

# Keeping up with peers in India

A new social interactions model of perceived needs

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  - show identification
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In our model:

- utility function has *needs*
  - act like negative income,
  - may depend on group-average expenditures (on many goods).
- Unlike typical social interactions models,
  - utility maximization implies nonlinearity in peer effects,
  - we can have group-level fixed (or random) effects,
  - a fixed (and small) number of group members are observed.

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  - Stevenson and Wolfers (2008): probably get somewhat happier;
  - Fliessbach et al (2007): fMRI evidence on relative rewards;
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  - also, Ravina (2008) and Clark and Senik (2010).
- This paper: use revealed preference instead of stated well-being.

# Empirical Consumption Peer Effects

- Veblen/observability
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  - De Giorgi, Frederiksen and Pistaferri (2016) use unbelievable Danish consumption data
- All find big externalities. But magnitude or significance of effects of  $\bar{q}$  or  $\bar{x}$  on behaviour does not measure economic implications or identify welfare effects. More structure is needed for that.

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- Different commodities have similar externalities
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    - luxuries and necessities
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- Estimates similar to well-being-based estimates
  - highly educated vs primary educated vs uneducated

# Object of Interest

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$$V_i = ax_i + b\bar{x}_g.$$

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- In this paper, we take a derivative and use consumer behaviour to illuminate the same externality.

# What's At Stake?

- If  $\alpha$  is large:
- the pareto set for helicopter drops of income is different from the standard model
  - the helicopter drop has to be somewhat equal, compensating everyone in the group for the externality
- interventions (e.g., taxation) that induce deadweight loss and thus reduce consumption are less bad in welfare terms (though their benefits might be similarly attenuated)
  - Boskin and Sheshinski (1978) show that the marginal cost of public funds is different
  - the MCPF for redistribution in the presence of costly transfers is lower, inducing a more equal optimal distribution of income
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- interventions that provide public goods may be better than those that provide private goods
- if  $\alpha$  is very large, we're burning down the Earth for nothing

# Paper in 3 Lines

- $i$  indexes households,  $g$  indexes groups (of households). overbars indicate true within-group means, hats indicate sample averages.  $\mathbf{q}$  is quantity vector,  $\mathbf{p}$  is price vector,  $x$  is budget,  $\mathbf{z}$  is characteristics.

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- (reference point) direct utility  $U$  and indirect utility  $V$

$$U_i(\mathbf{q}) = U(\mathbf{q} - \mathbf{f}_i)$$

- $\mathbf{f}_i$  is **needs** (aka: fixed costs, overheads).  $\mathbf{f}_i$  depend on  $\bar{\mathbf{q}}_g$  (and  $\mathbf{z}_i$ ).

$$V_i(\mathbf{p}, x) = V(\mathbf{p}, x - \mathbf{p}'\mathbf{f}_i)$$

- if  $\mathbf{f}_i = \alpha\bar{\mathbf{q}}_g$ ,  $\mathbf{p}'\mathbf{f}_i = \alpha\bar{x}_g$ , and  $V_i(\mathbf{p}, x) = V(\mathbf{p}, x - \alpha\bar{x}_g)$

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- Roy's Identity gives demand functions  $\mathbf{q}_i$ , add error terms  $\mathbf{v}_g$ ,  $\mathbf{u}_i$ :

$$\mathbf{q}_i = \mathbf{h}_i(\mathbf{p}, x) = \mathbf{h}(\mathbf{p}, x - \mathbf{p}'\mathbf{f}_i) + \mathbf{f}_i + \mathbf{v}_g + \mathbf{u}_i$$

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- Econometrics: reflection; endogeneity of  $\bar{\mathbf{q}}_g$ ; using sample  $\hat{\mathbf{q}}_g$  instead of  $\bar{\mathbf{q}}_g$ ;  $\mathbf{z}_i$ ; fixed effects  $\mathbf{v}_g$ ; system of equations
- Empirics: externalities similar across goods;  $\alpha$  is big, about 0.5.

# Reference Point Utility

- micro:
- (perceived) needs in utility functions
  - jumping off from: Samuelson (1947), Gorman (1976), Pollak and Wales (1981), Blackorby and Donaldson (1994), and Donaldson and Pendakur (2006).
- reference points
  - reference point utility: the valuation of one's income depends on income of one's reference group.
    - Surveys by Kahneman 1992; Clark Frijters, and Shields 2008.
  - In our case,  $\bar{q}_g$  influence needs
    - Veblen effects - visible luxuries are status symbols; I get utility from relative status.
- utilities and equivalent-incomes
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- macro:  $\bar{x}_g$  might affect marginal utility, and savings

# What we do: Econometrics

- Individual outcomes  $y_i$  depending on group means  $\bar{y}_g$  are a form of social interaction model.
- Is similar to a spatial model, with a very sparse contiguity matrix where all individuals within each group are equidistant from each other.

