated, and therefore, we use the following three equations.

\[
\begin{align*}
P[G|GB] + P[B|GB] &= 1 \quad (2) \\
P[G|\omega = L] &= \frac{1 - m}{k} \quad (3) \\
P[G|\omega = R] &= \frac{m}{1 - k} \quad (4)
\end{align*}
\]

Given that the signal structure is GB,

\[
1 = P[G] + P[B] = \left(\frac{P[G|\omega = R]}{2} \cdot \frac{1}{2} + P[G|\omega = L] \cdot \left(\frac{1}{2}\right)\right) + \left(\frac{P[B|\omega = R]}{2} \cdot \frac{1}{2} + P[B|\omega = L] \cdot \left(\frac{1}{2}\right)\right)
\]

\[
= \frac{1}{2} \left(\frac{P[G|\omega = R]}{P[G|\omega = R]} \left(1 + \frac{P[G|\omega = L]}{P[G|\omega = R]}\right) + (P[B|\omega = R]) \left(1 + \frac{P[B|\omega = L]}{P[B|\omega = R]}\right)\right)
\]

which simplifies to:

\[
1 = P[G|\omega = R] \left(\frac{1 + k - m}{2k}\right) + (1 - P[G|\omega = R]) \left(\frac{1 + m - k}{2(1 - k)}\right)
\]
Therefore, conditional on the state,
\[ P[G|GB \cap \omega = R] = k, \quad P[B|GB \cap \omega = R] = 1 - k \]
\[ P[G|GB \cap \omega = L] = 1 - m, \quad P[B|GB \cap \omega = L] = m \]

and unconditional on the state:
\[ P[G|GB] = \frac{1 + k - m}{2}, \quad P[B|GB] = \frac{1 + m - k}{2} \]

To calculate the likelihood of political identity preservation, and therefore, expected utility, it is helpful to recall that
\[ P[s = l|\omega = L] = k, \quad P[s = r|\omega = R] = m \]

The agent’s expected utility conditional on the state being \( \omega = R \) is:
\[ E[U_R|GB \cap \omega = R] = P[G|GB \cap \omega = R] + P[r|B \cap \omega = R] \cdot P[B|GB \cap \omega = R] \]
\[ = k + m (1 - k) \]

while the agent’s expected utility conditional on the state being \( \omega = L \) is:
\[ E[U_R|GB \cap \omega = L] = P[G|GB \cap \omega = L] + P[r|B \cap \omega = L] \cdot P[B|GB \cap \omega = L] \]
\[ = (1 - m) + (1 - k)m \]

The unconditional expected utility is simply a weighted average of the conditional expected utilities. If the agent’s beliefs about the signal structure of the Outside signal are correct, then:
\[ E[U_R|GB] = \frac{1}{2} \cdot E[U_R|GB \cap \omega = R] + \frac{1}{2} \cdot E[U_R|GB \cap \omega = L] \]
\[ = \frac{1 + k + m - 2km}{2} \]

A.2 The identity-L agent’s problem

Recall that:
\[ P[s = l|\omega = L] = k, \quad P[s = r|\omega = R] = m \]
The intuition behind the calculations is similar to the identity-$R$ agent’s problem. Furthermore, all one needs to do to arrive at these calculations is to use the calculations from the previous subsection, and replace $w$ with $1 - w$ and $k$ with $m$.

The MU for signal $G$ is 1. For signal $B$, the MU is $2k(\frac{1 - m}{1 + k - m})$. Finally, for signal $T$, the MU is 0. The price of each of these signals is determined according to the coefficient corresponding to it in the Martingale constraint $(\frac{m}{1 + m - k}) \cdot P_G + (\frac{1 - m}{1 + k - m}) \cdot P_B + 0 \cdot P_T = 0.5$. This price is simply the intermediate posterior generated by the signal. The MU-Price ratio is $\frac{1}{m} \frac{1 + m - k}{2m}$ for signal $G$, $\frac{2k(1 - m)}{(k + m)} = 2k$ for signal $B$, and undefined for signal $T$.

The signal structure $GT$ is optimal when $1 + m - k - 2km \geq 0$. If $1 + m - k - 2km \leq 0$, then signal structure $GB$ is optimal.

We can now calculate the probability of realization of different signals, the utility achieved, and the likelihood of voting for the preferred party under the signal structures $GT$ and $GB$.

**Signal structure $GT$:** Unconditional on the state, the likelihood that the signal $G$ is realized is $P[G] = \frac{1 + m - k}{2m}$, which is also the agent’s ex-ante expected utility.

Conditional on the state being $\omega = L$, the signal $G$ is always realized and so the agent’s expected utility is $E[U_L|GT \cap \omega = L] = P[G|\omega = L] = 1$.

Conditional on the state being $\omega = R$, the likelihood that signal $G$ is realized is $\frac{1 - k}{m}$. Whenever it is realized, the agent is able to preserve her political identity. Therefore, this also equals the agent’s expected utility ($E[U_L|G \cap \omega = R]$)

**Signal structure $GB$:** This signal structure is somewhat more complicated, and therefore, we use the following three equations.

\[
P[G|GB] + P[B|GB] = 1 \tag{5}
\]
\[
P[G|\omega = R] = \frac{1 - k}{m} \tag{6}
\]
\[
P[B|\omega = R] = \frac{k}{1 - m} \tag{7}
\]

Conditional on the state,

\[
P[G|GB \cap \omega = L] = m, \quad P[B|GB \cap \omega = L] = 1 - m
\]
\[
P[G|GB \cap \omega = R] = 1 - k, \quad P[B|GB \cap \omega = R] = k
\]
and unconditional on the state:

\[ P[G|GB] = \frac{1 + m - k}{2}, \quad P[B|GB] = \frac{1 + k - m}{2} \]

To calculate the likelihood of political identity preservation, and therefore expected utility, it is helpful to recall that:

\[ P[s = l|\omega = L] = k, \quad P[s = r|\omega = R] = m \]

