# Earnings Inequality and Mobility Trends in the United States: Nationally Representative Estimates from Longitudinally Linked Employer-Employee Data 

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#### Abstract

Decomposing the year-to-year changes in the earnings distribution from 2004 to 2013, we analyze the role of the employer in explaining earnings inequality in the United States. Movements between the bottom, middle, and top involve 20.5 million workers each year. Another 19.9 million move between employment and nonemployment. There are large gains from working at a top-paying firm for all skill types. Working for a high-paying firm produces benefits today, through higher earnings, that persist through an increase in the probability of upward mobility. High-paying firms facilitate moving workers to the top of the distribution and keeping them there.


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## I. Introduction

A growing body of work studies the rise in earnings inequality in the United States, ${ }^{1}$ with many studies focusing on the role of the employer in explaining these trends. ${ }^{2}$ Virtually all of these papers use administrative data to analyze employer effects on earnings inequality. Information from administrative sources, unlike data collected in household surveys, is found or organic data. ${ }^{3}$ That is, these data come from a convenient frame neither designed nor ensured to be representative of the population under study. Using found data to study features of a population-in particular features that evolve over time, like earnings inequality-requires additional effort to determine what types of individuals are included in the found data and how those who are excluded from the analysis affect the results.

In this paper, we analyze the importance of firms in explaining the evolution of earnings inequality in the United States using administrative data from the Longitudinal Employer-Household Dynamics (LEHD) infrastructure files of the US Census Bureau. We conduct two important analyses before turning to earnings inequality. First, unlike other studies of earnings inequality that use administrative data, we supplement the LEHD frame with data from the Social Security Administration (SSA) to create a consistent frame of workers over time. Specifically, we identify records in the administrative LEHD data that are either (a) associated with an invalid Social Security number (SSN) or ( $b$ ) used in a manner indicating possibly fraudulent labor market activity associated with a valid SSN. We remove both of these types
sarily represent the views of the US Census Bureau or other sponsors. All results have been reviewed to ensure that no confidential information is disclosed. This research uses data from the US Census Bureau's Longitudinal Employer-Household Dynamics Program, which was partially supported by NSF grants SES-9978093, SES-0339191, and ITR-0427889; National Institute on Aging grant AG018854; and grants from the Alfred P. Sloan Foundation. An archive of the code used to prepare analysis samples and conduct estimation along with the released results is available directly from https://doi.org/10.5281/zenodo.545680. Access to the underlying confidential data is controlled by the Federal Statistical Research Data Center network as described at https://www.census.gov/ces/dataproducts/restricted_data .html. Contact the corresponding author, John M. Abowd, at john.maron.abowd @census.gov. Contact Kevin L. McKinney and Nellie L. Zhao at kevin.l.mckinney @census.gov and nlz6@cornell.edu, respectively.
${ }^{1}$ See Katz and Autor (1999) for a summary of the extensive body of work that analyzed the rise in US wage inequality from the late 1970s to the mid-1990s and the forces behind this change in the wage structure.
${ }^{2}$ In particular, see Card, Heining, and Kline (2013) and Song et al. (2015). Aside from the increase in firm-specific wage premiums as a source of earnings inequality, other analyses have focused on skill-biased technological change (Acemoglu and Autor 2011) and the rise in the returns to education (Autor 2014).
${ }^{3}$ The term "found data" is commonly used in the data science literature, but the first formal use is Pato and Millett (2010, 72). Former US Census Bureau Director Robert Groves coined the term "organic data" (Groves 2010).
of records from our analysis and document the consequences. Second, we systematically compare the cross-sectional estimates of earnings inequality in our administrative data to estimates based on conventional household surveys and document the differences. Then we link the administrative and household survey data and use the linked data to understand where important features of the earnings distribution diverge.

By converting the found LEHD administrative data frame on workers to a designed frame, we can produce reliable estimates of features of the worker population. Conversion to a designed frame matters because trends in inequality differ between the designed frame and the original found frame. While our designed frame shows a widening of the earnings distribution after 2000 that is consistent with findings from other data sources, the found frame does not. Instead, the found frame shows no growth in earnings inequality since $2000 .{ }^{4}$ We show that the workers excluded from the found frame to create the designed frame tend to be individuals with very low earnings. In general, it is the bottom of the earnings distribution that is most affected by different frame-selection criteria.

Using our designed worker frame, we analyze how the earnings distribution has changed over time. We include inactive workers in our analysis, defined as individuals who are eligible to work but report no positive earnings. While most studies of earnings inequality limit the analysis to employed individuals, we highlight the importance of accounting for the mass of nonemployed workers when analyzing the patterns in earnings inequality. ${ }^{5}$ We show that by excluding these inactive workers in the analysis of earnings inequality, traditional measures of inequality like the Gini coefficient actually show a decline in earnings inequality during the Great Recession as workers, mostly from the bottom $80 \%$ of the earnings distribution, moved into nonemployment. ${ }^{6}$ While we do not receive a direct report of the labor force participation

[^1]status of these inactive workers from the administrative records, about $30 \%$ of them have reported positive earnings within the last 4 years, indicating that many have had some recent attachment to the labor market.

With both active and inactive workers in our analysis sample, we decompose the year-to-year changes in the earnings distribution into flows of workers across five employment outcomes from 2004 to 2013: (i) ineligibility, (ii) nonemployment, (iii) employment with annual earnings in the bottom $20 \%$ of the earnings distribution, (iv) employment in the middle $60 \%$, and (v) employment in the top $20 \%$. From this decomposition we find that mobility, both upward and downward, generally occurs between neighboring parts of the inactivity/earnings distribution. Specifically, inactive workers are most likely to transition into employment at the bottom of the earnings distribution, and rarely do employed workers jump from the bottom of the earnings distribution to the top. Furthermore, worker flows explain almost all of the changes in the earnings distribution in the last decade, with the average real earnings of workers in the bottom, middle, and top of the earnings distribution remaining fairly constant.

The Great Recession had a very large impact on these flows, with more than 9 million workers moving into nonemployment and almost 4 million workers falling from the middle of the earnings distribution to the bottom. While gross outflows from inactivity increased during the recovery, the flows have not been large enough to noticeably reduce the large pool of inactive workers accumulated during the early years of the Great Recession. Furthermore, overall mobility declined, with workers more likely to remain in their current employment state.

To understand the role of the firm in moving workers to the various parts of the earnings distribution, we decompose the above flows by worker and firm types. Specifically, we estimate the statistical model developed in Abowd, Kramarz, and Margolis (1999)—hereafter, AKM-to decompose annual earnings into firm and nonfirm components. Then, we characterize the firm component by its position in the overall distribution of firm components. For the person side of the analysis, we consider only the AKM worker effect and the estimated effect of the skill-related regressors. We label this component the skill type. Using the firm-type/skill-type dichotomy, we classify workers by their skill-type location in the earnings distribution and by their employer's location in the firm-component distribution. We examine the mobility patterns and earnings changes for different skill types of workers employed at different pay types of firms. We find that while the difference between working at a bottom- or middle-paying firm is relatively
cal variation in earnings inequality may also be connected to long-run trends in inequality. More recently, Piketty and Saez (2013) focus on the effect that business cycles have on the top of the income distribution, where transitions into unemployment are less of an issue.
small, the gains from working at a top-paying firm are large. In particular, workers benefit from working at a top-paying firm in two ways. First, observationally equivalent workers employed at a top-paying firm earn more than similar workers employed at bottom- and middle-paying firms. Second, workers at top-paying firms experience a higher probability of moving up the earnings distribution in the following year. Thus, top-paying firms are associated with increases in both the probability of upward mobility for a worker and the probability of remaining at the top of the earnings distribution even after controlling for the skill type of the worker.

## A. Related Literature

This paper makes two contributions to the literature on earnings inequality. First, we document the trends in earnings inequality using administrative data corrected using a consistent frame. Second, we analyze the sources of earnings inequality, with a particular emphasis on understanding the role of firms.

## Trends in Earnings Inequality

A large body of work documents the trends in inequality and tries to identify the sources of these changes. Many of the early studies analyzed the public-use micro data from the Current Population Survey (CPS). These studies documented a dramatic rise in wage rate and earnings inequality that started in the late 1970s and continued until the mid-1990s. ${ }^{7}$ This widening of the earnings distribution, while still present, has slowed since the mid-1990s. Much of the focus of this literature has shifted toward understanding the polarization of the wage rate distribution. ${ }^{8}$ Piketty and Saez (2003) directed the attention of researchers to analyzing the change in the share of income received by the top $1 \%$.

More recent studies also use administrative data to study earnings inequality. Unlike data collected from household surveys, administrative earnings data are generally free from measurement error and top coding (Abowd and Stinson 2013) but often lack direct information on labor supply, which makes the distinction between earnings and wage rate analyses salient. In the United States, given the absence of information on hours worked on most administrative records, the focus has shifted from wage rates to earnings or income. ${ }^{9}$ Kopczuk, Saez, and Song (2010) use micro data from the

[^2]SSA with information on taxable social security earnings to analyze the evolution of earnings inequality and mobility from 1937 to 2004. ${ }^{10}$ They find that earnings inequality over this period is $U$ shaped, decreasing until about 1953 and then increasing thereafter. ${ }^{11}$ Finally, Spletzer (2014) analyzes the trends in earnings inequality in the LEHD data. The trend in earnings inequality depends on the workers included in the sample for analysis. Specifically, he shows that quarterly earnings inequality has been increasing among workers who are very attached to the labor market. ${ }^{12}$ However, annual earnings inequality has not changed since around 2000, when Spletzer (2014) includes all workers aged 15 and older in his analysis sample, a result consistent with our findings when we use the data on all available jobs but inconsistent with our findings when we correct the estimation frame to exclude job records associated with what we call ineligible workers.

With the availability of all of these data sources for studying earnings inequality, Spletzer (2014) also analyzes how the patterns in inequality vary across data sources. While he conducts detailed comparison across several sources, we focus on the comparison between CPS's Annual Social and Economic Supplement (CPS-ASEC) and the LEHD data. ${ }^{13}$ In particular, he compares the evolution of the ratio of the 90th to the 10th percentile (90/ 10 ratio) in the CPS-ASEC and LEHD. When comparing these two sources, Spletzer documents different patterns in the $90 / 10$ ratio across the two that are very similar to our findings. In particular, the $90 / 10$ ratio in the CPSASEC has been increasing over the past 15 years, while the $90 / 10$ ratio in LEHD has remained relatively flat. While Spletzer (2014) identifies that it is differences in the evolution of the bottom half of the earnings distribution causing this discrepancy, he does not further analyze the differences in the
to decompose the growth in earnings inequality in Canada into its permanent and transitory components. They find that both of these components are important.
${ }^{10}$ Kopczuk et al. (2010) use several data sources from the SSA for their analysis. See Sec. II.B of their paper for the precise details.
${ }^{11}$ Guvenenetal, Ozkan, and Song (2014) also use micro data from the SSA; however, their earnings measure comes from W-2 forms (box 1) submitted directly by the employers. They focus on earnings risk changes during recessions. In their results, the trend in earnings inequality, which can be computed from their reported earnings percentiles, shows a small decline in earnings inequality during the 1990s until about 2000. Since 2000, earnings inequality has been on the rise. See table A3 of their app. A for the percentiles of the earnings distribution.
${ }^{12}$ To proxy for full-time workers, Spletzer (2014) includes only full-quarter workers: individuals with three consecutive quarters of positive earnings, for whom the interior quarter is studied as a time series.
${ }^{13}$ Spletzer (2014) also compares LEHD data to the data from the outgoing rotation group contained in the CPS basic monthly files and the IRS data used in Saez (2015).
sample of workers covered by the CPS-ASEC (a designed frame) and those covered by LEHD (a found frame), as we do. ${ }^{14}$

## The Role of Firms in Earnings Inequality

To evaluate the role of firms in the rise in inequality, many papers estimate a variation of the statistical model presented in Abowd et al. (1999). ${ }^{15}$ The data requirements that allow for the identification of separate worker and firm fixed effects-longitudinal links in both dimensions with sufficient network connectivity -almost always restrict such studies to administrative data. Card et al. (2013) applied this statistical technique to administrative data from Germany. Their analysis focused on full-time, full-year male employees. Their estimates suggest that, for this group of workers, the rise in German wage rate inequality was in part due to the increase in the dispersion in wage premiums paid by firms. Song et al. (2015) take a nonparametric approach to measurement of the firm's contribution to the rise in earnings inequality. Using SSA earnings data from the W-2 tax information forms from 1978 to 2012, they decompose the rise in earnings inequality into the part attributed to rising dispersion between firms in the average earnings they pay their employees and the part attributed to rising earnings dispersion among workers within a firm. They find that virtually all of the rise in earnings inequality is accounted for by an increase in the dispersion in the average earnings paid by firms. In their data, earnings differences among workers at the same firm have remained fairly constant over this period.