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- Is similar to a spatial model, with a very sparse contiguity matrix where all individuals within each group are equidistant from each other.
- Reflection problem: Manski (1993, 2000). See also Brock and Durlauf (2001), and Blume, Brock, Durlauf, and Ioannides (2010).
  - endogenous effects, exogenous effects, and the correlated effects cannot in general be separately identified
  - we exploit nonlinearity and utility derived restrictions to overcome the reflection problem.
- Network info helps, e.g., Bramoullé, Djebbari, and Fortin (2009).
- We show identification with sparse network info: we observe only a fixed (and small) number of members of each group.

# Generic Model Definition

- To illustrate our new identification strategy, consider a simpler generic social interactions model first.
- $i$  indexes individuals (later, households). Each individual  $i$  is in a peer group  $g \in \{g = 1, \dots, G\}$ .
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- We assume  $n_g$  is fixed, does not grow with the sample size.
- Outcome  $y_i$  depends on regressor  $x_i$  and on  $\bar{y}_g = E(y_i \mid i \in g)$ .
- Later extend to vector of outcomes, vector of interactions, vector of regressors, and utility based functional forms.

## Generic Model Definition - continued

- Write the model as  $y_i = h(\theta \mid \bar{y}_g, x_i) + v_g + u_i$
- $v_g$  are group level random or fixed effects.
- $u_i$  are mean zero errors, independent all  $x$  in all groups.

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- We do not include  $\bar{x}_g$  as a regressor because our model of utility implies that it does not appear in our demand equations.
- If we included  $\bar{x}_g$  additively, it would be absorbed into  $v_g$ .

## Generic Model Definition - continued

- The specification of  $h(\theta | \bar{y}_g, x_i) + v_g + u_i$  we use is quadratic

$$y_i = (\bar{y}_g a + x_i b + c)^2 d + (\bar{y}_g a + x_i b + c) + v_g + u_i$$

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- Difficulties for estimation of  $\theta$ 
  - $v_g$  could be correlated with  $\bar{y}_g$  and hence with  $\hat{y}_g$ .
  - $n_g$  does not go to infinity, so if  $\hat{y}_g$  contains  $y_i$ , it is correlated with  $u_i$ .
  - $n_g$  fixed so  $\varepsilon_{gi}$  doesn't vanish, is potentially correlated with all regressors due to nonlinearity (which we use to avoid nonidentification from reflection). For example  $\varepsilon_{gi}$  contains  $(\bar{y}_g - \hat{y}_g) x_i$ .

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- We consider two different approaches - fixed and random effects.
  - Fixed effects has fewer assumptions, random effects provides more identifying information.

# Generic Fixed Effects Model

- To remove the fixed effect **difference** two people  $i$  and  $i'$  in group  $g$ :

$$y_i - y_{i'} = h(\theta \mid \bar{y}_g, x_i) - h(\theta \mid \bar{y}_g, x_{i'}) + u_i - u_{i'}$$

- This also differences out the quadratic term  $\bar{y}_g^2 a^2$  inside  $h$ .

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- This also differences out the quadratic term  $\bar{y}_g^2 a^2$  inside  $h$ .
- Define the leave-two-out group mean estimator

$$\hat{y}_{g,-ii'} = \left( \frac{1}{n_g - 2} \right) \sum_{l \in g, l \neq i, i'} y_l. \quad \text{Here } i \text{ and } i' \text{ are both in group } g$$

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- To deal with measurement error due to small fixed group size, plug in  $\hat{y}_{g,-ii'}$  for  $\bar{y}_g$  to get

$$y_i - y_{i'} = h(\theta \mid \hat{y}_{g,-ii'}, x_i) - h(\theta \mid \hat{y}_{g,-ii'}, x_{i'}) + u_i - u_{i'} + \varepsilon_{gi} - \varepsilon_{gi'}$$

- Theorem 1: With

$$h(\theta \mid \bar{y}_g, x_i) = (\bar{y}_g a + x_i b + c)^2 d + (\bar{y}_g a + x_i b + c) \quad \text{we can show}$$

$$E(u_i - u_{i'} + \varepsilon_{gi} - \varepsilon_{gi'} \mid x_i, x_{i'}) = 0$$

## Generic Fixed Effects Model — continued

- since  $E(u_i - u_{i'} + \varepsilon_{gi} - \varepsilon_{gi'} \mid x_i, x_{i'}) = 0$ , valid instruments include
  - $(x_i - x_{i'})$  and its square,
  - $\tilde{x}_g$  equal to average  $x$  in the group in other periods and its square.