The agent’s expected utility conditional on the state being \( \omega = L \) is:

\[
E[U_L|GB \cap \omega = L] = P[G|GB \cap \omega = L] + P[l|B \cap \omega = L] \cdot P[B|GB \cap \omega = L]
= m + k(1 - m)
\]

The agent’s expected utility conditional on the state being \( \omega = R \) is:

\[
E[U_L|GB \cap \omega = R] = P[G|GB \cap \omega = R] + P[l|B \cap \omega = R] \cdot P[B|GB \cap \omega = R]
= (1 - k) + (1 - m)k
\]

The unconditional expected utility is simply a weighted average of the conditional expected utilities. If the agent’s beliefs about the signal structure of the Outside signal are correct, then:

\[
E[U_L|GB] = \frac{1}{2} \cdot E[U_L|GB \cap \omega = R] + \frac{1}{2} \cdot E[U_L|GB \cap \omega = L]
= \frac{1 + k + m - 2km}{2}
\]

### A.3 Robustness to noise

We now show that the key results of the model remain unchanged if we incorporate a small amount of noise in the agents’ threshold for political identity preservation. This is very similar to and follows directly from Extension A in Kamenica & Gentzkow (2011) in which the authors find that the stochasticity in the receiver’s action means that the sender’s expected payoff function is smooth, and that the key results are unchanged.

Suppose that the belief threshold that identity-\(R\) agents have for the preservation of their political identity is stochastic, with mean \( P[\omega = R|S_t, s_t] = 0.5 \). The noise in the threshold implies that the agent’s preservation of her political identity is now stochastic, and varies continuously with the agent’s interim posterior. The smoothness of the agent’s
expected utility function in figure 12 is due to this stochasticity.

If there is a small amount of mean-zero, normally distributed noise in this threshold, then for a less precise Outside signal structure, as can be seen in figure 12, a $G^+T$ signal is optimal. The $G^+$ signal generates an interim posterior that is more favorable to party $R$ than a $G$ signal and in the case of normally distributed noise, it is optimal because it allows the agent to preserve her political identity for a large proportion of the possible realizations of the noise.

Similarly, for high-precision Outside signals, a $G^+B^+$ signal structure is optimal for identity-$R$ agents. For minute levels of noise, the optimal signal structures remain almost identical and would result in almost the same signal structures being chosen.

Since the key results in propositions 1, 3, 4, and 2 were not knife-edge, they are robust to stochasticity in the belief threshold, as long as that the variance of the noise is low.

A.4  Robustness to gain from being correct

We now show for the general model that the key results are robust to including a small gain from being correct in the agents’ utility function. In other words, in addition to a gain from political identity preservation, agents also gain utility from being correct about the state of the world. The utility function of an identity-$R$ agent is, therefore, modified
to become:

\[ U_R = \begin{cases} 
(1 - \gamma) + \gamma, & \text{if } \mathbb{P}[\omega = R|S,s] \geq 0.5 \text{ and } \omega = R \\
(1 - \gamma), & \text{if } \mathbb{P}[\omega = R|S,s] \geq 0.5 \text{ and } \omega = L \\
\gamma, & \text{if } \mathbb{P}[\omega = R|S,s] < 0.5 \text{ and } \omega = L \\
0, & \text{if } \mathbb{P}[\omega = R|S,s] < 0.5 \text{ and } \omega = R 
\end{cases} \]  

(8)

In this case, \( \gamma \in (0,1) \) captures the extent to which the agent gains utility from being correct as opposed to a signal that allows her to preserve her political identity.\(^\text{29}\)

We now show two key results for an identity-\( R \) agent. First, for a low value of \( \gamma \), \( GT \) and \( GB \) signal structures are sufficient to solve the agent’s problem. Second, as \( \gamma \) increases, the threshold at which the agent switches from a \( GT \) signal structure to a \( GB \) signal structure changes continuously. These two results together imply that the key results of the model are robust to small values of \( \gamma \). For an identity -\( L \) agent, the same results hold analogously.

Based on the above utility function, there are four interim posteriors (generated after the agent observes her Inside signal, and before she observes the Outside signal) that are key to solving the agent’s problem. Three are derived from the \( G, B, \) and \( T \) signals, while the fourth is an \textit{Excellent} or \( E \) signal. The signals must be such that:

\[
\begin{align*}
\mathbb{P}[\omega = R|S = G] &= \frac{k}{1 + k - m} \\
\mathbb{P}[\omega = R|S = B] &= \frac{1 - k}{1 + m - k} \\
\mathbb{P}[\omega = R|S = T] &= 0 \\
\mathbb{P}[\omega = R|S = E] &= 1
\end{align*}
\]

The set of signal structures that satisfy the Martingale property is:

\[ \{ET, GT, EB, GB, EBT, EGT, GBT, EGBT\} \]

We disregard the signal structures \( EBT, EGT, GBT, \) and \( EGBT \) because whenever one of them is optimal, a simpler signal structure will also be.

In the next step, we compare the ex-ante expected utilities of each of these signal structures to show that for low values of \( \gamma \), \( GT \) and \( GB \) are sufficient to solve the agent’s prob-

\(^{29}\gamma = 0 \) is the benchmark model. \( \gamma = 1 \) corresponds to a case in which the agent only wants to know the correct state. In that case, the agent will choose a fully revealing echo chamber signal structure.
lem.