The remainder of the paper is organized as follows. Section II discusses the unemployment insurance (UI)-based individual- and job-level data we

[^3]use in our analysis as well as the creation of our all-workers and eligibleworkers frames. Section III presents and compares inequality trends in found versus designed data. This section also briefly discusses the results of comparing our analysis frames to data from the CPS and the American Community Survey (ACS). Section IV analyzes the evolution of the earnings distribution over time and presents a worker flow decomposition of the year-to-year change in the earnings distribution. Section V analyzes the importance of firms in understanding these changes in the earnings distribution. Section VI concludes.

## II. Data Sources and Methods

The empirical work in this paper uses three different sources of earnings information. The primary data source is the LEHD infrastructure files, developed and maintained by the US Census Bureau. ${ }^{16}$ We also use two household surveys: the CPS and the ACS. From these three data sources, we create two annual person-level earnings files covering the period 1990-2013. We construct the first file using the LEHD data and the second file using repeated cross-sectional CPS and ACS micro data. The replication archive for this paper is available at McKinney, Abowd, and Zhao (2017).

In the LEHD data infrastructure, a "job" is the statutory employment of a worker by a statutory employer as defined by the UI system in a given state. Mandated reporting of UI-covered wage and salary payments between one statutory employer and one statutory employee is governed by the state's UI system. Reporting covers private employers and state and local government. There are no self-employment earnings unless the proprietor drew a salary, which is indistinguishable from other employees in this case.

The Office of Personnel Management (OPM) supplied federal jobs data, included from 2000Q1 forward. The OPM data were edited as part of the LEHD infrastructure processing to produce records containing quarterly earnings reports comparable to those reported directly in the UI wage and salary payments. As part of this processing, pseudo-UI account numbers were created using the observed combinations of duty station state and agency/ subelement. ${ }^{17}$ The result is a set of state-level employer identifiers conceptually similar to those found on the UI data for private firms.

Due to national security regulations, which suppress certain jobs from the ones released by OPM to the public and other agencies, the coverage of the OPM extract varies by agency. Undercoverage is particularly severe for the Department of Defense (including the Air Force, Army, and Navy), the Department of Justice, the Department of State, and the Department of the Treasury. Although the federal jobs data are typically not included as

[^4]part of the state-based UI system, going forward in this paper, when we say "UI-covered" employment, we mean "statutory employment" as defined by the UI system or a statutory federal employee.

## B. Date Regimes

States and the federal government joined the partnership that supplies input data to the LEHD program at different dates. When a state or the federal government joined, the data custodians were asked to produce historical data for as many quarters in the past, back to 1990 Q1, as could be reasonably recovered from their information storage systems. As a result, the date that a data-supplying entity joined the partnership is not the same as the first quarter in which that entity's data appear in the system. The start date for any state or the federal government depends primarily on the amount of historical data the state or federal government could recover at the time it joined. This potential ignorability (in the sense of Rubin 1987 or Imbens and Rubin 2015) of the start data for a segment of the LEHD data is the basis for our methods of constructing nationally representative estimates back to the early 1990 s. ${ }^{18}$

To understand how state entrance into the LEHD program affects the trends in earnings inequality, we analyze four regimes that correspond to different epochs of data availability:

- regime 1: 1990-2013 (19\% of 2012Q1 Quarterly Census of Employment and Wages [QCEW] private employment; Alaska, Colorado, Maryland, Idaho, Illinois, Indiana, Kansas, Louisiana, Missouri, Washington, and Wisconsin);
- regimes 1 and 2: 1995-2013 (68\%; plus Arizona, California, Florida, Georgia, Minnesota, North Carolina, New York, Oregon, Montana, Pennsylvania, Rhode Island, South Dakota, Texas, and Wyoming);
- regimes 1-3: 1998-2013 (85\%; plus Connecticut, Hawaii, Kentucky, Michigan, North Dakota, New Jersey, New Mexico, Nevada, South Carolina, Tennessee, Virginia, and West Virginia); and
- regimes 1-4: 2004-2013 (100\%; plus Alabama, Arkansas, the District of Columbia, Delaware, Iowa, Massachusetts, Mississippi, Nebraska, New Hampshire, Ohio, Oklahoma, Utah, and Vermont).

The number in parentheses represents the percentage of private employment as reported in the Bureau of Labor Statistics (BLS) QCEW in 2012Q1 for the regimes listed. The construction of the different date regimes is shown graphically in figure 1. Table A1 presents a detailed tabulation of the coverage of each date regime.

[^5]
 coverage of the LEHD infrastructure data expressed as a percentage of 2012Q1 private Quarterly Census of Employment and Wages (QCEW) employment as received (solid line) and by date regime (dashed line). Office of Personnel Management data for federal workers are not shown in this figure but are available beginning in 2000 Q1. A color version of this figure is available online.

We did not create a separate date regime when the OPM data begin in 2000Q1 for two reasons. First, the proportion of reported federal jobs in 2000Q1 is small, no more than $4 \%$ of 2012Q1 UI-covered employment in a state and, on average, less than $1 \%$ except for the District of Columbia, where the proportion of OPM jobs is about $19 \%$. Second, although the proportion of OPM jobs in the District of Columbia is high, jobs there are part of regime 4, which does not begin until 2004Q1.

## C. Job and Person Sampling Frames

By 2004Q1, the LEHD data represent the complete universe of statutory jobs in the United States: all 50 states, the District of Columbia, and the federal government are reporting regularly. Before this date, LEHD data provide a complete frame for the states in each date regime (excluding the federal government before 2000Q1). After this date, the LEHD data provide a complete frame for the national population of UI-covered jobs, including federal employees. Studying job-level inequality, the task for which having a complete job frame is well suited, as a proxy for person-level inequality may be misleading because of the time-varying many-to-one assignment of jobs to workers. The number of employers per worker varies over the business cycle. Lower-earning workers tend to have more employers, complicating the interpretation of job-level results. ${ }^{19}$ Therefore, when studying inequality, it is preferable to have a person frame that covers a known population of interest, such as all persons legally eligible to work in the United States. For our analyses, we use two different approaches to creating frames of jobs and workers. The first approach relies only on the employer-employee links present in the UI data. This method captures all reported jobs. The second approach uses the US Census Bureau's edited version of the SSA's master SSN database (the Numident), capturing all reported employmenteligible workers but removing jobs associated with ineligible workers, as we elaborate below.

LEHD earnings records are reported quarterly by the employing firm. These records contain a nine-digit person identifier, typically assumed to be a SSN. However, at the time the report is received by the state UI office the nine-digit person identifiers are not verified, resulting in records both with and without a valid SSN. Using the Numident, we ascertain whether each earnings record is associated with a valid SSN. Records not associated with a valid SSN may have an alternate, valid person identifier, such as an Internal Revenue Service (IRS)-issued taxpayer identification number; nevertheless, we can distinguish only between valid and invalid SSNs. If the SSN

[^6]is valid, we have access to demographic characteristics, such as sex and birth date, from the Numident and other US Census Bureau sources. We also have an employment history from the UI wage records. If the SSN is not valid, we only have access to the employment history.

Our first frame, the "all-workers frame," contains earnings for all jobs reported on the UI data for each date regime in the relevant years from 1990 to 2013, as noted in figure 1. Our second frame, the "eligible-workers frame," is also delineated by these date regimes but includes jobs only for the subset of the all-workers frame that meets the following criteria:

- has a valid SSN on the Numident;
- individual is between the ages of 18 and 70 , inclusive;
- the year of the recorded data is greater than or equal to the SSN year of issue and less than or equal to the year of death (if available); and
- has a SSN that was associated with fewer than 12 jobs during the data year.

Every year from 1990 to 2013 in which an individual is between the ages of 18 and 70, an eligible worker is labeled as "active" in the labor market when UI earnings are positive and "inactive" otherwise. The valid SSN, age range, date of death, number of jobs, and active worker restrictions remove about $7 \%$ of the worker-year records found in the all-workers frame.

The purpose of the eligible-workers frame is twofold. The Numident data allow us to consistently identify a set of persons legally eligible to work each year while at the same time implicitly removing earning records from our analysis sample that are not associated with individuals in the covered population. We go a step further. We remove earnings records with valid SSNs where the available data strongly suggest that the SSN is not being used by the original owner. ${ }^{20}$ These two types of suspect nine-digit person identifiers-invalid SSNs that do not match to the Numident and valid SSNs apparently being used by multiple persons and/or for whom the age of the person issued the SSN is inconsistent with labor market activity-we call "immigrant candidates."

Table 1 presents basic counts of persons and jobs in the eligible-workers frame and the immigrant-candidate file. While we present some analysis of the immigrant-candidate jobs in appendix A , we do not have sufficient information to convert the collection of these jobs into an intertemporally consistent frame for this population of individuals. We have no plausible means of determining how many immigrant candidates are using each SSN in this collection of UI wage records.

[^7]Table 1
Observations per Year for Eligible Workers and Immigrant Candidates

| Year | Eligible Workers |  |  |  | Immigrant Candidates |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Persons | Inactive | Active | Jobs | Active | Jobs |
| 1990 | 190,814,228 | 167,224,366 | 23,589,862 | 34,936,872 | 1,585,988 | 2,173,054 |
| 1991 | 192,605,253 | 169,444,287 | 23,160,966 | 33,446,875 | 1,503,127 | 2,029,041 |
| 1992 | 194,341,714 | 171,098,747 | 23,242,967 | 33,588,257 | 1,485,173 | 2,024,225 |
| 1993 | 196,043,096 | 172,414,178 | 23,628,918 | 34,733,064 | 1,590,507 | 2,227,908 |
| 1994 | 197,726,878 | 173,562,792 | 24,164,086 | 36,705,168 | 1,737,988 | 2,546,460 |
| 1995 | 199,524,643 | 116,578,567 | 82,946,076 | 128,077,314 | 6,666,437 | 9,875,811 |
| 1996 | 201,276,549 | 117,660,582 | 83,615,967 | 129,681,393 | 6,725,830 | 10,144,571 |
| 1997 | 203,229,484 | 117,863,679 | 85,365,805 | 134,003,889 | 6,925,825 | 10,560,373 |
| 1998 | 205,266,723 | 94,856,664 | 110,410,059 | 173,778,794 | 8,919,168 | 13,680,138 |
| 1999 | 207,478,545 | 94,930,531 | 112,548,014 | 178,813,085 | 9,473,798 | 14,850,424 |
| 2000 | 209,895,465 | 94,701,668 | 115,193,797 | 184,243,425 | 9,975,102 | 15,909,402 |
| 2001 | 212,479,460 | 96,709,036 | 115,770,424 | 178,433,884 | 9,703,887 | 15,142,444 |
| 2002 | 214,891,408 | 99,804,179 | 115,087,229 | 172,249,424 | 9,109,574 | 13,646,946 |
| 2003 | 217,298,533 | 102,254,299 | 115,044,234 | 169,454,044 | 8,715,459 | 13,105,529 |
| 2004 | 219,763,469 | 83,200,954 | 136,562,515 | 202,935,084 | 10,218,971 | 15,254,789 |
| 2005 | 222,160,089 | 83,819,319 | 138,340,770 | 207,737,171 | 10,577,475 | 16,109,360 |
| 2006 | 224,721,578 | 84,357,718 | 140,363,860 | 212,227,031 | 10,943,861 | 16,830,576 |
| 2007 | 227,553,012 | 85,518,594 | 142,034,418 | 213,889,946 | 10,818,763 | 16,464,027 |
| 2008 | 230,355,015 | 88,245,425 | 142,109,590 | 206,906,286 | 9,845,415 | 14,509,746 |
| 2009 | 232,813,313 | 94,864,949 | 137,948,364 | 188,220,068 | 8,358,069 | 11,701,711 |
| 2010 | 234,304,705 | 96,959,047 | 137,345,658 | 188,740,259 | 7,919,195 | 11,019,697 |
| 2011 | 235,429,997 | 96,619,700 | 138,810,297 | 193,351,447 | 7,813,411 | 10,942,606 |
| 2012 | 236,484,312 | 96,068,987 | 140,415,325 | 197,879,809 | 8,254,250 | 11,556,277 |
| 2013 | 237,816,938 | 96,151,327 | 141,665,611 | 202,277,055 | 9,310,868 | 13,216,695 |

[^8]Even accounting for the increasing coverage of each date regime, there is a clear, strong upward trend in the number of immigrant-candidate records until the Great Recession and a strong downward trend thereafter. Because there are data in the system for each of these records, the associated ninedigit person identifier represents at least one worker but may represent many. A great deal of supplemental research would be required to estimate the relation between how many jobs are reported for a "worker" in the immigrant-candidate records and the number of individuals employed. Even more research would be required to estimate their characteristics. We do not attempt such research here. We note that when we use the all-workers frame, each associated nine-digit person identifier counts as one individual, but there is no adjustment for being inactive; that is, we do not assume zero earnings when this "worker" has no reported earnings. When we use the eligible-workers frame, all immigrant-candidate records are excluded. Eli-
gible inactive workers are assumed to have zero earnings when there is no reported activity in any job.

