# Effects of Elderly Care for an Aging Population on the Labor Market 

Jessie Wang<br>Furman University<br>January 2018

## Motivation

- Aging Population: demand for elderly care increases
- Suggested by literature: negatively affect caretakers.
- What about others?
- Wang (2017) finds that females are heterogeneous in their responses to parental health shocks
- How this will shape the labor markets?
- Will female labor force participation declines due to care-taking responsibilities?


## The Model

Differences from other models: no altruistic or other incentives

Two-period OLG:

- The young generation: work, leisure, care and save
- The old generation: consume saving, require care (with positive probability)
- Care requirements are in binding constraints of the young


## The Household Problem

The young's problem:
$\max \ln \left(c_{t}\right)+\nu \ln \left(I_{f}\right)+\beta E\left(u_{t+1}\right)$
s.t. $h_{f}+n_{f}+l_{f}=3$

$$
\begin{aligned}
& {\left[h_{f}^{\theta}+\alpha h_{s}^{\theta}\right]^{1 / \theta} \geq H(\eta), 0<\theta<1} \\
& w_{m} n_{m}+w_{f} n_{f}=c_{t}+p_{x} h_{s}+M(\eta)+M_{n}+s_{t}
\end{aligned}
$$

## Care Time Constraint

$$
\left[h_{f}^{\theta}+\alpha h_{s}^{\theta}\right]^{1 / \theta} \geq H(\eta), 0<\theta<1
$$

- Depend on parents' health condition, $\eta$
- $h_{f}$ is care time supplied by the household female
- $h_{s}$ is market care purchased
- $\alpha$ is an efficiency parameter
- Elasticity of Substitution, $1 /(1-\theta)$


## Budget Constraint

$$
w_{m} n_{m}+w_{f} n_{f}=c_{t}+p_{x} h_{s}+M(\eta)+M_{n}+s_{t}
$$

- $p_{x}$ is price per efficiency unit of care
- $M(\eta)$ is the medical expense requirement
- $M_{n}$ is a fixed monetary cost if the female chooses to work


## Abilities

Two production sectors: Goods (c) and Care (x)
Two types of abilities:

- Efficiency units of labor in goods production, $e_{c}$
- Efficiency units of labor in care production, $e_{x}$

Assumption: males work full-time in the goods sector and do not provide care.

Note: These abilities only apply to the formal production sectors.

## The Model Population

Households are characterized by three independent draws:

- Female efficiency unit of labor in goods, $e_{f, c}$
- Female efficiency unit of labor in care, $e_{f, x}$
- Intra-household ability ratio, $r_{f m}$

Male efficiency unit of labor in goods is calculated as:

$$
e_{m, c}=r_{f m} e_{f, c}
$$

## The Production Sectors

Production technologies:
Consumption goods sector: $\quad Y_{c}=A_{c} N_{c}$
Care sector:
$Y_{x}=N_{x}$

- Labor is the only input
- $A_{c}$ - the total factor productivity in the goods market
- $N_{c}$ and $N_{x}$ are measured in efficiency units of labor


## Calibration

Data Sources:

- Health and Retirement Survey (1992-2012)
- Shock probability: 10\%
- American Community Surveys (2007)
- Ability distributions
- Female labor force participation rate
- Care sector size
- Care worker wage
- Magnitude of female labor supply responses


## Summary

$\beta$ : discount rate ..... 0.96
Shock probability ..... 10\%
Mean $\log (f e m a l e ~ g o o d s ~ a b i l i t y) ~$ ..... 1
Std dev $\log ($ female goods ability) ..... 0.29
Mean $\log$ (male/female ability ratio) ..... 0.29
Std dev $\log$ (male/female ability ratio) ..... 0.85
Mean $\log$ (female care ability) ..... 0
Std dev $\log$ (female care ability) ..... 0.2
$A_{c}$ : goods sector TFP ..... 1
$\theta$ : Elasticity parameter ..... 0.75
$\nu$ : female leisure utility weight ..... 2.2
$\alpha$ : market care effectiveness ..... 18
$M(\eta)$ : Medical expense requirement ..... 0.05
$H_{\eta}$ : Care time requirement ..... 1.5
$\bar{M}$ : fixed cost to work ..... 0.15

## Matching the Moments

| Moments | Model | Data |
| :--- | :--- | :--- |
| Female labor force part. rate | $64.17 \%$ | $64.42 \%$ |
| Care/Goods worker wage ratio | 0.563 | 0.56 |
| Care sector size | $3.34 \%$ | $3.32 \%$ |
| High-wage shock response | $4.07 \%$ | $7.68 \%(3.83 \%, 11.53 \%)$ |
| Low-wage shock response | $1.19 \%$ | $6.24 \%(-2.22 \%, 14.73 \%)$ |

## In an Aging Population

What are the implications for an aging population?

From census predictions, by 2060, elderly population/working-age population will increase by $115 \%$ :

- Number of households with aged parents: shock probability
- Care intensity when parents need care: $H(\eta)$ and $M(\eta)$


## Number of Children Born by Age Group Age of Mothers in 2014



## A Quantitative Experiment

## Current Experiment Changes (in \%)

| Parameters |  |  |  |
| :--- | :--- | :--- | :--- |
| Shock Probability | 0.1 | 0.143 | $+43 \%$ |
| $H(\eta):$ Care time | 1.5 | 2.25 | $+50 \%$ |
| $M(\eta):$ Medical expense | 0.05 | 0.075 | $+50 \%$ |
|  |  |  |  |
| Moments |  |  |  |
| Female labor force part. rate | $64.17 \%$ | $65.28 \%$ | $+1.73 \%$ |
| Care/Goods wage ratio | 0.56 | 0.49 | $-12.5 \%$ |
| Care sector size | $3.32 \%$ | $5.19 \%$ | $+56.3 \%$ |
| High-wage shock response | $4.07 \%$ | $5.06 \%$ |  |
| Low-wage shock response | $1.14 \%$ | $2.21 \%$ |  |

## Conclusion

- High-wage and low-wage females have heterogeneous responses when parents age and require care
- Female labor supply increases in an aging population
- Specific policy is necessary to target different households

Thank You!