**Signal structure** $ET$:

$$E[U_R|_{ET \cap \omega = R}] = 1, \quad E[U_R|_{ET \cap \omega = L}] = \gamma$$

$$E[U_R|_{ET}] = \frac{1 + \gamma}{2}$$

**Signal structure** $EB$:

$$E[U_R|_{EB \cap \omega = R}] = 1 - \frac{(1-k)(1-m)}{m}, \quad E[U_R|_{EB \cap \omega = L}] = 1 - \gamma - m + 2\gamma m$$

$$E[U_R|_{EB}] = 1 - \frac{1}{2}\left[\frac{(1-k)(1-m)}{m} + \gamma + m - 2\gamma m\right]$$

**Signal structure** $GT$:

$$E[U_R|_{GT \cap \omega = R}] = 1, \quad E[U_R|_{GT \cap \omega = L}] = \gamma + \frac{1-m}{k} - 2\gamma \frac{1-m}{k}$$

$$E[U_R|_{GT}] = \frac{1 + \gamma}{2} + \left(\frac{1-m}{k}\right) \left(\frac{1}{2} - \gamma\right)$$

**Signal structure** $GB$:

$$E[U_R|_{GB \cap \omega = R}] = k + m - km, \quad E[U_R|_{GB \cap \omega = L}] = \gamma + (1-2\gamma)(1-km)$$

$$E[U_R|_{GB}] = \frac{1 - \gamma + k + m}{2} - (1 - \gamma) km$$

**Claim 5** Suppose that $\gamma \leq 0.5$. The signal structures $GT$ and $GB$ are then sufficient to solve the agent’s problem.

**Proof.** We now show that the signal structure $GT$ provides the agent with at least as much expected utility as $ET$ or $EB$ as long as $\gamma \leq 0.5$.

$E[U_R|_{GT}] - E[U_R|_{ET}] \geq 0$ simplifies to $\left(\frac{1-m}{k}\right) \left(\frac{1}{2} - \gamma\right) \geq 0$, and holds if $\gamma \leq 0.5$.

Similarly, $E[U_R|_{GT}] - E[U_R|_{EB}] \geq 0$ simplifies to $(1-m)(1-k) \left(\frac{1-2\gamma}{k} + \frac{1}{m}\right) \geq 0$, and holds if $\gamma \leq 0.5$. ■
Because $E[U_R|_{GT}]$ and $E[U_R|_{GB}]$ are continuous functions of $\gamma$, the agent’s choice of Inside signal structure depends on a threshold that varies continuously with $\gamma$. Therefore, for low values of $\gamma$, the region of information aggregation failure doesn’t disappear completely, although it may shrink.

In general, as long as $\gamma \leq 0.5$, there exists a region of information aggregation failure. If $\gamma > 0.5$, then all agents optimally choose an ET signal structure and there is no information aggregation failure.

Consider the parameters used in the example in the introduction. Specifically, suppose the precision of the Outside signal is 0.51 for identity-R agents and 0.75 for identity-L agents. Then, as long as $\gamma < 0.2$, identity-R agents would optimally choose a GT signal structure and identity-L agents would prefer a GB signal structure, and information aggregation failure would occur.

### A.5 Robustness to gain from holding more favorable posteriors

We now show that if the agents also gain utility from holding posteriors that are more favorable to their preferred party, then for all levels of that gain, the results are identical.

The utility function of an identity-R agent is now modified to become:

$$U_R = \begin{cases} (1 - \lambda) + \lambda \mathbb{P}[\omega = R|S,s] & \text{if } \mathbb{P}[\omega = R|S,s] \geq 0.5 \\ \lambda \mathbb{P}[\omega = R|S,s] & \text{if } \mathbb{P}[\omega = R|S,s] < 0.5 \end{cases}$$

As in the earlier setup, the agent gains a utility from preserving her political identity. She also gains some utility from holding favorable posteriors. Here, $\lambda \in [0,1)$ captures the weight that the agent places on holding more favorable posteriors, while $1 - \lambda$ is the agent’s utility from preserving her political identity.$^{30}$

Based on the above utility function, there are three interim posteriors (generated after the agent observes her Inside signal, and before she observes the Outside signal) which are key to solving the agent’s problem, and which are the same as in the benchmark

---

$^{30}$ $\lambda = 0$ is the benchmark model. $\lambda = 1$ corresponds to a case in which the agent’s utility is linear in how favorable her posterior belief is towards her party.
model:

\[
P[\omega = R | S = G] = \frac{k}{1 + k - m} \\
P[\omega = R | S = B] = \frac{1 - k}{1 + m - k} \\
P[\omega = R | S = T] = 0
\]

As in the benchmark model, only two signal structures are required to solve the agent’s problem, i.e. GT and GB. Furthermore, the trade-off between the two signals remains unchanged. Specifically, the agent chooses GT if the MU-Price ratio of the G signal is at least as large as that of the B signal. This simplifies to:

\[
\frac{\text{MU}_G}{P_G} \geq \frac{\text{MU}_B}{P_B} \\
\frac{\lambda \frac{k}{1+k-m} + (1 - \lambda)}{1 + \frac{k}{1+k-m}} \geq \frac{\lambda \frac{(1-k)}{1+m-k} + (1 - \lambda) \frac{2m(1-k)}{1+m-k}}{1 + m - k} \\
\lambda + \frac{(1 - \lambda)(1 + k - m)}{k} \geq \lambda + (1 - \lambda)(2m) \\
1 + k - m - 2km \geq 0
\]

This condition is identical to the one in the benchmark model. Therefore, the agent’s choice of Inside signal structure remains unchanged in this modified model. This also implies that the results of the modified model are identical to those of the benchmark for all values of \( \lambda \in [0, 1] \).

B Applications

B.1 Asymmetric exposure to an unbiased Outside signal

An identity-\( L \) agent receives an Outside signal such that:

\[
P[s = l | \omega = L] = t \in [0.5, 1], \quad P[s = r | \omega = R] = t \in [0.5, 1]
\]

An identity-\( R \) agent receives a less precise Outside signal:

\[
P[s = l | \omega = L] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1], \quad P[s = r | \omega = R] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1]
\]
where $\tau \in [0, 1]$.

**B.1.1 The identity-$R$ agent’s problem**

We use the results developed in Appendix A.1 and simply plug in $k = m = \frac{1 - \tau}{2} + \tau t$.

**Signal structure $GT$:** This signal structure is chosen if $\tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \leq \frac{1}{\sqrt{2}} \approx 0.71$.