Appendix A contains additional detailed analyses of the construction of the eligible-workers frame. In particular, figure A1 plots the count of earnings records excluded from the eligible-workers frame each year, disaggregated by earnings records each year associated with individuals who have invalid SSNs who are either too young or too old and/or who report working 12 or more jobs in a year. Detailed counts are reported in table A2.

## C. Earnings Definitions and Coverage

In this section, we define our earnings measures for both the all-workers frame and the eligible-workers frame. Our primary measure of earnings is based on annual UI job-level earnings reports. We adjust nominal earnings to real earnings using the consumer price index for all urban consumers (CPI-U), with 2000 as the base year. Let $y_{i j t}$ be the real earnings for worker $i$ employed at firm $j$ in year $t$. Person-level annual earnings sum all jobs for each worker in each year:

$$
\begin{equation*}
e_{i t}=\sum_{j} y_{i j t} \tag{1}
\end{equation*}
$$

Using $e_{i t}$, we estimate total annual earnings for the eligible-workers frame in year $t$ using

$$
\begin{equation*}
E_{t}^{\mathrm{EW}}=\sum_{i \mid(i, t) \in \mathrm{EW}} e_{i}, \tag{2}
\end{equation*}
$$

where $\mathrm{EW}_{t}$ is the set of workers in the eligible-workers frame in year $t$. For the period 2004-13, when our frames contain data for the entire United States, the eligible-workers frame is approximately $90 \%$ of wage and salary compensation as defined in the national income and product accounts (NIPA). ${ }^{21}$

## D. Estimation of the Earnings/Inactivity Distribution

We begin by calculating deciles of eligible-workers person-level earnings, $e_{i t}$, pooled across the years 2004-13. Using these deciles, we create three earnings bins, as shown in table 2. The bins are designed to capture the bottom, middle, and top of the earnings distribution over the entire 10 -year period. For example, the first two columns in table 2 show the results for bin 2, workers in the bottom $20 \%$ of the earnings distribution. ${ }^{22}$ Workers in this bin have a minimum annual earnings value of $\$ 2$, a maximum value

[^9]Table 2
Descriptive Statistics by Real Earnings Bins

|  | Earnings Bins $\left(e_{i t}\right)$ |  |  |
| :--- | :---: | :---: | :--- |
|  | 2: Bottom $20 \%$ | 3: Middle $60 \%$ | 4: Top 20\% |
| Minimum | $.693(2)$ | $8.795(6,600)$ | $10.750(46,630)$ |
| Mean | $7.473(1,760)$ | $9.938(20,700)$ | $11.240(76,110)$ |
| Maximum | $8.795(6,600)$ | $10.750(46,630)$ | $16.140(10,220,000)$ |

Note.-The table presents statistics on real earnings for three categories of workers: (i) the bottom $20 \%$ of the pooled annual-earnings distribution of eligible workers from 2004 to 2013 ("Bin 2"), (ii) the middle $60 \%$ ("Bin 3"), and (iii) the top $20 \%$ ("Bin 4"). The rows show the minimum, mean, and maximum log earnings, $\log \left(e_{i t}\right)$, of each bin. The exponentiated values (implied geometric means) are listed in parentheses. All earnings are in real 2000 dollars (adjusted using the consumer price index for all urban consumers). The minimum and maximum values of each bin are rounded to four significant digits. The quantiles, but not the means or geometric means, were computed from data winsorized at the 0.01 and 99.99 percentiles.
of $\$ 6,600$, and a mean log earnings in real 2000 dollars of $\$ 7.473$ (implied geometric mean real earnings, $\$ 1,760$ ).

The low mean log earnings in bins 2 and 3 suggest that a large proportion of workers in these bins are employed for only part of the year. In table 3 we present information about the labor force activity of workers in each of the three earnings bins. Each row in the table (except the residual category "All

Table 3
Labor Force Activity of Workers in Each Earnings Bin

| $\begin{array}{l}\text { Quarters Worked, } \\ \text { Longest Job }\end{array}$ | Workers |  |  |  | $\begin{array}{c}\text { Average } \\ \text { No. of Jobs }\end{array}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | \(\left.$$
\begin{array}{c}\text { Counts }\end{array}
$$ \begin{array}{c}Average <br>

Earnings (\$)\end{array}\right)\)

Note.-Each row in the table represents a specific combination of quarters worked and number of quarters in the longest job. The number of quarters in the longest job takes on values from 1 to 6 . A 5 -quarter longest job is active in either the fourth quarter of the previous year or the first quarter of the subsequent year, while a 6-quarter longest job is active in both. The most prevalent pattern in each earnings bin is listed first with the next most prevalent second, continuing until the table contains the patterns for approximately $80 \%$ of the workers in a typical year. "All other" is the residual category. The counts are averages per year from the eligible-workers frame. The full table of counts is available in table A4.
other") represents a specific combination of quarters worked and number of quarters in the longest job, truncated at a maximum of 6 quarters. The number of quarters in the longest job takes on values from 1 to 6 . A 5 -quarter longest job is active in either the fourth quarter of the previous year or the first quarter of the subsequent year, while a 6-quarter longest job is active in both. Thus, a 6 -quarter active job is active at the beginning of a calendar year, the end of a calendar year, and all quarters in the middle. The most prevalent pattern in each earnings category is listed first, followed by the next most prevalent and continuing until the table contains the patterns for approximately $80 \%$ of the workers in a typical year.

The dominant labor force attachment pattern varies substantially across bins: $31 \%$ of the workers in the bottom $20 \%$ of the earnings distribution work only 1 quarter. In contrast, for workers in the top $20 \%$ of the earnings distribution, the most common labor force status is employment with at least one firm for the entire year. Although there are almost certainly large differences in average wages for workers at the bottom, middle, and top of the earnings distribution, one of the primary reasons average annual earnings for workers in the bottom earnings category are so low is that they are employed for only a small portion of the year.

Finally, we combine the earnings bins discussed above with the active/ inactive status information available for the eligible-workers frame to create four mutually exclusive earnings/inactivity categories:

1. eligible to work but no reported UI earnings (inactive);
2. working and in the bottom $20 \%$ of the overall UI earnings distribution;
3. working and in the middle $60 \%$ of the overall UI earnings distribution; and
4. working and in the top $20 \%$ of the overall UI earnings distribution.

We analyze these four bins comprehensively in Sections IV and V, when we study the dynamics of earnings distribution changes and the role of the firm.

## III. Inequality Trends in the LEHD Infrastructure Data (1990-2013)

The determination of an appropriate frame for studying changes in earnings inequality led us to analyze our eligible-workers frame, which is the complete population for the United States during the critical period from 2004 to 2013. The results in this section and in the rest of the paper relate exclusively to the eligible-workers frame. Where we have also analyzed comparable data for the all-workers frame, we reference results in appendix B.

We begin by examining the evolution of the percentiles of the earnings distribution. To understand how state entry into the LEHD partnership might affect the earnings distribution over time, we estimate percentiles
of the earnings distribution for workers in each of the four date regimes by year. Figure 2 plots the 10 th, 20th, 50 th, 80 th, 90 th, and 95 th percentiles of the cumulative earnings distribution by date regime. The cumulative distribution contains data for all regimes less than or equal to the date regime shown in the legend.

Notice that differences in the 10th, 20th, and 50th percentiles are virtually indistinguishable across date regimes. Above the median, however, there is some variation in the 80th, 90th, and 95th percentiles across date regimes. In particular, the inclusion of data from high earnings and populous states, like California and New York, in date regime 2 increases the estimated quantile values, especially for the 95th percentile. However, once these states have entered, the effect of the states entering in regimes 3 and 4 is much less pronounced. The level differences in the percentiles are relatively minor, especially after 1995 (regime 2 ). The trends in inequality are very similar across date regimes. We conclude that the date of state entry does not appear to significantly affect earnings inequality measures, especially after 1995. ${ }^{23}$

We next turn to the evolution of earnings inequality over the past 23 years. Figure 3 presents the following measures of earnings inequality: (i) the ratio of the 99 th to the 1 st percentile ( $99 / 1$ ratio and so forth), (ii) the ratio of the 95 th to the 5 th percentile, (iii) the ratio of the 90 th to the 10 th percentile, (iv) the ratio of the 80 th to the 20th percentile, and (v) the variance of log earnings. ${ }^{24}$ These measures are all reported relative to their value in 2000. ${ }^{25}$ After 2000, there is a persistent increase in earnings inequality according to all measures. On average, the $99 / 1$ ratio is $15.4 \%$ higher, the $95 / 5$ ratio is $13.6 \%$ higher, and the $90 / 10$ ratio is $11.4 \%$ higher than in 2000 . Much of the rise in earnings inequality occurs during the Great Recession and persists into the recovery. For example, the $90 / 10$ ratio was, on average, $6.7 \%$ higher

[^10]

$\begin{array}{llll}0 & 8 & 8 & 8 \\ 0 & 0 & 0 & 0 \\ 0 & 8 & 0 & 0\end{array}$
60,000
50,000
40,000
30,000
20,000
10,000
Fig. 2.-Percentiles of the earnings distribution for eligible workers by cumulative date regime. The figure plots the 10th, 20th, 50th, 80th, әш!
 For example, "P95 Regime 2" indicates the 95 th percentile for all states in regimes 1 and 2. A color version of this figure is available online.