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  - $\tilde{x}_g$  equal to average  $x$  in the group in other periods and its square.
- Let  $\mathbf{r}_{gii'}$  be a vector of functions of  $x_i, x_{i'}, \tilde{x}_g$  and other instruments  $\mathbf{r}_g$ .
- Use  $\mathbf{r}_{gii'}$  as instruments for GMM estimation, based on moments

$$E\{[y_i - y_{i'} - h(\theta \mid \hat{y}_{g,-ii'}, x_i) + h(\theta \mid \hat{y}_{g,-ii'}, x_{i'})] \mathbf{r}_{gii'}\} = 0$$

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- Theorem 1 shows that  $\theta$  is identified by these moments.
- Observations for the GMM are every pair of individuals  $i$  and  $i'$  in each group.
- Use clustered standard errors, each group is a cluster: by construction errors are correlated across observations within each group.

# Generic Random Effects Model

- Fixed effects loses a lot of information from differencing.
- Consider instead the random effects assumption:  $v_g \perp x_i$ , homoskedastic.

# Generic Random Effects Model

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- Consider instead the random effects assumption:  $v_g \perp x_i$ , homoskedastic.
- Rewrite the quadratic model as:

$$y_i = (\bar{y}_g a + x_i b + c) [(\bar{y}_g a + x_i b + c) d + 1] + v_g + u_i$$

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- $\bar{y}_g a$  times itself will not be differenced out, so must now cope with squared error that results from replacing  $\bar{y}_g$  with an estimate.
- Replace the *first*  $\bar{y}_g$  with  $\hat{y}_{g,-i}$  as before, and replace the *second*  $\bar{y}_g$  with  $y_{i'}$ .

# Generic Random Effects Model—continued

- This replacement adds an error  $\tilde{\varepsilon}_{gij'}$ . Model becomes

$$y_i = (\hat{y}_{g,-ii'} a + x_i b + c) [(y_i' a + x_i b + c) d + 1] + v_g + u_i + \tilde{\varepsilon}_{gij'}$$

- and, with  $v_0 = E(v_g) + da^2 \text{Var}(v_g)$ , we can show

$$E[y_i - (\hat{y}_{g,-ii'} a + x_i b + c) [(y_i' a + x_i b + c) d + 1] - v_0 \mid x_i] = 0$$

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- Since this applies for all  $i, i'$ , use observations comprised of every pair of individuals in a cluster.
- Now,  $x_i$  and  $\tilde{x}_g$  (but not  $x_{i'}$ ) are valid instruments.

# Generic Model—Formal Identification 1

- Allow a  $K$ – vector of covariates  $\mathbf{x}$
- **Assumption A1:** Each individual  $i$  in group  $g$  satisfies

$$y_i = (\bar{y}_g a + \mathbf{x}'_i \mathbf{b})^2 d + (\bar{y}_g a + \mathbf{x}'_i \mathbf{b}) + v_g + u_i$$

- Unobserved  $v_g$  are group level fixed effects.
- Unobserved  $u_i$  are independent across groups  $g$  and have  $E(u_i | \text{all } \mathbf{x}_{i'} \text{ having } i' \in g \text{ where } i \in g) = 0$ .
- The number of observed groups  $G \rightarrow \infty$ . For each observed group  $g$ , we observe a fixed sample of  $n_g \geq 3$  observations of  $y_i, \mathbf{x}_i$ .

- **Assumptions A2, A3:** Let  $\bar{\mathbf{x}}_g = E(\mathbf{x}_i \mid i \in g)$ ,  $\overline{\mathbf{x}\mathbf{x}'}_g = E(\mathbf{x}_i\mathbf{x}_i' \mid i \in g)$ . The coefficients  $a$ ,  $\mathbf{b}$ ,  $d$  are unknown constants satisfying  $d \neq 0$ ,  $\mathbf{b} \neq 0$ , and  $[1 - a(2\mathbf{b}'\bar{\mathbf{x}}_gd + 1)]^2 - 4a^2d[d\mathbf{b}'\overline{\mathbf{x}\mathbf{x}'}_g\mathbf{b} + \mathbf{b}'\bar{\mathbf{x}}_g + v_g] \geq 0$ . Individuals within each group agree on an equilibrium selection rule.
- Need  $d \neq 0$  to have nonlinearity, avoid the reflection problem.
- Need  $\mathbf{b} \neq 0$  else no exogenous covariates.
- The inequality ensures an equilibrium  $\bar{y}_g$  exists (coherence as in Tamer 2003).