The agent’s expected utilities are the same as her likelihood of political identity preservation and are equal to:

\[
E[U_R|_{GT \cap \omega = R}] = 1, \quad E[U_R|_{GT \cap \omega = L}] = \frac{1 + \tau - 2\tau t}{1 - \tau + 2\tau t}
\]

Unconditioned on the realization of the state, the ex-ante expected utility is

\[
E[U_R|_{GT}] = \frac{1}{1 - \tau + 2\tau t}
\]

**Signal structure $GB$:** This signal structure is chosen if $\tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \geq \frac{1}{\sqrt{2}} \approx 0.71$.

The agent’s expected utilities are the same as the likelihood of political identity preservation for the agent, and they equal:

\[
E[U_R|_{GB \cap \omega = R}] = \frac{3}{4} + \tau t - \frac{\tau}{2} - \tau^2 \left(\frac{1}{4} + t^2 - t\right), \quad E[U_R|_{GB \cap \omega = L}] = 1 - \left(\frac{1 - \tau + 2\tau t}{2}\right)^2
\]

Unconditioned on the realization of the state, the ex-ante expected utility is

\[
E[U_R|_{GB}] = \frac{3}{4} - \tau^2 \left(t^2 + \frac{1}{4} - t\right)
\]

**B.1.2 The identity-$L$ agent’s problem**

**Signal structure $GT$:** This signal structure is chosen if $t \leq \frac{1}{\sqrt{2}} \approx 0.71$.

\[
E[U_L|_{GT \cap \omega = R}] = \frac{1 - t}{t}, \quad E[U_L|_{GT \cap \omega = L}] = 1
\]

**Signal structure $GB$:** This signal structure is chosen if $t \geq \frac{1}{\sqrt{2}} \approx 0.71$.

\[
E[U_L|_{GB \cap \omega = R}] = 1 - t^2, \quad E[U_L|_{GB \cap \omega = L}] = 2t - t^2
\]
B.1.3 Proof of proposition 1

**Proof.** Suppose that $\tau = 0.04$ and $t = 0.75$. An identity-$R$ agent chooses a $GT$ signal structure because $\tau \cdot t + (1 - \tau) \cdot \frac{1}{2} = 0.51 < \frac{1}{\sqrt{2}}$, while identity-$L$ agent chooses a $GB$ signal structure because $t = 0.75 > \frac{1}{\sqrt{2}}$. These conditions hold in the neighborhood of the parameter values $\tau = 0.04$ and $t = 0.75$. Since the likelihood of political identity preservation is continuous in these parameter values, and since the margin of victory for party $R$ in state $L$ at these parameter values is bounded away from zero, the result of information aggregation failure holds for a non-trivial subset of values.

If agents of both identities choose a $GT$ signal structure, and if the state of the world is $R$, then all identity-$R$ agents vote for party $R$, and some identity-$L$ agents also vote for party $R$. If the state of the world is $L$, then all identity-$L$ agents vote for party $L$ and some identity-$R$ agents also vote for party $L$. Clearly, the correct party wins in either state.

Furthermore, there is no parameter space in which identity-$R$ agents choose a $GB$ signal structure while identity-$L$ agents choose a $GT$ signal structure.

If agents of both identities choose a $GB$ signal structure and if the state of the world is $R$, then party $R$ wins if:

$$\frac{3}{4} + \tau t - \frac{\tau}{2} - \tau^2 \left(\frac{1}{4} + t^2 - t\right) > 1 - t^2$$

which simplifies to:

$$\tau \left( t - \frac{1}{2} \right) \left( 1 - \tau \left( t - \frac{1}{2} \right) \right) + \left( t^2 - \frac{1}{4} \right) > 0$$

which always holds.

Similarly, if the state of the world is $L$, then party $L$ wins if:

$$1 - \left( \frac{1 - \tau + 2\tau t}{2} \right)^2 < 2t - t^2$$

which simplifies to:

$$\left( \frac{1 - \tau + 2\tau t}{2} \right)^2 - (1 - t)^2 > 0$$

This always holds because $1 - t \in [0, 0.5]$ while $\left( \frac{1 - \tau + 2\tau t}{2} \right) \in [0.5, 1]$. ■
B.2 Correlated signals

In our model, we suppose that the signals (Inside and Outside) realize independently. That is, the two signals are independent of each other and they realize independently for each agent. In the key example in the Introduction, we saw that party R wins for sure in either state of the world. Because the winning margin of party R is positive (specifically, bounded away from zero), we know that the result of information aggregation failure is robust to some, possibly small, degree of correlation of the two signals.

Below, we consider three cases of correlated signals. In each case, we suppose that the two signals (Inside and Outside) realize independently. For ease of illustrating the effects, we also suppose that there is full correlation in the realization of the signal across all agents of a particular identity. Finally, we fix parameter values to be the same as studied in the key example of the paper. That is, there is an equal proportion of infinite identity-$R$ and identity-$L$ agents. Identity-$R$ agents receive a less precise Outside signal than identity-$L$ agents ($t_R = 0.51$ and $t_L = 0.75$). The common prior belief is that each state of the world is equally likely.

First, we consider the case that the Outside signal realization is fully correlated across agents of the same identity. Second, we suppose that Inside signal realization is fully correlated in the same way. Finally, we study the situation where both signals are fully correlated in the way they realize for all agents of the same identity. In each scenario, since the Outside signals realize independently of the Inside signal, the optimal signal structure choice for agents remains the same as in the baseline model. This implies that the expected winning margin advantage for party R remains the same ex-ante ($+29\%$) and conditional on the state being $R$ ($+56\%$) or $L$ ($+2\%$). The aggregate implications of this expected winning margin advantage vary according to the kind of correlation we consider. In each case, party R wins with a higher probability than party L. Table 3 illustrates the outcomes, and the probabilities with which those occur, conditional on the state of the world and for each case of correlated signals we consider.

**Outside signals:** Suppose the Outside signals are fully correlated such that either all identity-$R$ agents receive favorable news from the Outside, or all of them receive unfavorable news. The correlation functions similarly for all identity-$L$ agents. Here, we find that the likelihood that party R wins is 50%, while the same for party L is 37.5%. The chance of a tie is 12.5%.