Fig. 3.-Selected inequality measures 1990-2013, relative to 2000. The figure presents measures of earnings inequality for eligible workers in all states relative to 2000 from 1990 to 2013 . The measures of earnings inequality considered are (i) the ratio of the 99 th to the 1 st percentile ("P99 to P1"), (ii) the ratio of the 95 th to the 5th percentile ("P95 to P5"), (iii) the ratio of the 90th to the 10th percentile ("P90 to P10"), (iv) the ratio of the 80th to the 20th percentile ("P80 to P20"), and (v) the variance of log annual earnings ("Variance"). Results are based on the eligible-workers frame from the Longitudinal Employer-Household Dynamics infrastructure files. A color version of this figure is available online.
from 2001 to 2007 than in 2000. Then, during the Great Recession, the 90/ 10 ratio was $15.1 \%$ higher from 2008 to 2009 than in 2000 . This increase does not peak until 2010, resulting in inequality being $17.8 \%$ higher from 2010 to 2013 than in 2000. Except for the 99/1 ratio, post-2000 trends do not appear in the all-workers frame. ${ }^{26}$

Figure 4 presents changes in the top and bottom halves of the earnings distribution by decomposing the ratios around the median. ${ }^{27}$ At the top of

[^11]

Fig. 4.-Selected inequality measures for the top and bottom of the earnings distribution 1990-2013, relative to 2000. $A$ and $B$ decompose the $99 / 1$ ratio, the $95 / 5$ ratio, the $90 / 10$ ratio, and the $80 / 20$ ratio for eligible workers in all states relative to 2000 from 1990 to 2013 relative to the median. A plots the following ratios for the top half of the earnings distribution: (i) the ratio of the 99th to the 50th percentile ("P99 to P50"), (ii) the ratio of the 95th to the 50th percentile ("P95 to P50"), (iii) the ratio of the 90 th to the 50 th percentile ("P90 to P50"), and (iv) the ratio of the 80th to the 50th percentile ("P80 to P50"). $B$ plots the following ratios for the bottom half of the earnings distribution: (i) the ratio of the 50th to the 1st percentile ("P50 to P1"), (ii) the ratio of the 50th to the 5th percentile ("P50 to P5"), (iii) the ratio of the 50th to the 10 th percentile ("P50 to P10"), and (iv) the ratio of the 50th to the 20th percentile ("P50 to P20"). The estimates are based on the eligible-workers frame from the Longitudinal Employer-Household Dynamics infrastructure files. See figure B4 for comparable data using the all-worker frame. A color version of this figure is available online.
the distribution, we compute the ratio of the 99th to the 50th percentile (99/ 50 ratio and so forth), the ratio of the 95 th to the 50 th percentile, the ratio of the 90 th to the 50 th percentile, and the ratio of the 80 th to the 50 th percentile. At the bottom, we analyze the ratio of the 50 th to the 1 st percentile, the ratio of the 50 th to the 5 th percentile, the ratio of the 50 th to the 10 th percentile, and the ratio of the 50th to the 20th percentile. These ratios are all reported relative to the their value in $2000 .{ }^{28}$ The top and the bottom of the earnings distribution have evolved quite differently. Since 2000, the ratios of the top percentiles to the median have been increasing very gradually, as shown in figure $4 A$. However, this increase at the top has been small compared with the rise in inequality at the bottom of the earnings distribution, as shown in figure $4 B$. The ratios of the median to the bottom percentiles have been increasing dramatically, indicating that earnings growth at the bottom of the distribution has not kept up with earnings growth at the median. The bottom of the earnings distribution is more cyclically sensitive, with much of the rise in inequality occurring during the Great Recession. ${ }^{29}$

To summarize, earnings inequality has been on the rise since 2000 and spiked during the Great Recession. This conclusion depends materially on our use of the eligible-workers frame. Direct use of the all-workers framethat is, using all of the job records in the LEHD infrastructure files-produces earnings inequality measures and trends that appear not to change from 2000 through the Great Recession to 2013. Constructing the eligibleworkers frame by excluding immigrant-candidate records shifts the earnings distribution of eligible workers to the right of the earnings distribution of all workers. While this shift in the earnings distribution is not particularly surprising, the resulting change in the trends in earnings inequality between the two frames is. When studying changes in earnings inequality over time, especially when using administrative data, the choice of worker frame matters substantially.

## A. Comparison of LEHD Data to the CPS and the ACS

To understand the differences between analyses using respondentprovided earnings data in large-scale household surveys and those using administrative data on earnings in the UI system, we constructed detailed analysis samples from the CPS-ASEC (1990-2004) and the ACS (20002013). We also linked the LEHD earnings data to the ACS data at the individual record level (2005-13). We used the linked data to study differences between individuals found only in the ACS data and those found in both

[^12]Table 4
Average Percentiles of the Earnings Distribution from Household Surveys versus Longitudinal Employer-Household Dynamics (LEHD)

|  | Percentile |  |  |  |  |  |  |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Frame | 5th | 10th | 20th | 50th | 80th | 90th | 95th |
| CPS/ACS: covered workers | 3,419 | 6,412 | 11,703 | 26,345 | 49,059 | 67,872 | 89,323 |
| LEHD: eligible workers | 1,005 | 2,527 | 6,463 | 21,762 | 45,343 | 64,021 | 86,108 |
| Difference: HHLD survey - UI | 2,414 | 3,884 | 5,240 | 4,583 | 3,716 | 3,850 | 3,215 |
| Ratio of HHLD survey to UI | 3.4027 | 2.5370 | 1.8108 | 1.2106 | 1.0819 | 1.0601 | 1.0373 |

Note.-The first row presents the average percentile values from the earnings distribution of covered workers in the combined Current Population Survey (CPS)/American Community Survey (ACS) data from 1995 to 2013. The second row presents the average percentile values from the earnings distribution of eligible workers in all states from 1995 to 2013. The third row computes the difference between the average percentiles in the household surveys and the same ones computed from the LEHD eligible-workers frame. The last row computes the ratio of each percentile from the covered workers in the household surveys to the LEHD eligible-workers frame. HHLD $=$ household.
sources. ${ }^{30}$ Details on the data construction can be found in section C 1 of appendix C. Details on the data linkage can be found in section C3 of appendix C.

In the household survey data, we defined "covered workers" to be individuals who worked in a job that should have appeared in the LEHD data. Table 4 shows that the estimated percentile values of the earnings distribution tend to be greater for covered workers than for all workers in the household survey data. ${ }^{31}$ For percentiles at or above the median, the values from the LEHD eligible-workers frame are close to the ones from the covered workers in household surveys. Below the median, however, the differences are greater, with the percentiles estimated from the household surveys being much greater than the percentiles estimated from the LEHD eligibleworkers frame. For example, earnings associated with the 10th percentile in the CPS/ACS data are close to the 20th percentile in the LEHD data. ${ }^{32}$ We conclude that the differences between survey-reported and administrative earnings data at or above the median are minimal. Below the median, conclusions must be more nuanced. Household surveys seem to capture earnings not captured by the administrative data, but it is difficult to know what to conclude from that finding. One possibility is that respondents report earnings from activity that so closely resembles formal sector work we think we ought to find corresponding earnings reports but do not. Another

[^13]plausible explanation is that the coverage of the low-earning population is very different in the ACS compared with the UI data. We consider reconciling the administrative and survey data at the bottom of the earnings distribution to be an open research question. ${ }^{33}$

Figure 5 shows that the trends in earnings inequality in the household survey data are consistent with our findings from the eligible-worker frame in the LEHD data and are inconsistent with the findings from the all-worker frame. This conclusion also holds for the analysis of trends in the top and bottom separately. ${ }^{34}$ The pattern of inequality ratios around the Great Recession also is similar to the one found in the eligible-workers frame and is dissimilar to the analysis based on the all-workers frame. ${ }^{35}$ Additional results and discussion are provided in section C 2 of appendix C .
To better understand the discrepancies at the bottom of the earnings distribution, we analyzed linked ACS and LEHD individual records. Eightyfive percent of the individuals we expect to find in both the ACS and the LEHD data are present in both with positive earnings. The other $15 \%$ are not found in the LEHD data and, therefore, have zero administrative earnings. ${ }^{36}$ The result suggests that survey respondents are giving answers that imply that their job should be covered in the administrative data, but there are not corresponding administrative records to match the survey-reported income. The reported income of these individuals appears to be the reason for the discrepancy between the survey and administrative data at the bottom of the earnings distribution. ${ }^{37}$

Our analysis of the trends in earnings inequality using the various samples of workers in CPS/ACS and the two worker frames in the LEHD data shows that, whether the data were designed or found, an understanding of the contributions of individuals included or excluded from the sample is essential. Conclusions regarding fundamental trends in inequality depend on these decisions.

## B. Effects of Inactivity on Earnings Inequality

We used our household survey to confirm that the trends in the estimated employment-to-population ratio produced directly from the micro data match those of the official estimates. In particular, the employment-topopulation ratio fell during the Great Recession and had not recovered through $2013 .{ }^{38}$

[^14]

Fig. 5.-Selected inequality measures 1990-2013, relative to 2000 (Current Population Survey [CPS]/American Community Survey [ACS]). A, All workers from household surveys. $A$ presents measures of earnings inequality for all workers in CPS/ACS relative to 2000 from 1990 to 2013. B, Covered workers from household surveys. $B$ presents measures of earnings inequality for covered workers in CPS/ ACS relative to 2000 from 1990 to 2013. The measures of earnings inequality considered are (i) the ratio of the 95th to the 5th percentile ("P95 to P5"), (ii) the ratio of the 90 th to the 10 th percentile ("P90 to P10"), (iii) the ratio of the 80th to the 20th percentile ("P80 to P20"), and (iv) the variance of log annual earnings ("Variance"). A color version of this figure is available online.

We document that around 30 million eligible workers per year had no earnings in the current year but positive earnings in at least one of the past 4 years. ${ }^{39}$ Their treatment materially affects the distribution of earnings in any given year. It also materially affects the cyclical features of inequality mea-

[^15]sures, such as the Gini coefficient. ${ }^{40}$ Additional results and discussion are provided in section D2 of appendix D.

Although it is unclear which of the adjusted inequality measures correctly weights the inactive workers, it is worthwhile to consider adjusted measures that count at least some of the zero-earning workers as part of any general analysis of changes in earnings inequality.

## IV. Decomposing Changes in the Earnings Distribution

## A. Evolution of the Earnings/Inactivity Distribution

Beginning in 2004 our eligible-workers frame is complete, including all states, the District of Columbia, and the federal government. The adventitious timing of the start of the complete-data period presents us with the opportunity to study the evolution of the earnings distribution and the dynamics of nonemployment during three distinct epochs of labor market conditions. According to the National Bureau of Economic Research (NBER), the Great Recession began in December 2007 and ended in June 2009. Applying this definition to annual data, we have a prerecession epoch spanning 2004-7, a recession epoch running from 2008 to 2009, and a postrecession epoch beginning in 2010 and ending in 2013.

As we did in Section II.D, we simplify the earnings distribution by assigning each active worker to one of three earnings categories (bottom, middle, and top) and assign inactive but eligible workers to a fourth category. Using the estimated annual earnings/inactivity distributions, we start by comparing the distribution in 2005 with the distribution in 2004, repeating this process for each subsequent year until 2013. Each year, the earnings/ inactivity distribution may change relative to the previous year. The extent of this change depends on the number of workers entering and exiting the eligible-workers frame, the number of workers moving between earnings/ inactivity categories, and changes in average earnings within each category. ${ }^{41}$

From 2004 through 2013 there is relatively strong growth in the number of eligible workers, averaging about $1 \%$ per year through 2009 and declining to about half that rate after 2009, although growth within each category is uneven. For example, the largest growth in the number of workers occurs in the eligible to work but inactive category (i.e., no earnings in the indicated year), a category with a growth rate almost twice that of any other group. The growth rate of workers in the bottom and middle earnings categories

[^16]is less than half the overall growth rate. When we examine total earnings, most of the growth is found in the top $20 \%$ of the earnings distribution, with relatively little growth in the bottom $80 \%$. Given that average earnings are falling for the bottom $80 \%$ of workers, it should not be surprising that total earnings for this group fails to keep pace with the growth in the number of workers. The situation for workers at the top, however, is much brighter: the top $20 \%$ of workers have relatively strong earnings growth of $4.4 \%$ over the period, resulting in growth in total earnings ( $12.2 \%$ ) that outpaces the growth in the number of workers ( $7.8 \%$ ).

The relatively high growth in both the number of eligible workers and the average earnings in the top $20 \%$ of the earnings distribution has a strong effect on the distribution of total earnings. Figure 6 shows the share of total earnings attributed to each earnings category by year. We see substantial earnings inequality: earnings for the top $20 \%$ of workers are greater than those for the bottom and middle combined, with the relative share of the top increasing almost continuously except for a brief pause in 2008 during the height of the Great Recession. We also see the declining share of income accruing to the middle $60 \%$ of workers. Although the number of workers in the middle recovered after the Great Recession, average earnings continued to decline while higher growth in the number of workers at the bottom and top resulted in a declining share of earnings for workers in the middle $60 \%$ of the earnings distribution.


Fig. 6.-Share of total earnings in each earnings category. The figure plots the share of total earnings in each earnings category by year for the following categories: (i) the bottom $20 \%$ of the earnings distribution ("Bin 2"), (ii) the middle $60 \%$ of the earnings distribution ("Bin 3"), and (iii) the top $20 \%$ of the earnings distribution ("Bin 4"). A color version of this figure is available online.