- **Assumption A4:** Let  $\mathbf{r}_g$  be a vector (possibly empty) of observed group level instruments that are independent of each  $u_i$ . Assume  $E((\mathbf{x}_i - \bar{\mathbf{x}}_g) \mid i \in g, \bar{\mathbf{x}}_g, \overline{\mathbf{x}\mathbf{x}'}_g, \mathbf{v}_g, \mathbf{r}_g) = 0$ ,  $E((\mathbf{x}_i\mathbf{x}'_i - \overline{\mathbf{x}\mathbf{x}'}_g) \mid i \in g, \mathbf{r}_g) = 0$ , and that  $\mathbf{x}_i - \bar{\mathbf{x}}_g$  and  $\mathbf{x}_i\mathbf{x}'_i - \overline{\mathbf{x}\mathbf{x}'}_g$  are independent across individuals  $i$ .
- A4 is essentially instrument validity. A stronger sufficient condition is that  $\varepsilon_{ix} = \mathbf{x}_i - \bar{\mathbf{x}}_g$  are independent across individuals  $i$  and independent of group level variables  $\bar{\mathbf{x}}_g, \overline{\mathbf{x}\mathbf{x}'}_g, \mathbf{v}_g, \mathbf{r}_g$ . This would hold if each  $\mathbf{x}_i$  is a randomly drawn deviation  $\varepsilon_{ix}$  around  $\bar{\mathbf{x}}_g$ .

- **Theorem:** If Assumptions A1 to A4 hold then

$$E[y_i - y_{i'} - (2ad\hat{y}_{g,-ii'}\mathbf{b}'(\mathbf{x}_i - \mathbf{x}_{i'}) + d\mathbf{b}'(\mathbf{x}_i\mathbf{x}_i' - \mathbf{x}_{i'}\mathbf{x}_{i}')\mathbf{b} + \mathbf{b}'(\mathbf{x}_i - \mathbf{x}_{i'})) \\ | \mathbf{r}_g, \mathbf{x}_i, \mathbf{x}_{i'}] = 0$$

- A standard order and rank condition then ensures all parameters are identified from these moments and can be estimated by GMM.
- Proof consists of plugging  $\hat{y}_{g,-ii'}$  in for  $\bar{y}_g$ , and then verifying that the resulting measurement and model errors  $u_i - u_{i'} + \varepsilon_{gi} - \varepsilon_{gi'}$  are mean independent of  $\mathbf{r}_g, \mathbf{x}_i, \mathbf{x}_{i'}$ .
- Random effects are analogous.

# Well-Being Analysis

- Data set WVS: 2006 and 2014 India modules of the World Values Survey (WVS). 3236 observations.
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- Define groups by education of head, religion/caste, and state.
- Ordered Logit regressions of self-reported life-satisfaction (“how satisfied are you with your life”) on a 1 to 5 scale.
- Regress on imputed household expenditures  $x_i$  (in reals), demographics  $z_i$ , group average  $\hat{x}_g$  ( $\hat{x}_g$  in reals, matched from NSS data).

Table 3: Satisfaction on household and peer income

|                                   | OLS (SDs)           |                     |                   | Ordered logit       |                     |                   |
|-----------------------------------|---------------------|---------------------|-------------------|---------------------|---------------------|-------------------|
|                                   | (1)                 | (2)                 | (3)               | (4)                 | (5)                 | (6)               |
| Imputed expenditure               | 0.068***<br>(0.013) |                     |                   | 0.179***<br>(0.031) |                     |                   |
| Group expenditure                 | -0.100**<br>(0.049) |                     |                   | -0.203*<br>(0.115)  |                     |                   |
| Imputed expenditure, CPI deflated |                     | 0.131***<br>(0.025) | 0.141*<br>(0.079) |                     | 0.335***<br>(0.058) | 0.359*<br>(0.198) |
| Group expenditure, deflated       |                     | -0.190*<br>(0.107)  | -0.182<br>(0.114) |                     | -0.424*<br>(0.256)  | -0.407<br>(0.285) |
| Own X group expenditure           |                     |                     | -0.003<br>(0.018) |                     |                     | -0.006<br>(0.044) |
| Year FEs                          | Yes                 | Yes                 | Yes               | Yes                 | Yes                 | Yes               |
| Ratio                             | 1.47<br>(0.764)     | 1.45<br>(0.850)     | 1.29<br>(1.249)   | 1.13<br>(0.684)     | 1.27<br>(0.803)     | 1.13<br>(1.202)   |
| P(Own + group = 0)                | 0.528               | 0.588               | 0.799             | 0.848               | 0.734               | 0.908             |
| Dependent mean                    | 0.00                | 0.00                | 0.00              | 3.07                | 3.07                | 3.07              |
| Dependent SD                      | 1.00                | 1.00                | 1.00              | 1.22                | 1.22                | 1.22              |
| Observations                      | 3236                | 3236                | 3236              | 3236                | 3236                | 3236              |