Note that a tie occurs with a probability of 25% in state R. This is when all identity-$R$ individuals, having observed a G Inside signal, preserve their political identity, and all identity-$L$ citizens also preserve their political identity because all of them receive a favorable Outside signal. If the correlation of the realization...
Table 3: Outcomes and probabilities with correlated signals

<table>
<thead>
<tr>
<th>Correlated Outside signal</th>
<th>( \omega = R )</th>
<th>( \omega = L )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Probability</td>
<td>Win Margin R</td>
<td>Probability</td>
</tr>
<tr>
<td>0.75</td>
<td>+75%</td>
<td>0.25</td>
</tr>
<tr>
<td>0.25</td>
<td>0%</td>
<td>0.75</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Correlated Inside signal</th>
<th>( \omega = R )</th>
<th>( \omega = L )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Probability</td>
<td>Win Margin R</td>
<td>Probability</td>
</tr>
<tr>
<td>0.75</td>
<td>+75%</td>
<td>0.2402</td>
</tr>
<tr>
<td>0.25</td>
<td>0%</td>
<td>0.7206</td>
</tr>
<tr>
<td>0.0098</td>
<td>−75%</td>
<td>0.0294</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Correlated Inside and Outside signals</th>
<th>( \omega = R )</th>
<th>( \omega = L )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Probability</td>
<td>Win Margin R</td>
<td>Probability</td>
</tr>
<tr>
<td>0.5625</td>
<td>+100%</td>
<td>0.06005</td>
</tr>
<tr>
<td>0.4375</td>
<td>0%</td>
<td>0.9032</td>
</tr>
<tr>
<td>0.03675</td>
<td>−100%</td>
<td></td>
</tr>
</tbody>
</table>

**Inside signals:** Suppose the Inside signals are fully correlated such that if \( GT \) is the chosen signal structure for identity-\( R \) agents, then either they all receive a \( G \) signal, or all of them receive a \( T \) signal. The correlation functions similarly for all identity-\( L \) agents. Here, we find that the likelihood that party \( R \) wins is 49.51%, while the same for party \( L \) is 1.96%. The chance of a tie is 48.53%.

**Inside and Outside signals:** Suppose that both, the Inside and Outside signals are fully correlated in how they realize for agents of the same identity. Crucially, they realize independently of each other. Here, we find that the likelihood that party \( R \) wins is 31.13%, while the same for party \( L \) is 1.84%. The chance of a tie is 67.03%.

**B.3 Non-common priors**

Suppose that identity-\( R \) and identity-\( L \) agents have different priors. Specifically,

\[
P_R[\omega = R] := w_R \quad P_L[\omega = R] := w_L
\]

of the Outside signal was anything less than full, then instead of a tie, party \( R \) would win.
where $w_L < 0.5 < w_R$.

As in Subsection ??, an identity-$L$ agent receives an Outside signal, such that:

$$P[s = l|\omega = L] = t \in [0.5, 1], \quad P[s = r|\omega = R] = t \in [0.5, 1]$$

An identity-$R$ agent receives a less precise Outside signal, such that:

$$P[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1], \quad P[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1]$$

where $\tau \in [0, 1]$

B.3.1 The identity-$R$ agent’s problem

We use the results developed in Appendix A.1 and allow for $w_R > 0.5$ while plugging in $k = m = \frac{1-\tau}{2} + \tau t$.

**Signal structure $N$:** This signal structure is chosen if $\tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \leq w_R$.

The agent is able to preserve her political identity regardless of the realization of the Outside signal.

$$E[U_R|N \cap \omega = R] = 1, \quad E[U_R|N \cap \omega = L] = 1$$

**Signal structure $GT$:** This signal structure is chosen if $w_R < \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \leq \frac{1}{\sqrt{2}} \approx 0.71$.

The agent’s expected utilities are the same as her likelihood of political identity preservation, and are equal to:

$$E[U_R|GT \cap \omega = R] = 1, \quad E[U_R|GT \cap \omega = L] = \frac{w_R(1 + \tau - 2\tau t)}{(1 - w_R)(1 - \tau + 2\tau t)}$$

**Signal structure $GB$:** This signal structure is chosen if $\tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \geq \max\{\frac{1}{\sqrt{2}}, w_R\}$.

The agent’s expected utilities are the same as her likelihood of political identity preservation, and are equal to:

$$E[U_R|GB \cap \omega = R] = \frac{(2\tau t + 1 - \tau)(2\tau t - 1 - \tau)}{4w_R \tau (2t - 1)} + \frac{(2\tau t + 1 - \tau)(2\tau t + 1 - \tau - 2w_R)(1 + \tau - 2\tau t)}{8w_R \tau (2t - 1)}$$
and
\[ E[U_R|_{GB\cap \omega = L}] = \frac{(1 + \tau - 2\tau t)(2\tau t - 1 - \tau)}{4(1 - w_R)\tau(2t - 1)} + \frac{(2\tau t + 1 - \tau)(2\tau t + 1 - \tau - 2w_R)(1 + \tau - 2\tau t)}{8(1 - w_R)\tau(2t - 1)} \]

B.3.2 The identity-\(L\) agent’s problem

Signal structure \(N\): This signal structure is chosen if \(t \leq 1 - w_L\).