## B. Earnings/Inactivity Distribution: Decomposition of the Changes

In the previous section, we discussed the changing structure of the earnings/inactivity distribution around the time of the Great Recession. Several key facts stand out. First, there is enormous growth in the number of eligible workers with no reported earnings from 83,200,954 in 2004 to $96,959,047$ in 2010, remaining as high as $96,151,327$ in 2013. Second, average earnings stagnate (bottom 20\%) or decline (middle 60\%) for active workers. Third, the growth in the share of earnings accruing to the top $20 \%$ results from both growth in the number of workers and average earnings in that category. ${ }^{42}$

To better understand these changes, we turn our focus to the flows of workers moving between active and inactive status as well as between different earnings categories. When interpreting these results, we implicitly assume average earnings within each category are stable between 2004 and 2013. Although changes in average earnings have a role to play, the data suggest that we focus on worker flows because the impact of a change in the number of workers dominates the impact of a change in average earnings for each category. ${ }^{43}$

Starting in 2005, each year we calculate the change in the number of workers between the current year and the previous year for the four earnings/inactivity categories. The year-to-year change in the number of workers in a specific category is driven by changes in the number of workers entering (inflows) and the number of workers leaving (outflows). Section E1 of appendix E provides the derivation of the flow accounting that we summarize here.

Figure 7 shows the change in the number of workers for each earnings/ inactivity category by year. The data used to calculate the year-to-year differences can be found in the first panel of table E1. Each line in the graph represents the year-to-year change in the number of workers for one of the four earnings/inactivity categories. For example, in 2009 there were 94,864,949 eligible workers with no reported UI earnings, while in 2008 there were only $88,245,425$ workers in the same category, resulting in an increase of $6,619,524$ workers. This increase in the number of eligible but inactive workers occurred during the height of the Great Recession and dwarfs the change in any other period, even the relatively large increases in the preceding and subsequent years. The area between the inactive line and the $X$ axis represents the cumulative change in the number of eligible workers with

[^17]

Fig. 7.-Year-to-year change in the number of workers in each earnings bin. Estimates are based on the authors' calculations using year-to-year changes in the distribution of inactive and active workers among the activity/earnings bins. A color version of this figure is available online.
no earnings over the entire period of $12,950,373$. We can clearly see that the recovery has largely failed to reduce the number of eligible workers with no earnings through 2013. In contrast, the middle $60 \%$ faced a large reduction in numbers during the Great Recession, but, unlike the inactive category, the number of workers in the middle has returned to prerecession levels, as reflected by the area between the middle $60 \%$ line and the $X$-axis.

Table 5 presents an overview of the flow analysis, which we decompose using the transition count matrix. The "Count $t-1$," "Count $t$," and "Net Change" columns are shown in table E1 and figure 7. They are reproduced here for comparison with sums of the transition counts. The stayers (i.e., $c_{22}$ ) are also included, and while they do not directly affect the net change in the flows, they represent the number of workers who remain in a given category for at least 2 years-giving an indication of the earnings stability of the typical worker. The outflows, inflows, and net change columns show the results of using equation (E1). The difference between the inflows and the outflows equals the net change, which should also equal the difference in counts between the current period and the previous period. For example, returning to the eligible workers with no earnings in 2009, we can see that the inflows were $16,166,420$ and the outflows were $9,546,896$. The large increase in the number of workers in this category was due primarily to a large increase in the inflows relative to the previous year and a small decrease in the number of outflows. That is, a relatively large number of workers who had a job in the previous year were unable to find an employer in the current year, while a relatively small number of workers without a job in the previous year were able to find one in the current year or moved out of the eligible-workers frame.

The table also shows a relatively large increase in the number of eligible workers with no earnings for at least 2 years over the entire period (stayers in the "Eligible but No Reported UI Earnings" panel). The change in the number of stayers equals the difference between the inflows in the previous period (the candidates to become stayers) minus the outflows in the current period. For example, in 2008 there were 13,271,459 eligible workers with at least 1 year without reported earnings (inflows), and 9,546,896 of these workers transitioned to another category in 2009 (outflows), resulting in an increase in the stayers between 2008 and 2009 of 3,724,563 workers. The stayers are useful for understanding the short-term (2-year) volatility differences between each of the categories. For example, the bottom $20 \%$ of the UI earnings distribution has relatively few stayers compared with the middle and the top, consistent with the results presented earlier that most of these jobs are of relatively short duration. The results also imply that a large number of workers in the bottom $20 \%$ of the earnings distribution stay there for only a year or two before moving to another category, frequently inactivity.

Table 6 presents demographic characteristics for the 24 possible year-toyear transitions, excluding workers not eligible to work in both year $t-1$ and year $t$. The transitions labeled 0 represent workers moving into or out of the eligible-workers frame. The workers moving into the eligible-worker frame are typically young and predominately nonwhite, while the workers leaving the eligible workforce are typically older ( 60 years of age or more) and predominately white. One interesting transition group is the $0 \_4$ (workers not eligible in $t-1$ who transition to the top $20 \%$ of the earnings distribution in $t$ ). These workers are predominately older than other newly eligible workers, male, nonwhite, and overwhelmingly not born in the United States. The remaining transitions have roughly similar characteristics, although older male workers are generally more prevalent in transitions associated with bin 4 (the top 20\%), while female workers are more likely to be associated with transitions with bin 2 (the bottom 20\%).

Next, we decompose the inflows and outflows further by using the transition matrix of counts. Figures 8-12 show the outflows and inflows for each earnings/inactivity category and the relevant transition counts by year. In particular, each year an individual can be in one of the following states: bin 0 , not in the eligible-workers frame, or bins $1-4$ as defined in Section II.D. We remind the reader that the cutoffs for the real earnings distribution bins are based on the pooled years 2004-13 and do not change over time. It is possible for substantially more or less than $20 \%$ of current earners to be in the top $20 \%$ bin, for example, in any given year.

The first subplot in each figure shows the gross outflows (solid line) and the gross inflows (dashed line) into an earnings/inactivity category. The difference between the two lines is the net inflows presented in the last column of table 5. The second subplot shows the transitions to other categories

Table 5
Flows into and out of Each Earnings Category

| Year | Count <br> $t-1$ | Count $t$ | Net <br> Change | Stayers | Outflows | Inflows |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | | Net |
| :---: |
| Change |


| 2005 | 83,200,954 83,819,319 | 618,365 | 71,931,565 11,269,389 | 11,887,754 | 618,365 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2006 | 83,819,319 84,357,718 | 538,399 | 72,513,714 11,305,605 | 11,844,004 | 538,399 |
| 2007 | 84,357,718 85,518,594 | 1,160,876 | 73,295,146 11,062,572 | 12,223,448 | 1,160,876 |
| 2008 | 85,518,594 88,245,425 | 2,726,831 | 74,973,966 10,544,628 | 13,271,459 | 2,726,831 |
| 2009 | 88,245,425 94,864,949 | 6,619,524 | 78,698,529 9,546,896 | 16,166,420 | 6,619,524 |
| 2010 | 94,864,949 96,959,047 | 2,094,098 | 82,548,100 12,316,849 | 14,410,947 | 2,094,098 |
| 2011 | 96,959,047 96,619,700 | -339,347 | 83,573,226 13,385,821 | 13,046,474 | -339,347 |
| 2012 | 96,619,700 96,068,987 | -550,713 | 83,628,961 12,990,739 | 12,440,026 | -550,713 |
| 2013 | 96,068,987 96,151,327 | 82,340 | 83,990,110 12,078,877 | 12,161,217 | 82,340 |
|  | Bottom 20\% of the Overall UI Earnings Distribution |  |  |  |  |
| 2005 | 27,062,314 27,376,301 | , | 12,712,348 14,349 | 14,663,953 | 87 |
| 2006 | 27,376,301 27,598,826 | 222,525 | 12,919,731 14,456,570 | 14,679,095 | 222,525 |
| 2007 | 27,598,826 27,800,774 | 201,948 | 13,055,172 14,543,654 | 14,745,602 | 201,948 |
| 2008 | 27,800,774 28,120,283 | 319,509 | 13,270,031 14,530,743 | 14,850,252 | 319,509 |
| 2009 | 28,120,283 28,119,169 | -1,114 | 13,215,490 14,904,793 | 14,903,679 | -1,114 |
| 2010 | 28,119,169 28,154,014 | 34,845 | 13,057,840 15,061,329 | 15,096,174 | 34,845 |
| 2011 | 28,154,014 28,498,111 | 344,097 | 13,227,239 14,926,775 | 15,270,872 | 344,097 |
| 2012 | 28,498,111 28,269,636 | -228,475 | 13,415,083 15,083,028 | 14,854,553 | -228,475 |
| 2013 | 28,269,636 28,119,381 | -150,255 | 13,437,328 14,832,308 | 14,682,053 | -150,255 |


| 2005 | $82,821,341$ | $84,079,363$ | $1,258,022$ | $69,752,528$ | $13,068,813$ | $14,326,835$ | $1,258,022$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2006 | $84,079,363$ | $84,946,369$ | 867,006 | $70,696,052$ | $13,383,311$ | $14,250,317$ | 867,006 |
| 2007 | $84,946,369$ | $85,576,064$ | 629,695 | $71,377,690$ | $13,568,679$ | $14,198,374$ | 629,695 |
| 2008 | $85,576,064$ | $85,548,690$ | $-27,374$ | $71,739,593$ | $13,836,471$ | $13,809,097$ | $-27,374$ |
| 2009 | $85,548,690$ | $81,894,162$ | $-3,654,528$ | $69,594,276$ | $15,954,414$ | $12,299,886$ | $-3,654,528$ |
| 2010 | $81,894,162$ | $81,314,722$ | $-579,440$ | $67,945,643$ | $13,948,519$ | $13,369,079$ | $-579,440$ |
| 2011 | $81,314,722$ | $82,538,961$ | $1,224,239$ | $68,441,704$ | $12,873,018$ | $14,097,257$ | $1,224,239$ |
| 2012 | $82,538,961$ | $83,930,862$ | $1,391,901$ | $69,837,520$ | $12,701,441$ | $14,093,342$ | $1,391,901$ |
| 2013 | $83,930,862$ | $84,707,469$ | 776,607 | $71,114,783$ | $12,816,079$ | $13,592,686$ | 776,607 |


| 2005 | $26,678,860$ | $26,885,106$ | 206,246 | $22,942,722$ | $3,736,138$ | $3,942,384$ | 206,246 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2006 | $26,885,106$ | $27,818,665$ | 933,559 | $23,460,710$ | $3,424,396$ | $4,357,955$ | 933,559 |

Table 5 (Continued)

|  | Count <br> Year <br> $t-1$ | Count $t$ | Net <br> Change | Stayers | Outflows | Inflows | Net <br> Change |
| :--- | :---: | :---: | ---: | :---: | :---: | :---: | ---: |
| 2007 | $27,818,665$ | $28,657,580$ | 838,915 | $24,260,307$ | $3,558,358$ | $4,397,273$ | 838,915 |
| 2008 | $28,657,580$ | $28,440,617$ | $-216,963$ | $24,629,289$ | $4,028,291$ | $3,811,328$ | $-216,963$ |
| 2009 | $28,440,617$ | $27,935,033$ | $-505,584$ | $24,138,725$ | $4,301,892$ | $3,796,308$ | $-505,584$ |
| 2010 | $27,935,033$ | $27,876,922$ | $-58,111$ | $24,278,404$ | $3,656,629$ | $3,598,518$ | $-58,111$ |
| 2011 | $27,876,922$ | $27,773,225$ | $-103,697$ | $24,365,840$ | $3,511,082$ | $3,407,385$ | $-103,697$ |
| 2012 | $27,773,225$ | $28,214,827$ | 441,602 | $24,551,484$ | $3,221,741$ | $3,663,343$ | 441,602 |
| 2013 | $28,214,827$ | $28,838,761$ | 623,934 | $25,057,962$ | $3,156,865$ | $3,780,799$ | 623,934 |

Note.- The estimates are based on the authors' calculations using transitions into and out of the eligibleworkers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories. $\mathrm{UI}=$ unemployment insurance.
associated with the gross outflows line in the first graph. Note that the sum of each series in the second subplot is equal to the gross outflows line in the first subplot. The third subplot shows the transition counts associated with gross inflows. Similarly, the sum of each of the series in the third subplot is equal to the gross inflows line in the first subplot.