Dependent variable as noted in column header, in SD. Subjective well being data from World Values Survey, imputations from NSS. Peer groups defined as intersection of education (below primary, primary or partial secondary, secondary+) and religion (Hindu and non-Hindu). All columns include controls for household size, age, sex, marital status and education. Standard errors in parentheses and clustered at the group level. \*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ .

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- $\bar{x}_g$  affects well-being like lower  $x_i$ ; roughly offsetting, like Luttmer.
- Interaction  $x_i\bar{x}$  insignificant, so additive model is okay

# Needs and AESE Equivalent-Incomes

- Notation reminder:  $i$  indexes households,  $g$  indexes groups (of households). overbars indicate true within-group means, hats indicate sample averages.  $\mathbf{q}$  is quantity vector,  $\mathbf{p}$  is price vector,  $x$  is budget,  $\mathbf{z}$  is characteristics.

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- The *equivalent-income function*  $X_i(\mathbf{p}, x)$  is the  $x_i$  needed to give  $i$  the same utility as a reference consumer  $i = 0$  having a budget  $x$ .
  - drop  $\mathbf{z}$  for now—it is absorbed into  $i$ .
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- $X_i(\mathbf{p}, x)$  is an interpersonally-comparable money metric utility function. It could be an argument of a social welfare function.
- Define *Absolute Equivalence Scale Exactness* (AESE) as  $X_i(\mathbf{p}, x) = x - \tilde{F}_i(\mathbf{p})$  for some  $\tilde{F}_i$ .
- Theorem (Blackorby and Donaldson 1994) AESE holds iff  $V_i(\mathbf{p}, x_i) = V(\mathbf{p}, x_i - F_i(\mathbf{p}))$  where  $\tilde{F}_i(\mathbf{p}) = F_i(\mathbf{p}) - F_0(\mathbf{p})$ .
- $F_i(\mathbf{p})$  is the cost of satisfying the **perceived needs** of consumer  $i$ .
- Our model (and Luttmer's) fits into AESE.

# Implications of AESE on Preferences

- By Roys identity, AESE implies demand functions  $\mathbf{q}_i = \mathbf{h}_i(\mathbf{p}, x_i)$ :

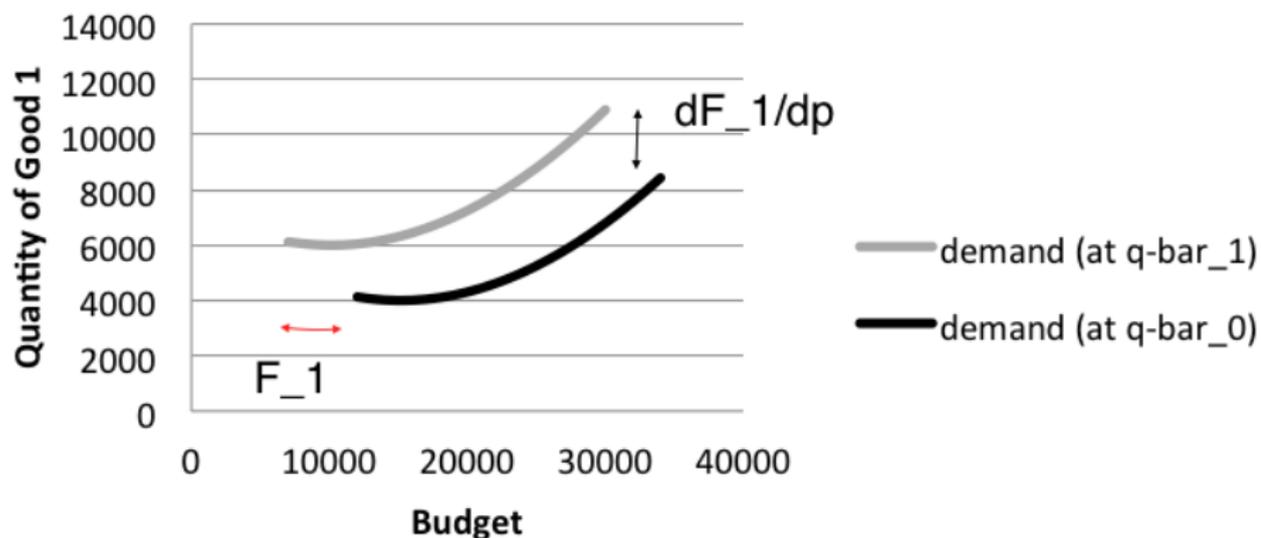
$$\mathbf{h}_i(\mathbf{p}, x_i) = \mathbf{h}(\mathbf{p}, x_i - \tilde{F}_i(\mathbf{p})) + \frac{\partial \tilde{F}_i(\mathbf{p})}{\partial \mathbf{p}},$$