The agent is able to preserve her political identity regardless of the realization of the Outside signal.

\[ E[U_L|_{N\cap \omega = R}] = 1, \quad E[U_L|_{N\cap \omega = L}] = 1 \]

Signal structure \(GT\): This signal structure is chosen if \(1 - w_L < t \leq \frac{1}{\sqrt{2}} \simeq 0.71\).

\[ E[U_L|_{GT\cap \omega = R}] = \frac{(1 - w_L)(1 - t)}{wLt}, \quad E[U_L|_{GT\cap \omega = L}] = 1 \]

Signal structure \(GB\): This signal structure is chosen if \(t \geq \max\{\frac{1}{\sqrt{2}}, 1 - w_L\}\).

\[ E[U_L|_{GB\cap \omega = R}] = \frac{(1 - t)(t - w)}{w(2t - 1)} + \frac{t(1 - t)(t + w - 1)}{w(2t - 1)} \]

and
\[ E[U_L|_{GB\cap \omega = L}] = \frac{t(2t - 1 - \tau^2 + (1 - w)t)}{(1 - w)(2t - 1)} \]

B.4 Distrust in the mainstream media’s precision

Suppose that identity-\(R\) agents believe (incorrectly) that the media is less precise than it actually is. Specifically, identity-\(L\) agents correctly believe that the process generating the Outside signal is such that:

\[ P[s = l|\omega = L] = t \in [0.5, 1], \quad P[s = r|\omega = R] = t \in [0.5, 1] \]

In contrast, identity-\(R\) agents incorrectly believe that the process that generates the Outside signal is more noisy, such that:

\[ P[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1], \quad P[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot \frac{1}{2} \in [0.5, 1] \]
where $\tau \in [0, 1]$.

This is similar to an asymmetry in exposure to mainstream media. As such, the signal choices and expected utilities are identical to those calculated in Subsection B.1.

For identity-\(L\) agents, the probability of political identity preservation is identical to the expected utilities calculated in Subsection B.1.

For identity-\(R\) agents, if the chosen signal is of type \(GT\), then the probability of political identity preservation is identical to the expected utility calculated in Subsection B.1. If the chosen signal is of type \(GB\), then an identity-\(R\) agent’s probability of political identity preservation is calculated conditioned on the state.

If the state is \(\omega = R\), then:

$$\mathbb{P}(\text{PFP}_R|GB \cap \omega = R) = \mathbb{P}(G|GB \cap \omega = R) + \mathbb{P}(r|B \cap \omega = R) \cdot \mathbb{P}(B|GB \cap \omega = R)$$

$$= \left(\frac{1 - \tau}{2} + \tau t\right) + \left(\frac{1 + \tau}{2} - \tau t\right)$$

$$= \frac{1}{2} \left(1 - \tau + t + 3\tau t - 2\tau t^2\right)$$

If the state is \(\omega = L\), then:

$$\mathbb{P}(\text{PFP}_R|GB \cap \omega = L) = \mathbb{P}(G|GB \cap \omega = L) + \mathbb{P}(r|B \cap \omega = L) \cdot \mathbb{P}(B|GB \cap \omega = L)$$

$$= \left(\frac{1 + \tau}{2} - \tau t\right) + (1 - t) \cdot \left(\frac{1 - \tau}{2} + \tau t\right)$$

$$= \frac{1}{2} \left(2 - t + \tau t - 2\tau t^2\right)$$

**B.5 Distrust in unbiasedness of mainstream media**

Suppose that the true process of the Outside signal is:

$$\mathbb{P}(s = l|\omega = L) = t \in [0.5, 1], \quad \mathbb{P}(s = r|\omega = R) = t \in [0.5, 1]$$

Identity-\(L\) agents know the true process, while identity-\(R\) agents believe that the process of the Outside signal is biased in the following way:

$$\mathbb{P}(s = l|\omega = L) = \tau \cdot t + (1 - \tau) \cdot 1, \quad \mathbb{P}(s = r|\omega = R) = \tau \cdot t + (1 - \tau) \cdot 0$$

where $\tau \in [0, 1]$.

---

For identity-\(R\) agents, the expectations are based on incorrect beliefs. We will, therefore, separately calculate the probability of political identity preservation.
B.5.1 The identity-\(R\) agent’s problem

**GT signal structure:** This signal structure is chosen if \(2 - \tau - 2\tau t - 2\tau^2t^2 + 2\tau^2t \geq 0\).

The agent’s expected utilities are:

\[
E[U_{R|\text{GT}\cap\omega=R}] = 1, \quad E[U_{R|\text{GT}\cap\omega=L}] = \frac{1 - \tau t}{1 + \tau t - \tau}
\]

If the agent chooses a \(GT\) signal structure, then the likelihood of political identity preservation does not depend on the realization of the Outside signal. Therefore, the likelihood of political identity preservation is identical to the expected utility.

**GB signal structure:** This signal structure is chosen if \(2 - \tau - 2\tau t - 2\tau^2t^2 + 2\tau^2t \leq 0\).

The agent’s expected utilities (under incorrect beliefs) are:

\[
E[U_{R|\text{GB}\cap\omega=R}] = 1 - \tau + \tau t + \tau^2t - \tau^2t^2, \quad E[U_{R|\text{GB}\cap\omega=L}] = 1 - \tau t + \tau^2t - \tau^2t^2
\]

In this case, the likelihood of political identity preservation differs from the agent’s expected utility, such that:

\[
P[F_{\text{FP}R|\text{GB}\cap\omega=R}] = 1 - \tau + 2\tau t - \tau^2, \quad P[F_{\text{FP}R|\text{GB}\cap\omega=L}] = 1 - \tau^2t^2
\]

B.5.2 The identity-\(L\) agent’s problem

**GT signal structure:** This signal structure is chosen if \(t \leq \frac{1}{\sqrt{2}}\).

The agent’s expected utilities are:

\[
E[U_{L|\text{GT}\cap\omega=R}] = \frac{1 - t}{t}, \quad E[U_{L|\text{GT}\cap\omega=L}] = 1
\]

**GB signal structure:** This signal structure is chosen if \(t \geq \frac{1}{\sqrt{2}}\).

The agent’s expected utilities are:

\[
E[U_{L|\text{GB}\cap\omega=R}] = 1 - t^2, \quad E[U_{L|\text{GB}\cap\omega=L}] = 2t - t^2
\]

B.5.3 Proof of proposition

**Proof.** Suppose that \(\tau = 0.1\) and \(t = 0.75\). An identity-\(R\) agent chooses a \(GT\) signal structure because \(2 - \tau - 2\tau t - 2\tau^2t^2 + 2\tau^2t \simeq 1.75 > 0\). An identity-\(L\) agent chooses a \(GB\) signal structure because \(t = 0.75 > \frac{1}{\sqrt{2}}\). These conditions hold in the neighborhood
of the parameter values $\tau = 0.1$ and $t = 0.75$. Since the likelihood of political identity preservation is continuous in these parameter values, and since the margin of victory for party $R$ in state $L$ at these parameter values is bounded away from zero, the result of information aggregation failure holds for a non-trivial subset of values.