Figure 8 plots the counts of workers moving out of the eligible-workers frame and those moving into the frame. Notice that gross inflows into eligibility are always greater than gross outflows from eligibility. Thus, net inflows into eligibility are always positive but decline and fail to recover after the Great Recession. This decline is primarily due to a decrease of inflows into eligibility, although there is a small increase in outflows as well. Notice that the outflows from eligibility come primarily from inactivity. Recall that inactive individuals are part of the eligible-workers frame but have no reported earnings. The first row under the "Inactivity" origin category in table 6 shows that inactive workers moving to ineligibility (1_0) tend to be older, with an average age of 68 . The inflows into eligibility tend to be young workers around the age of 20 moving into either inactivity or the bottom $20 \%$ of the earnings distribution. The exception are individuals moving into the top $20 \%$ of the earnings distribution (0_4), who tend to be older (average age is 33 years old), male ( $79.1 \%$ are male), and foreign born (only $12.7 \%$ are born in the United States). Prior to the Great Recession, on average 38.3\% of workers moving into eligibility went into inactivity and $49.1 \%$ went into the bottom of the earnings distribution. This flipped during the Great Recession, with $47.5 \%$ of newly eligible workers moving into inactivity and $43.4 \%$ moving into the bottom of the earnings distribution.

Figure 9 plots the flows into and out of inactivity. Net inflows are generally close to zero, except during the Great Recession, when they became very positive. This spike in net inflows into inactivity was driven by both a large increase in inflows and a substantial decline in outflows. The increase in inflows

Table 6
Demographic Characteristics of Workers by Transition Type

| Origin, Destination | Flow | Average Age | Male (share) | White (share) | Born US (share) |
| :--- | :--- | :--- | :---: | :---: | :---: |
| Ineligibility: |  |  |  |  |  |
| Inactivity | $0 \_1$ | 21 | .521 | .221 | .710 |
| Bottom 20\% | $0 \_2$ | 19 | .481 | .336 | .886 |
| Middle 60\% | $0 \_3$ | 21 | .560 | .328 | .730 |
| Top 20\% | $0 \_4$ | 33 | .791 | .279 | .127 |
| Inactivity: |  |  |  |  |  |
| Ineligibility | $1 \_0$ | 68 | .493 | .743 | .795 |
| Inactivity | $1 \_1$ | 48 | .504 | .585 | .690 |
| Bottom 20\% | $1 \_2$ | 35 | .478 | .520 | .825 |
| Middle 60\% | $1 \_3$ | 38 | .580 | .582 | .765 |
| Top 20\% | $1 \_4$ | 44 | .730 | .701 | .737 |
| Bottom 20\%: |  |  |  |  |  |
| Ineligibility | $2 \_0$ | 64 | .525 | .784 | .888 |
| Inactivity | $2 \_1$ | 39 | .484 | .576 | .831 |
| Bottom 20\% | $2 \_2$ | 34 | .421 | .566 | .891 |
| Middle 60\% | $2 \_3$ | 33 | .464 | .556 | .850 |
| Top 20\% | $2 \_4$ | 41 | .667 | .680 | .778 |
| Middle 60\%: |  |  |  |  |  |
| Ineligibility | $3 \_0$ | 66 | .560 | .785 | .858 |
| Inactivity | $3 \_1$ | 45 | .548 | .659 | .806 |
| Bottom 20\% | $3 \_2$ | 39 | .468 | .604 | .846 |
| Middle 60\% | $3 \_3$ | 41 | .465 | .659 | .844 |
| Top 20\% | $3 \_4$ | 41 | .608 | .723 | .842 |
| Top 20\%: |  |  |  |  |  |
| Ineligibility | $4 \_0$ | 68 | .768 | .861 | .855 |
| Inactivity | $4 \_1$ | 51 | .699 | .771 | .821 |
| Bottom 20\% | $4 \_2$ | 51 | .659 | .759 | .859 |
| Middle 60\% | $4 \_3$ | 46 | .626 | .751 | .861 |
| Top 20\% | $4 \_4$ | 47 | .667 | .776 | .855 |

Note.-The estimates are based on the authors' calculations using characteristics of workers who transition into and out of the eligible-workers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories.
is seen for every category except for the top of the distribution. The decrease in outflows during the Great Recession is primarily due to a reduction in workers moving to jobs in the bottom and middle of the earnings distribution; however, these flows return to their prerecession levels fairly quickly. The net result is a roughly symmetric increase in gross outflows and a decrease in gross inflows. Without either a very large relative increase in gross outflows or a relatively large decrease in gross inflows, little progress can be made toward reducing the almost 13 million person increase in the number of eligible workers with no reported earnings during the Great Recession.
Figure 10 plots the flows into and out of the bottom $20 \%$ of the earnings distribution. Compared with some of the other categories, the counts for the bottom $20 \%$ are relatively stable. The transitions show large changes

| $\begin{aligned} & 6,000,000 \\ & 5,000,000 \end{aligned}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
| 4,000,000 |  |  |  |  |  |  |  |  |  |
| $3,000,000$ |  |  |  |  |  |  |  |  |  |
| 2,000,000 2005 2007 2000 |  |  |  |  |  |  |  |  |  |
| 2,250,000 |  |  |  |  |  |  |  |  |  |
|  | 1_0: Outflows from Inactivity 2_0: Outflows from Bottom $20 \%$ <br> 3_0: Outflows from Middle 60\% 4_0: Outflows from Top 20\% |  |  |  |  |  |  |  |  |
| 1,500,000 |  |  |  |  |  |  |  |  |  |
| 750,000 |  |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |  |
|  | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 |
|  |  |  |  |  |  |  |  |  |  |
| 2,250,000 |  |  |  |  |  |  |  |  |  |
| 1,500,000 $\square \bigcirc 0$ 1. Inflows to Inactivity 0 3. Inflows to Middle $60 \%$ |  | 0_1: Inflows to Inactivity <br> 0_3: Inflows to Middle 60\% <br> 0_2: Inflows to Bottom 20\% 0 0_4: Inflows to Top 40\% |  |  |  |  |  |  |  |
| 750,000 |  |  |  |  |  |  |  |  |  |
| 0 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 |

Fig. 8.-Flows into and out of the eligible-workers frame. Estimates are based on the authors' calculations using transitions into and out of the eligible-workers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories. A color version of this figure is available online.

FIg. 9.-Flows into and out of inactivity. Estimates are based on the authors' calculations using transitions into and out of the eligible-
workers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories. A color version of this figure is available online.

Fig. 10.-Flows into and out of the bottom $20 \%$ of the earnings distribution. Estimates are based on the authors' calculations using transitions into and out of the eligible-workers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories. A color version of this figure is available online.

- Gross Outflows
$\cdots$

18,000,000
16,000,000
14,000,000
12,000,000
10,000,000
9,000,000
6,750,000
4,500,000
2,250,000
0


## $9,000,000$ $6,750,000$ $4,500,000$ $2,250,000$

Fig. 11.-Flows into and out of the middle $60 \%$ of the earnings distribution. Estimates are based on the authors' calculations using tranbetween the earnings categories. A color version of this figure is available online.
occurring during the Great Recession. Outflows increased to nonemployment, while outflows to the middle of the earnings distribution fell (fewer workers moving up). At the same time, inflows from nonemployment decreased and inflows from the middle of the distribution increased. Workers who moved to nonemployment are being replaced (not at the job level but in terms of earnings) with workers from the middle of the distribution.

Figure 11 shows the flows into and out of the middle $60 \%$ of the earnings distribution. There is a large decrease in net inflows in 2009. This is largely due to an increase in the outflows of workers to the bottom $20 \%$ and nonemployment and a decrease in workers moving up from the bottom $20 \%$. Although net inflows turn positive again after the Great Recession, these inflows are not large enough to halt the decreasing share of earnings accruing to workers in the middle $60 \%$. There has also been a decline in workers moving from the middle to the top $20 \%$, which peaked in 2007, implying a decrease in upward earnings mobility. A decrease in workers moving from the top to the bottom is also present, implying a decrease in downward earnings mobility. Postrecession, workers in the middle are more likely to stay in the middle, and workers at the top are more likely to stay at the top.

Figure 12 plots the flows into and out of the top $20 \%$ of the earnings distribution. Notice that there is a strong net inflow of workers to the top $20 \%$ prior to the Great Recession and a decrease during the recession. Although net inflows turn positive again in 2012, they do not return to the heights seen prior to the Great Recession. Workers at the top are relatively disconnected from the rest of the earnings distribution. The only substantial flows are to and from the middle, but the magnitudes of both of these flows appear to be declining after the recession. ${ }^{44}$

Overall, mobility occurs most often between neighboring parts of the earnings/inactivity distribution. It is relatively rare to jump more than one earnings/inactivity category. For example, moving from the bottom to the top is a relatively rare event, while moving from the bottom to the middle is a common transition. ${ }^{45}$

## V. Firm Differences in Worker Earnings and Mobility

## A. The Worker-Firm Earnings Decomposition

Having established (1) that the eligible-workers frame is more likely to be representative of the entire US labor market than uncorrected administrative

[^18]
Fig. 12.-Flows into and out of the top $20 \%$ of the earnings distribution. Estimates are based on the authors' calculations using transitions into and out of the eligible-workers frame used to construct the earnings distributions, including inactive workers, and transitions between the earnings categories. A color version of this figure is available online.
record frames and (2) that it is complete and suitable for studying changes in the entire earnings distribution, including the movements into and out of activity, we now turn to the role of the employer as a source of earnings inequality. We use the statistical approach introduced to the labor economics literature in Abowd et al. (1999).

To understand the role of firms in the rise in earnings inequality, we estimate the following AKM model for the eligible-worker sample:

$$
\begin{equation*}
\ln y_{i j t}=x_{i t} \beta+\theta_{i}+\psi_{j}+\varepsilon_{i j t}, \tag{3}
\end{equation*}
$$

where $y_{i j t}$ is real annual earnings for worker $i=1, \ldots, 200,665,944 \mathrm{em}-$ ployed at firm $j=1, \ldots, 14,645,104$ in year $t=2004, \ldots, 2013 .{ }^{46}$ On the right-hand side we include $\theta_{i}$, the fixed person effect; $\psi$, the fixed firm effect; and the vector $x_{i t}$, which includes a constant demographic characteristic interacted with actual labor force experience, labor force attachment variables, date-regime variables, and aggregate labor market conditions.

During the process of converting job-level firm effect estimates to personlevel firm effect estimates, we move back and forth between dollars (levels) and logarithms as appropriate. We estimate equation (3) in semilogarithmic form due to the approximately lognormal conditional distribution of the dependent variable. However, a semilog specification returns estimated firm effects showing the log points of earnings attributable to the employer (approximately proportional for small effects). To combine the estimated joblevel firm effects for workers who have multiple employers during the year into a single person-level firm effect, the relative firm effects must be converted to dollar values. For example, suppose we have a worker who earns $\$ 10,000$ at job 1 and $\$ 50,000$ at job 2, with fixed firm effects of 0.2 and 0.1 , respectively, in logs. Although the estimated firm effect is twice as large in job 1 , the earnings are only $20 \%$ of the earnings in job 2 . To account for the earnings differences across jobs, we convert the estimated firm effects to dollars, aggregate the dollar amounts, and then convert the dollar value of the person and firm components back to logs.

First, we isolate the real dollar value of the firm component of earnings for a given job in a given year. Specifically, for individual $i$ working at firm $j$ in year $t$, the firm component of earnings $y_{i j t}$ is defined as

$$
\begin{equation*}
y_{i j t}^{\mathrm{firm}}=y_{i j t}-\exp \left(\ln y_{i j t}-\widehat{\psi}_{j}\right) . \tag{4}
\end{equation*}
$$

[^19]We define the nonfirm component of earnings $y_{i j t}$ as the residual from the above equation:

$$
\begin{equation*}
y_{i j t}^{\mathrm{nonfirm}}=y_{i j t}-y_{i j t}^{\mathrm{firm}} \tag{5}
\end{equation*}
$$

Aggregating across jobs for each worker gives a decomposition of total annual earnings into two person-level components:

$$
\begin{align*}
\sum_{j} y_{i j t} & =\sum_{j} y_{i j t}^{\mathrm{firm}}+\sum_{j} y_{i j t}^{\mathrm{nonfirm}}  \tag{6}\\
y_{i t}^{\mathrm{total}} & =y_{i t}^{\mathrm{firm}}+y_{i t}^{\mathrm{nonfirm}}
\end{align*}
$$

The person-level log firm component is recovered by taking the difference between the log of person-level earnings and the log of the nonfirm component:

$$
\begin{equation*}
\ln y_{i t}^{\text {firm }}=\ln y_{i t}^{\text {total }}-\ln y_{i t}^{\text {nonfirm }} \tag{7}
\end{equation*}
$$

Continuing the example above, the total earnings for the hypothetical worker are $\$ 60,000$. After applying equations (4)-(6), the estimated dollar value of the firm component across all jobs is $\$ 6,571$, and the estimated nonfirm component is $\$ 53,429$. Applying equation (7) results in a log firm component of 0.116 . Conceptually, the resulting person-level firm component is very similar to taking the earnings-weighted average of the log firm components.