and, if  $\tilde{F}_i(\mathbf{p}) = F_i = \mathbf{p}'\mathbf{f}_i$

$$\mathbf{h}_i(\mathbf{p}, x_i) = \mathbf{h}(\mathbf{p}, x_i - F_i) + \mathbf{f}_i.$$

- This is shape-invariance in quantity demands as in Pendakur (2005).
  - It is similar to budget share shape invariance as in Pendakur (1999), Lewbel (2010), and Blundell, Chen and Kristensen (2007).
- Shape invariance is empirically testable by comparing differences in  $\mathbf{h}_i(\mathbf{p}, x)$  across consumers.
- Shape invariance exhausts the testable implications of AESE.

## Shape-Invariance, where $q\text{-bar}_1$ is higher than $q\text{-bar}_0$



# More Implications of AESE

- AESE has other, untestable (cardinal utility), implications.
- All shape invariant utility functions can be written as  $V_i(\mathbf{p}, x_i) = H_i [V^0(\mathbf{p}, x_i - F_i(\mathbf{p}))]$ .
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- The untestable restriction is that  $H_i$  is the identity function.
- Every choice of  $H_i$  yields a new equivalent-income function.
- However, Blackorby and Donaldson (1994) show that, given AESE, differences in needs  $\tilde{F}_i(\mathbf{p}) = F_i(\mathbf{p}) - F_0(\mathbf{p})$  are identified from behaviour.
- Welfare calculations only require differences  $\tilde{F}_i(\mathbf{p})$ .

# Our Demand Model

- We use (AESE) demands with needs  $\tilde{F}_i(\mathbf{p}) = F_i = \mathbf{p}'\mathbf{f}_i$   
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- So,

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- We are interested in  $\mathbf{A}$ ; it may be scalar where  $\mathbf{A} = \alpha\mathbf{I}$ .

# Empirical Application: NSS Data

- Household consumption and demographics from rounds 59 to 62 of the National Sample Survey (NSS) of India (2002/3 to 2005/6).
- Rural Hindu non-Dalit households head over 20 only. Yields 56,516 households.
- Groups: education (3 levels) by district (575 across 33 states).
  - Get 1111 groups with at least 10 observations in at least 1 period.
  - 2354 group-periods with 2,055,776 within-group pairs.

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- Also consider further dividing luxuries and necessities into visible (to others) vs invisible as in Roth (2014).

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- 76 nondurable consumption categories, aggregate into luxuries and necessities (defined by budget shares increasing or decreasing in log total expenditures). About 1/4 of categories are luxuries.
- Also consider further dividing luxuries and necessities into visible (to others) vs invisible as in Roth (2014).
- Deaton-styled local-average unit-value commodity prices  $\mathbf{p}$  vary by time and state.
- Demographics  $\mathbf{z}$  include household size, household head age, marital status, land-holdings (in hectares) and ration card holder status.