If agents of both identities choose a $GT$ signal structure, and if the state of the world is $R$, then all identity-$R$ agents vote for party $R$, and some identity-$L$ agents also vote for party $R$. If the state of the world is $L$, then all identity-$L$ agents vote for party $L$ and some identity-$R$ agents also vote for party $L$. Clearly, the correct party wins in either state.

There is no parameter space where identity-$R$ agents choose a $GB$ signal structure while identity-$L$ agents choose a $GT$ signals structure.

If agents of both identities choose a $GB$ signal structure, and if the state of the world is $R$, then party $R$ wins if:

$$1 - \tau + 2\tau t - \tau t^2 > 1 - t^2$$

This simplifies to:

$$\tau(2t - 1) + t^2(1 - \tau) > 0$$

which always holds.

Similarly, if the state of the world is $L$, then party $L$ wins if:

$$2t - t^2 > 1 - \tau t^2$$

which simplifies to:

$$(2t - 1) - t^2(1 - \tau) > 0$$

which holds for values of $t \in \left[\frac{1}{\sqrt{2}}, 1\right]$ and $\tau \in \left[\frac{2}{3}, 1\right]$. The region where agents of both identities choose a $GB$ signal structure is a subset of the region where $t \in \left[\frac{1}{\sqrt{2}}, 1\right]$ and $\tau \in \left[\frac{2}{3}, 1\right]$. Therefore, if agents of both identities choose a $GB$ signal structure, then the correct party wins. ■
B.6 Propagandized Outside signal with censorship

Here that the Outside signal is biased towards party $L$, which is common knowledge. The structure of the Outside signal is:

$$
\mathbb{P}[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot 1,
\mathbb{P}[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
$$

where $t > 0.5$.

We can use the results from Appendix A.1 and A.2 by simply plugging in $k = 1 + \tau t - \tau$ and $m = \tau t$.

Because we are considering censorship, no agent of either identity has access to any information other than her prior and the realized Outside signal. The agents share common and symmetric priors, and their posteriors on observing the Outside signals are:

$$
Pr[\omega = L|s = l] = \frac{1 + \tau t - \tau}{2 - \tau}
$$

Since $t > 0.5$, $Pr[\omega = L|s = l] > 0.5$

and

$$
Pr[\omega = L|s = r] = 1 - t
$$

Since $t > 0.5$, $Pr[\omega = L|s = r] < 0.5$

For party $L$ to win in state $R$, we require that $Pr(s = l|\omega = R) > Pr(s = r|\omega = R)$ or $1 - \tau t > \tau t$. That is, $\tau t < 0.5$.

For party $L$ to win in state $L$, we require that $Pr(s = l|\omega = L) > Pr(s = r|\omega = L)$ or $1 + \tau t - \tau > \tau - \tau t$. That is, $\tau(1 - t) < 0.5$. If $\tau \in [0, 1]$, and $t > 0.5$, or if $\tau \in (0, 1]$ and $t \geq 0.5$ then this always holds.

Therefore, party $L$ can win in both states of the world if $\tau t < 0.5$.

B.7 Propagandized Outside signal without censorship

Here, that the Outside signal is biased towards party $L$, and this bias is common knowledge. The structure of the Outside signal is:

$$
\mathbb{P}[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot 1,
\mathbb{P}[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
$$

where $t > 0.5$.

We can use the results from Appendix A.1 and A.2 by simply plugging in $k = 1 + \tau t - \tau$ and $m = \tau t$. 

64
B.7.1 The identity-\(R\) agent’s problem

**GT signal structure:** Chosen if \(2 - \tau - 2t - 2\tau^2t^2 + 2\tau^2t \geq 0\).

The agent’s expected utilities are:

\[
E[U_{R|GT\cap\omega=R}] = 1, \quad E[U_{R|GT\cap\omega=L}] = \frac{1 - \tau t}{1 + \tau t - \tau}
\]

**GB signal structure:** Chosen if \(2 - \tau - 2t - 2\tau^2t^2 + 2\tau^2t \leq 0\).

The agent’s expected utilities are:

\[
E[U_{R|GB\cap\omega=R}] = 1 - \tau + \tau t + \tau^2t - \tau^2t^2, \quad E[U_{R|GB\cap\omega=L}] = 1 - \tau t + \tau^2t - \tau^2t^2
\]

B.7.2 The identity-\(L\) agent’s problem

**GT signal structure:** Chosen if \(\tau(1 - 2t - 2\tau t^2 + 2\tau t) \geq 0\) The agent’s expected utilities are:

\[
E[U_{L|GT\cap\omega=R}] = \frac{1 - t}{t}, \quad E[U_{L|GT\cap\omega=L}] = 1
\]

**GB signal structure:** Chosen if \(\tau(1 - 2t - 2\tau t^2 + 2\tau t) \leq 0\) The agent’s expected utilities are:

\[
E[U_{L|GB\cap\omega=R}] = 1 - \tau t + \tau^2t - \tau^2t^2, \quad E[U_{L|GB\cap\omega=L}] = 1 - \tau + \tau t + \tau^2t - \tau^2t^2
\]

B.7.3 Proof of proposition 3

**Proof.** Suppose that \(\tau = 0.3\) and \(t = 0.6\). Type-\(R\) agents choose a \(GT\) signal structure because \(2 - \tau - 2t - 2\tau^2t^2 + 2\tau^2t = 1.3832 > 0\), while an identity-\(L\) agents choose a \(GB\) signal structure because \(\tau(1 - 2t - 2\tau t^2 + 2\tau t) = -0.0168 < 0\). These conditions hold in the neighborhood of the parameter values \(\tau = 0.3\) and \(t = 0.6\). Since the likelihood of political identity preservation is continuous in these parameter values, and since the margin of victory for party \(R\) in state \(L\) at these parameter values is bounded away from zero, the result of information aggregation failure holds for a non-trivial subset of values.