We also extract a component of log earnings that we can associate with the worker's skill type. This component consists of the constant, which has been standardized to a year with average unemployment and full-year, fulltime work; the estimated effects associated with labor force experience; and the estimated person effect. Thus, the skill component can represent the log earnings associated with the annual wage rate for a worker with a given person effect and labor experience. ${ }^{47}$

We calculated both dollar and log estimates of the firm and nonfirm earnings components. We calculated only the log component for estimating the skill type. We used the skill component, which is logarithmic, to classify workers by bottom $20 \%$, middle $60 \%$, and top $20 \%$ of the skill distribution. When referencing the discrete distribution of the skill component, we refer to skill types. When referencing the value, we refer to the skill component of log earnings.

We similarly classified the firm component into three bins, and we also used the firm and nonfirm components to decompose earnings in the bottom, middle, and top bins. When referencing the discrete distribution of the firm component, we refer to firm types. We do not classify the cells of the

[^20]discrete distribution of the nonfirm component of earnings. In all cases, distributions were estimated using the pooled person-level observations over the 2004-13 period. See table 7 for the minimum, maximum, and average log values of all three components.

Our approach has three main benefits. First, all workers at a firm with only one job during the year are placed in the same firm-type bin. Second, the total earnings of the worker do not affect the firm-type bin assignment. Third, classifying the workers by their skill bin rather than the nonfirm bin controls for the state of the labor market and labor force attachment as well as eliminates the influence of the AKM residual. Using the log values of each component also allows us to study all possible mixes of worker skill types. If we had used the dollar-value bin assignments, the highest-paid workers would have dominated the top and bottom categories for each estimated component. For example, a worker with a very small $\log$ firm effect but high earnings would likely dominate a low earning worker with a large log firm effect.

Comparing the earnings bins in table 2 with the firm and nonfirm component bins in table 7, notice that, except for a relatively small number of extreme values, the distribution of log earnings and $\log$ nonfirm earnings component are similar within bins. This result is due to the small relative

Table 7
Statistics for Firm, Nonfirm, and Skill Bins

|  | 2. Bottom 20\% | 3: Middle 60\% | 4: Top 20\% |
| :---: | :---: | :---: | :---: |
|  | Firm-Type Bins |  |  |
| Log firm: |  |  |  |
| Minimum | -. 945 | -. 374 | . 556 |
| Mean | -. 716 | . 113 | . 807 |
| Maximum | -. 374 | . 556 | 13.190 |
|  | Nonfirm-Type Bins |  |  |
| Log nonfirm: |  |  |  |
| Minimum | -4.499 | 8.922 | 10.480 |
| Mean | 7.708 | 9.803 | 10.980 |
| Maximum | 8.922 | 10.480 | 19.590 |
|  | Skill-Type Bins |  |  |
| Log skill: |  |  |  |
| Minimum | -16.960 | 6.255 | 7.203 |
| Mean | 5.898 | 6.695 | 7.679 |
| Maximum | 6.255 | 7.203 | 17.460 |

Note.-The estimates are based on the authors' calculations using the decomposition of person-level log earnings into firm/nonfirm components that sum to log total earnings. Firm-type and nonfirm-type bins are formed for each component separately using the logarithmic scale. The skill component, also on a logarithmic scale, uses only the constant, person effect, and actual labor force experience effects as the basis for the skill-type bins. Distributions are based on the pooled person-level observations for the eligible-workers frame from 2004 to 2013. Statistics are rounded to four significant digits.
magnitude of the $\log$ firm component. ${ }^{48}$ In spite of their relatively small magnitude in logs, the firm components can have a substantial effect, conditional on the size of the nonfirm component of earnings. The log firm component is about -0.716 for the typical firm in the bottom of the firm compensation distribution, 0.113 in the middle, and 0.807 at the top. All statistics are worker duration-weighted averages, implying that a worker at the middle-type firm receives about $11 \%$ more than would be expected given the worker's characteristics. In comparison, the difference between the average log earnings value and the average log nonfirm earnings component for workers in the middle is $0.135(=9.938-9.803)$, which is very similar to the 0.113 estimated for the worker duration-weighted average log firm component. Although this comparison is not a true worker-level comparison, it should be similar given that most workers are in the same nonfirm-type and overallearnings bins.

There is some evidence of worker sorting. Taking the difference between the average log earnings for each overall-earnings bin (table 2) and the average log nonfirm components for the same nonfirm bin (table 2) shows that workers at the bottom of the overall-earnings distribution and the bottom of the nonfirm component distribution tend to work in lower-paying firms (7.473-7.708 $=-0.235$ ) compared with workers at the top (11.236$10.976=0.260$ ).

Consider the magnitude of the average firm effect for each firm type and its potential effect on workers in different parts of the nonfirm component distribution. For example, the typical worker at the bottom of the nonfirm component distribution has average log earnings of 7.708. If this worker were employed at a firm in the middle of the firm component distribution, his log earnings would be greater by about 0.113, which is not enough to move him to the middle of the overall-earnings distribution (7.708 + $0.113=7.821<9.938$ ). Even if this worker were able to transition to a firm at the top of the firm component distribution, ceteris paribus, his log earnings would be greater by $0.694(=0.807-0.113) \log$ points. The resulting log earnings of $8.515(=7.708+0.807)$ would still not be large enough to move the worker to the middle overall-earnings bin. In comparison, for a worker in the top of the nonfirm component distribution, moving from a middle to a top firm results in an earnings increase large enough for the worker to transition from the middle to the top of the overall-earnings distribution $(10.976+0.807=11.783>11.236)$. Although the relative effect

[^21]is the same, the dollar value of the effect of working at a high-paying firm increases the greater a worker's nonfirm component of earnings is.

Table 6 shows characteristics of workers associated with each of the 24 possible earnings and inactivity transitions. Given that the overwhelming majority of workers are in the same bin of the overall earnings and nonfirm component distributions, the characteristics of the workers in each corresponding nonfirm component bin will largely be the same. In table 8, we show the characteristics of firms across each of the three firm-type categories. There are clear differences in the industry distribution by where the firm lies in the firm component distribution. Low-paying firms are highly concentrated in Trade, Transportation, and Utilities and Leisure and Hospitality, with more than $50 \%$ of workers at low-paying firms in these two industries. Firms in the middle of the pay distribution are not nearly as concentrated by industry, but nevertheless workers in these firms are prevalent

Table 8
Firm Characteristics by Position in the Firm Component Distribution

| Characteristic | Bottom | Middle | Top |
| :--- | ---: | ---: | ---: |
| Industry distribution (\%): |  |  |  |
| Natural Resources/Mining | .012 | .011 | .023 |
| Construction | .012 | .060 | .075 |
| Manufacturing | .014 | .104 | .178 |
| Trade, Transportation, and Utilities | .246 | .211 | .140 |
| Information | .017 | .016 | .050 |
| Finance | .017 | .057 | .119 |
| Professional and Business Services | .118 | .123 | .212 |
| Education and Health | .209 | .276 | .074 |
| Leisure and Hospitality | .290 | .070 | .006 |
| Other Services | .048 | .031 | .021 |
| State/Local Government | .017 | .041 | .062 |
| Federal Government | .000 | .001 | .041 |
| Firm age: |  |  |  |
| Mean | 20.988 | 22.700 | 24.760 |
| Standard deviation | 9.670 | 9.419 | 9.882 |
| 25th percentile | 10 | 13 | 17 |
| Median | 24 | 27 | 29 |
| 75th percentile | 32 | 32 | 33 |
| Firm size: |  |  |  |
| 10th percentile | 6 | 8 | 11 |
| 25th percentile | 26 | 40 | 118 |
| Median | 330 | 502 | 2,359 |
| 75th percentile | 9,433 | 9,088 | 20,991 |
| 90th percentile | 73,330 | 68,535 | 64,448 |

[^22]in Trade, Transportation, and Utilities; Education and Health; and Manufacturing. Somewhat surprisingly, except for Leisure and Hospitality and Finance, the distribution of workers in high-paying firms across industries is relatively diffuse. Most industries have a substantial number of workers in high-paying firms, implying that, except for Leisure and Hospitality, it is not necessary to change industries to work at a high-paying firm. As found in other studies, low-paying firms tend to be both younger and smaller than high-paying firms (Haltiwanger et al. 2012, fig. 7).

## B. Earnings and Mobility by Person and Firm Type

In this section, we use the AKM decomposition to explore how the three types of workers (bottom, middle, and top of the skill-type distribution) sort into the three types of firms (bottom, middle, and top of the firm-type distribution). The results for each worker type are presented separately. Tables 9,10 , and 11 present outcomes for workers in the bottom, middle, and top bins of the skill-type distribution, respectively.
The tables were created as follows. Bin types are based on the previous year's data, that is, year $t-1$ classifications. Beginning in 2004 and ending in 2012, for every year that an eligible worker has positive earnings a single observation is added to one of the three tables. The appropriate table classification for each observation is determined by the skill type of the worker for that year, which can vary over time as workers accumulate experience. Within each skill type, the earnings record is further classified based on the firm type, resulting in each earnings observation being classified into one of nine possible cells. ${ }^{49}$ Within each of the skill-type $\times$ firm-type cells, we break down the results by the three possible overall-earnings outcomes (bottom, middle, and top). There are, thus, 27 cells for which we present information on the number of workers, average earnings for the previous year $t-1$, and average earnings for the current year $(t)$ by flow type. ${ }^{50}$

To fix ideas, we will take a detailed look at two rows in table 9. To be recorded in this table, the person must have been in the bottom (lowest) bin of the skill-type distribution in the previous year, that is, $t-1$.

Consider the first row of the table. This row is in the panel labeled "Bottom Firm," indicating that this person is employed at a firm in the bottom bin of the firm-type distribution in $t-1$. Persons in this row are also in the

[^23]bottom bin of the overall-earnings distribution in year $t-1$, and 0.782 is the share of such persons relative to those in the middle or top of the overallearnings distribution. The flow labeled 2_0 is the movement from the bottom of the overall-earnings distribution (bin 2) to the ineligible (bin 0 ); that is, this is the flow out of the frame for persons at the bottom of the overallearnings distribution. There were, on average, 39,565 such persons each previous year $(t-1)$. They represent $0.7 \%$ of the flows from bin 2 of the overall-earnings distribution for low-skill workers in bottom-paying firms. Average earnings in $t-1$ were $\$ 1,921$, of which $-\$ 2,285$ are attributed to the firm component of our decomposition and \$4,207 are attributed to the nonfirm component of our decomposition. There were no earnings in the current year $(t)$ because the person has moved out of the frame in $t$.

Next consider the row labeled "Middle" in the "All Earnings" column in the "Middle Firm" panel with a 3_3 flow. All persons in this row were, once again, at the bottom of the skill component distribution in year $t-1$. Of all low-skill persons, $60 \%$ are employed by a firm in the middle of the firmtype distribution. Of all low-skill persons employed at middle firm types in year $t-1$, the proportion 0.608 were in the middle of the overall-earnings distribution. Among such persons, the 3_3 row shows those who remain in the middle of the overall-earnings distribution in the current year, $t$, of which there were, on average, $8,507,780$ in the nine pairs of years for which the table was constructed. Those who stayed in the middle of the overallearnings distribution represented $82.4 \%$ of all persons who were in the middle of the overall-earnings distribution, in the low-skill bin, and in a middlepaying firm in year $t-1$, on average. In year $t-1$, their earnings averaged $\$ 17,361$, of which $\$ 2,337$ are attributed to the firm component of our decomposition and $\$ 15,024$ are attributed to the nonfirm component of our decomposition. In the current year, $t$, average earnings were $\$ 18,013$, of which $\$ 2,619$ are associated with the firm component and $\$ 15,394$ are associated with the nonfirm component.