Table 5: Summary Statistics for Indian NSS Data  
2354 group-rounds

|                   | Observations (N=56,516) |         |      |      |
|-------------------|-------------------------|---------|------|------|
|                   | mean                    | std dev | min  | max  |
| $x_i$             | 1.12                    | 0.66    | 0.10 | 8.75 |
| $q_i$ luxuries    | 0.31                    | 0.37    | 0.00 | 7.96 |
| $q_i$ necessities | 0.83                    | 0.40    | 0.03 | 4.32 |
| $p$ luxuries      | 0.98                    | 0.08    | 0.81 | 1.29 |
| $p$ necessities   | 0.99                    | 0.07    | 0.86 | 1.34 |
| Educ med          | 0.48                    | 0.50    | 0.00 | 1.00 |
| Educ high         | 0.06                    | 0.24    | 0.00 | 1.00 |
| (hhsz-1)/10       | 0.40                    | 0.22    | 0.00 | 1.10 |
| headage/120       | 0.40                    | 0.11    | 0.17 | 0.94 |
| married           | 0.87                    | 0.34    | 0.00 | 1.00 |
| ln(land+1)        | 0.60                    | 0.58    | 0.00 | 2.30 |
| ration card       | 0.23                    | 0.42    | 0.00 | 1.00 |

# Fixed Effects Estimates

|                 |                        | Fixed Effects                    |         |                       |         |
|-----------------|------------------------|----------------------------------|---------|-----------------------|---------|
|                 | Needs Response         | $\mathbf{A} = \alpha \mathbf{I}$ |         | $\mathbf{A}$ Diagonal |         |
|                 |                        | est                              | std err | est                   | std err |
| luxuries        | own                    | 0.50                             | 0.11    | -2.63                 | 0.40    |
| necessities     | own                    | 0.50                             | 0.11    | 2.99                  | 0.28    |
| test A same     | $\chi^2$ stat, [p-val] |                                  |         | 80                    | [0.00]  |
| Hausman test RE | $z$ stat, [p-val]      | -0.31                            | [0.76]  | -7.8                  | [0.00]  |
|                 |                        |                                  |         | 8.8                   | [0.00]  |

Std errors are big with different A elements.

A is identified off  $x_i \hat{\mathbf{q}}$  interactions.

Since, the elements of  $\hat{\mathbf{q}}$  are correlated with each other, it is hard to pick up 2 parameters

# Random Effects Estimates

Table 5: 2 good system, Random Effects

|                                       |       | Random Effects                   |         |                       |         |                   |         |
|---------------------------------------|-------|----------------------------------|---------|-----------------------|---------|-------------------|---------|
|                                       |       | $\mathbf{A} = \alpha \mathbf{I}$ |         | $\mathbf{A}$ Diagonal |         | $\mathbf{A}$ Full |         |
|                                       |       | est                              | std err | est                   | std err | est               | std err |
| luxuries                              | own   | 0.55                             | 0.02    | 0.46                  | 0.02    | 0.20              | 0.09    |
| necessities                           | own   | 0.55                             | 0.02    | 0.57                  | 0.02    | 1.09              | 0.10    |
| luxuries                              | cross |                                  |         |                       |         | 0.42              | 0.08    |
| necessities                           | cross |                                  |         |                       |         | -0.33             | 0.11    |
| test $\mathbf{A} = \alpha \mathbf{I}$ |       |                                  |         | 43                    | [0.00]  |                   |         |

- RE diagonal estimates don't show much difference across goods.
- RE Full estimates (with crosses) are difficult to identify—interaction terms identify cross effects.

# Visible and Invisible

Table 6: 4 Goods

|                                       |       | Fixed Effects                        |                | Random Effects                       |                |                       |                |
|---------------------------------------|-------|--------------------------------------|----------------|--------------------------------------|----------------|-----------------------|----------------|
|                                       |       | FE: $\mathbf{A} = \alpha \mathbf{I}$ |                | RE: $\mathbf{A} = \alpha \mathbf{I}$ |                | RE: $\mathbf{A}$ Diag |                |
|                                       |       | est                                  | <i>std err</i> | est                                  | <i>std err</i> | est                   | <i>std err</i> |
| lux                                   | vis   | 0.71                                 | <i>0.05</i>    | 0.65                                 | <i>0.01</i>    | 0.54                  | 0.01           |
|                                       | invis | 0.71                                 | <i>0.05</i>    | 0.65                                 | <i>0.01</i>    | 0.62                  | 0.01           |
| necc                                  | vis   | 0.71                                 | <i>0.05</i>    | 0.65                                 | <i>0.01</i>    | 0.76                  | 0.01           |
|                                       | invis | 0.71                                 | <i>0.05</i>    | 0.65                                 | <i>0.01</i>    | 0.66                  | 0.01           |
| test RE                               |       | 1.26                                 | <i>[0.21]</i>  |                                      |                |                       |                |
| test $\mathbf{A} = \alpha \mathbf{I}$ |       |                                      |                |                                      |                | 658                   | <i>[0.00]</i>  |

# Bigger Demand Systems

- Like Di Giorgio, Frederiksen and Pistaferri (2016), visible luxuries don't have larger peer effects than invisible luxuries or necessities.
- However, visible necessities do have larger peer effects than invisible necessities.
- Not the typical Veblen type conspicuous consumption story.
- Changing the number of goods does not change the spirit of the estimates: peer effects are still similar across goods, and large.
- Using more goods yields substantial benefits in terms of precision, because each element of  $\mathbf{A}$  shows up in each equation.