If agents of both identities choose a \(GT\) signal structure, and if the state of the world is \(R\), then all identity-\(R\) agents vote for party \(R\), and some identity-\(L\) agents also vote for party \(R\). If the state of the world is \(L\), then all identity-\(L\) agents vote for party \(L\) and some identity-\(R\) agents also vote for party \(L\). Clearly, the correct party wins in either state.
There is no parameter space where identity-\(R\) agents choose a \(GB\) signal structure while identity-\(L\) agents choose a \(GT\) signals structure.

If agents of both identities choose a \(GB\) signal structure, and if the state of the world is \(R\), then party \(R\) wins if:

\[
1 - \tau + \tau t + \tau^2 t - \tau^2 t^2 > 1 - \tau t + \tau^2 t - \tau^2 t^2
\]

which simplifies to:

\[
\tau(2t - 1) > 0
\]

which always holds.

Similarly, if the state of the world is \(L\), then party \(L\) wins if:

\[
1 - \tau + \tau t + \tau^2 t - \tau^2 t^2 > 1 - \tau t + \tau^2 t - \tau^2 t^2
\]

which simplifies to:

\[
\tau(2t - 1) > 0
\]

which always holds.

\[\blacksquare\]

### B.8 Propaganda with oblivious citizens

In this case, that the true process of the Outside signal is:

\[
P[s = l|\omega = L] = \tau \cdot t + (1 - \tau) \cdot 1, \quad P[s = r|\omega = R] = \tau \cdot t + (1 - \tau) \cdot 0
\]

where \(\tau \in [0, 1]\) and \(t \in [0.5, 1]\). Agents don’t know that the true process, and believe that the process generating the Outside signal is unbiased, such that:

\[
P[s = l|\omega = L] = t, \quad P[s = r|\omega = R] = t
\]

#### B.8.1 The identity-\(R\) agent’s problem

**\(GT\) signal structure:** This signal structure is chosen if \(t \leq \frac{1}{\sqrt{2}}\)

The agent’s expected utilities are:

\[
E[U_R|_{GT \cap \omega = R}] = 1, \quad E[U_R|_{GT \cap \omega = L}] = \frac{1 - t}{t}
\]
If the agent chooses a $GT$ signal structure, then the likelihood of political identity preservation does not depend on the realization of the Outside signal. Therefore, the likelihood of political identity preservation is identical to the expected utility.

**GB signal structure:** This signal structure is chosen if $t \geq \frac{1}{\sqrt{2}}$. The agent’s expected utilities (under incorrect beliefs) are:

$$E[U_R|_{GB\cap \omega=R}] = 2t - t^2,$$
$$E[U_R|_{GB\cap \omega=L}] = 1 - t^2$$

Here, the likelihood of political identity preservation differs from the agent’s expected utility.

$$P[PFP_R|_{GB\cap \omega=R}] = t(1 + \tau - \tau t), \quad P[PFP_R|_{GB\cap \omega=L}] = (1 + \tau t)(1 - t)$$

**B.8.2 The identity-L agent’s problem**

**GT signal structure:** This signal structure is chosen if $t \leq \frac{1}{\sqrt{2}}$. The agent’s expected utilities are:

$$E[U_L|_{GT\cap \omega=R}] = \frac{1-t}{t}, \quad E[U_L|_{GT\cap \omega=L}] = 1$$

If the agent chooses a $GT$ type signal structure, then the likelihood of political identity preservation does not depend on the realization of the Outside signal. Therefore, the likelihood of political identity preservation is identical to the expected utility.

**GB signal structure:** This signal structure is chosen if $t \geq \frac{1}{\sqrt{2}}$. The agent’s expected utilities (under incorrect beliefs) are:

$$E[U_L|_{GB\cap \omega=R}] = 1 - t^2,$$
$$E[U_L|_{GB\cap \omega=L}] = 2t - t^2$$

In this case, the likelihood of political identity preservation differs from the agent’s expected utility, such that:

$$P[PFP_L|_{GB\cap \omega=R}] = 1 - \tau t^2,$$
$$P[PFP_L|_{GB\cap \omega=L}] = 1 - \tau(1 - t)^2$$
Proof. Suppose that $\tau = 0.1$ and $t = 0.75$. Both agents of both identities choose a $GB$ signal structure for their Inside media because $t > \frac{1}{\sqrt{2}}$. These conditions hold in the neighborhood of the parameter values $\tau = 0.1$ and $t = 0.75$. Since the likelihood of political identity preservation is continuous in these parameter values, and since the margin of victory for party $L$ in state $R$ at these parameter values is bounded away from zero, the result of information aggregation failure holds for a non-trivial subset of values.

If agents of both identities choose a $GT$ signal structure, and if the state of the world is $R$, then all identity-$R$ agents vote for party $R$, and some identity-$L$ agents also vote for party $R$. If the state of the world is $L$, then all identity-$L$ agents vote for party $L$ and some identity-$R$ agents also vote for party $L$. Clearly, the correct party wins in either state.

There is no parameter space in which agents of the two identities choose different signal structures for their respective Inside media consumption.

If agents of both identities choose a $GB$ signal structure, and if the state of the world is $L$, then party $L$ wins if:

$$1 - \tau (1 - t)^2 > (1 + \tau t)(1 - t)$$

This simplifies to:

$$t + \tau t - \tau > 0$$

which always holds.

Furthermore, if the state of the world is $R$, then party $L$ wins if:

$$1 - \tau t^2 > t(1 + \tau - \tau t)$$

which simplifies to

$$t < \frac{1}{1+\tau}$$

Therefore, party $L$ wins regardless of the state if $t \in \left(\frac{1}{\sqrt{2}}, \frac{1}{1+\tau}\right)$. There are no parameter values for which party $R$ can win in state $L$. ■