# Population Subgroups

Table 7: Fixed Effects,  $\mathbf{A} = \alpha \mathbf{I}$ , Subgroups

|                   | Religion<br>separate regs |                | Education<br>Hindus only |                | Expenditure<br>separate regs |                |
|-------------------|---------------------------|----------------|--------------------------|----------------|------------------------------|----------------|
|                   | est                       | <i>std err</i> | est                      | <i>std err</i> | est                          | <i>std err</i> |
| Hindu, non-SC/ST  | 0.50                      | <i>0.11</i>    |                          |                |                              |                |
| SC/ST             | 0.13                      | <i>0.18</i>    |                          |                |                              |                |
| non-Hindu         | -0.06                     | <i>0.23</i>    |                          |                |                              |                |
| Illiterate/None   |                           |                | 0.08                     | <i>0.15</i>    |                              |                |
| Pri. or some Sec. |                           |                | 0.56                     | <i>0.12</i>    |                              |                |
| Sec. or more      |                           |                | 0.37                     | <i>0.22</i>    |                              |                |
| below med. exp.   |                           |                |                          |                | 0.26                         | <i>0.05</i>    |
| above med. exp.   |                           |                |                          |                | 0.59                         | <i>0.17</i>    |

# Poorer Subgroups Have Smaller $\alpha$

- Hindu has much bigger value of  $\alpha$ .
- Not the same as in the well-being analysis.
- Primary education (middle group) has the biggest value of  $\alpha$ .
- The same as in the well-being analysis.
- SC/ST have lower  $\alpha$
- uneducated/illiterate have lower  $\alpha$
- below median expenditure households have lower  $\alpha$ .

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- In our model, there is an additional public benefit channel: public goods raise money metrics more than do transfers.
- if jealousy or envy are the underlying cause:
  - Public goods, e.g., clean water, public sanitation, better air quality, or better schools.
  - public goods—all people consume the same quantity—cause no envy.
  - so, are better in terms of money metric than private goods

# Public Goods Are Half a Free Lunch

- The National Food Security Act (2013)
  - subsidized cereals to 75 per cent of households at  $1/3$  market price,
  - (projected) costs roughly 1.35% of GDP.
  - increases consumption, with externality on to needs.
  - up to 5 kg/month/person at Rs3/kg. Rice was Rs15/kg in 2016.
  - Public cost: Rs12/kg, so Rs60/month/person.

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- suppose households increase their necessities spending by Rs60/month/person.
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- NFSA program targets 1 billion people, yielding potential annual money-metric welfare gains (of switching from rice subsidies to a public goods program) of Rs336 billion to Rs408 billion.
  - smaller welfare gains if consumers increase luxury spending instead.
  - larger welfare gains if rich taxpayers have bigger consumption externalities.

# Summary: Econometrics

- identification and GMM estimation of peer effects in a generic quadratic model,
  - in data where we observe a fixed and small number of members of each group
  - allows for fixed or random effects
- a utility and consumer demand model where ones perceived needs for each commodity depends in part on the average consumption of one's peers.
  - demand model is extension of our generic quadratic peer effects model, and so identification and GMM estimation are the same
- model specifies the equivalent-income function, and so can be used for utility and social welfare analysis

# Summary: Findings

- Peer effects in consumption are large.
  - If peer-average spending rises by Rs1000, household needs rise by roughly Rs500.
- Increased needs affect utilities exactly as do decreased budgets. So, some of the gains to income growth may be lost.
  - 50 per cent of income growth may be eaten away by increased needs.
- Public goods may be a “half-price” lunch.
- Income taxes are less costly in terms of welfare than they seem - no longer need to spend as much for the same level of welfare when neighbors are taxed.
  - If peer effects were larger for luxuries, then progressive taxes would be smart, even if, absent peer effects, the marginal utility of money was the same for rich and poor.
  - But, they're not.