We use these tables to investigate worker sorting directly by looking at the interaction of the skill and firm type for each worker-year-earnings observation. If there were no sorting, the distribution of earnings observations across firm types would be similar for all three tables because outcomes would be unaffected by which part of the skill-type distribution an individual occupied, given his place in the overall-earnings distribution. This hypothesis is clearly not supported by the data and forms the basis of our major conclusion that the influence of the firm operates through channels that are, at least in part, different from the channels that intermediate the skilltype effect. For example, again using table 9 showing the bottom of the skill-type distribution, about $27 \%$ of the earnings observations are in firms at the bottom of the firm-type distribution, $60 \%$ are in firms of the middle type, and only $13 \%$ are in top firms. By comparison, tables 10 and 11 show that persons in the middle and top of the skill-type distributions are much

Table 9
Earnings Associated with Flows by Firm Bin for Low-Skill Persons

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (27\%) |  |  |  |  |  |  |  |
| Bottom (.782): |  |  |  |  |  |  |  |  |
| 2_0 | 39,565 | . 7 | 1,921 | -2,285 | 4,207 |  |  |  |
| 2_1 | 1,102,440 | 18.9 | 1,014 | -1,039 | 2,053 |  |  |  |
| 2_2 | 3,713,490 | 63.6 | 2,282 | -2,492 | 4,774 | 2,562 | -2,262 | 4,824 |
| 2_3 | 978,706 | 16.8 | 3,398 | -3,236 | 6,634 | 10,487 | -3,913 | 14,400 |
| 2_4 | 1,326 | . 0 | 1,977 | -4,694 | 6,672 | 80,726 | 25,927 | 54,800 |
| Middle (.217): |  |  |  |  |  |  |  |  |
| 3-0 | 5,655 | . 3 | 10,686 | -10,132 | 20,818 |  |  |  |
| 3_1 | 32,834 | 2.0 | 10,298 | -9,484 | 19,782 |  |  |  |
| 3_2 | 380,336 | 23.5 | 9,359 | -8,313 | 17,673 | 3,771 | -3,133 | 6,904 |
| 3_3 | 1,194,533 | 73.9 | 12,342 | -10,417 | 22,760 | 13,660 | -8,628 | 22,289 |
| 3_4 | 2,705 | . 2 | 31,037 | -32,962 | 63,999 | 58,165 | -34,136 | 92,301 |
| Top (.001): |  |  |  |  |  |  |  |  |
| 4_0 | 20 | . 3 | 100,000 | -130,000 | 230,000 |  |  |  |
| 4_1 | 160 | 2.1 | 66,408 | -85,919 | 152,326 |  |  |  |
| 4_2 | 362 | 4.6 | 180,230 | -163,472 | 343,702 | 2,486 | -6,377 | 8,863 |
| 4_3 | 2,151 | 27.6 | 59,430 | -67,891 | 127,321 | 33,563 | -33,499 | 67,062 |
| 4_4 | 5,106 | 65.5 | 66,745 | -74,157 | 140,902 | 67,457 | $-64,741$ | 132,199 |
|  | Middle Firm (60\%) |  |  |  |  |  |  |  |
| Bottom (.381): |  |  |  |  |  |  |  |  |
| 2_0 | 65,494 | 1.0 | 2,447 | 2 | 2,445 |  |  |  |
| 2_1 | 1,428,036 | 22.1 | 1,749 | 1 | 1,748 |  |  |  |
| 2_2 | 3,411,867 | 52.7 | 2,781 | -209 | 2,990 | 2,719 | -505 | 3,225 |
| 2_3 | 1,566,180 | 24.2 | 3,726 | -167 | 3,893 | 11,739 | 438 | 11,302 |
| 2_4 | 2,684 | . 0 | 2,981 | 252 | 2,729 | 69,808 | 27,963 | 41,845 |
| Middle (.608): |  |  |  |  |  |  |  |  |
| 3 -0 | 46,878 | . 5 | 12,749 | 1,501 | 11,249 |  |  |  |
| 3_1 | 310,560 | 3.0 | 11,957 | 1,722 | 10,235 |  |  |  |
| 3_2 | 1,396,266 | 13.5 | 11,989 | 725 | 11,263 | 3,367 | -386 | 3,752 |
| 3-3 | 8,507,780 | 82.4 | 17,361 | 2,337 | 15,024 | 18,013 | 2,619 | 15,394 |
| 3_4 | 60,049 | . 6 | 35,329 | 7,277 | 28,052 | 55,148 | 13,567 | 41,580 |
| Top (.011): |  |  |  |  |  |  |  |  |
| 4_0 | 289 | . 2 | 73,365 | 14,053 | 59,313 |  |  |  |
| 4_1 | 1,586 | . 9 | 72,382 | 12,255 | 60,128 |  |  |  |
| 4_2 | 5,942 | 3.2 | 67,356 | 7,642 | 59,714 | 1,985 | -454 | 2,439 |
| 4_3 | 47,624 | 25.7 | 55,476 | 10,714 | 44,761 | 34,993 | 6,711 | 28,282 |
| 4_4 | 130,216 | 70.1 | 62,989 | 12,797 | 50,193 | 63,549 | 13,399 | 50,150 |
|  | Top Firm (13\%) |  |  |  |  |  |  |  |
| Bottom (.143): |  |  |  |  |  |  |  |  |
| 2_0 | 8,510 | 1.7 | 2,456 | 1,367 | 1,089 |  |  |  |
| 2_1 | 176,522 | 34.3 | 2,131 | 1,203 | 928 |  |  |  |
| 2 _2 | 207,481 | 40.4 | 2,979 | 1,642 | 1,336 | 2,711 | 920 | 1,791 |
| 2_3 | 119,756 | 23.3 | 3,749 | 2,039 | 1,710 | 15,047 | 6,912 | 8,135 |
| 2_4 | 1,650 | . 3 | 3,051 | 1,820 | 1,232 | 109,852 | 63,556 | 46,296 |

Table 9 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| Middle (.771): |  |  |  |  |  |  |  |  |
| 3_0 | 12,848 | . 5 | 18,789 | 10,749 | 8,040 |  |  |  |
| 3_1 | 128,415 | 4.6 | 16,324 | 9,505 | 6,820 |  |  |  |
| 3_2 | 209,939 | 7.6 | 17,926 | 9,809 | 8,117 | 2,911 | 914 | 1,997 |
| 3_3 | 2,351,400 | 84.6 | 24,984 | 13,686 | 11,297 | 25,168 | 13,437 | 11,731 |
| 3_4 | 76,365 | 2.7 | 36,786 | 21,709 | 15,077 | 56,997 | 33,932 | 23,065 |
| Top (.087): |  |  |  |  |  |  |  |  |
| 4_0 | 677 | . 2 | 88,542 | 65,161 | 23,381 |  |  |  |
| 4_1 | 4,682 | 1.5 | 93,519 | 62,575 | 30,944 |  |  |  |
| 4_2 | 11,856 | 3.8 | 82,512 | 49,460 | 33,051 | 1,976 | 377 | 1,599 |
| 4_3 | 63,883 | 20.4 | 59,192 | 36,042 | 23,151 | 33,313 | 19,085 | 14,228 |
| 4_4 | 232,083 | 74.1 | 72,919 | 47,838 | 25,081 | 73,785 | 48,162 | 25,624 |

[^24]less likely to be employed at firms in the bottom type ( $17 \%$ and $21 \%$, respectively) and are much more likely to be employed at top firms ( $21 \%$ and $25 \%$, respectively).

Focusing on each skill type, we start with the earnings observations for low-skill types in table 9 . For workers at the bottom of the skill-type distribution, working at a higher-paying firm has two advantages: higher earnings than otherwise and a greater chance of moving to a higher bin in the overall-earnings distribution. For example, a worker at the bottom of the skill-type and overall-earnings distributions has a probability of moving to the middle of the overall-earnings distribution of $16.8 \%$ at a low-paying firm, $24.2 \%$ at a middle-paying firm, and $23.3 \%$ at a high-paying firm. Prior to the 2 _ 3 transition, the average low-skill worker at a low-, middle-, and high-paying firm earns $\$ 3,398, \$ 3,726$, and $\$ 3,749$, respectively. ${ }^{51}$ After the
${ }^{51}$ Notice that the nonfirm component of earnings declines as we move up the firm-type distribution. Although it is unclear exactly which covariate is primarily responsible for this decline (perhaps weeks worked), the impact of working at a higher-paying firm would be much greater if the person component of earnings were the same across firm types.

Table 10
Earnings Associated with Flows by Firm Bin for Middle-Skill Persons

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (17\%) |  |  |  |  |  |  |  |
| Bottom (.444): |  |  |  |  |  |  |  |  |
| 2_0 | 36,376 | . 6 | 2,766 | -4,188 | 6,953 |  |  |  |
| 2_1 | 1,413,148 | 21.9 | 1,828 | -1,999 | 3,827 |  |  |  |
| 2_2 | 3,101,345 | 48.1 | 2,774 | -3,688 | 6,462 | 3,056 | -3,388 | 6,444 |
| 2_3 | 1,894,531 | 29.4 | 3,540 | -3,808 | 7,348 | 11,709 | -6,015 | 17,725 |
| 2_4 | 6,629 | . 1 | 2,514 | -4,166 | 6,680 | 71,419 | 15,598 | 55,821 |
| Middle (.547): |  |  |  |  |  |  |  |  |
| 3-0 | 31,137 | . 4 | 12,442 | -11,801 | 24,242 |  |  |  |
| 3-1 | 212,893 | 2.7 | 11,397 | -10,634 | 22,031 |  |  |  |
| 3_2 | 983,862 | 12.4 | 10,788 | -10,662 | 21,450 | 3,785 | -3,651 | 7,436 |
| 3_3 | 6,669,365 | 84.0 | 15,820 | -14,127 | 29,946 | 16,803 | -12,701 | 29,505 |
| 3_4 | 45,779 | . 6 | 33,527 | -32,569 | 66,096 | 57,183 | -33,647 | 90,830 |
| Top (.008): |  |  |  |  |  |  |  |  |
| 4_0 | 195 | . 2 | 69,394 | -89,283 | 158,677 |  |  |  |
| 4_1 | 1,370 | 1.1 | 74,112 | -139,818 | 213,929 |  |  |  |
| 4_2 | 1,950 | 1.6 | 68,735 | -88,619 | 157,355 | 2,844 | -5,364 | 8,209 |
| 4_3 | 30,542 | 24.9 | 56,942 | -59,886 | 116,828 | 35,086 | -31,411 | 66,497 |
| 4_4 | 88,637 | 72.2 | 63,707 | -64,986 | 128,693 | 64,695 | $-60,302$ | 124,997 |
|  | Middle Firm (62\%) |  |  |  |  |  |  |  |
| Bottom (.130): |  |  |  |  |  |  |  |  |
| 2_0 | 44,834 | . 7 | 3,037 | 27 | 3,010 |  |  |  |
| 2_1 | 1,917,160 | 28.5 | 2,653 | 10 | 2,642 |  |  |  |
| 2_2 | 2,264,104 | 33.6 | 3,077 | -231 | 3,308 | 2,992 | -803 | 3,795 |
| 2_3 | 2,485,434 | 36.9 | 3,706 | -149 | 3,855 | 14,551 | 398 | 14,152 |
| 2_4 | 19,469 | . 3 | 3,366 | 427 | 2,939 | 63,885 | 21,915 | 41,969 |
| Middle (.802): |  |  |  |  |  |  |  |  |
| 3_0 | 124,637 | . 3 | 19,293 | 1,958 | 17,335 |  |  |  |
| 3_1 | 1,502,717 | 3.6 | 15,071 | 2,193 | 12,877 |  |  |  |
| 3-2 | 2,535,882 | 6.1 | 15,344 | 1,061 | 14,283 | 3,442 | -487 | 3,929 |
| 3_3 | 36,185,391 | 87.4 | 24,165 | 3,268 | 20,897 | 24,688 | 3,412 | 21,276 |
| 3_4 | 1,075,334 | 2.6 | 37,532 | 8,695 | 28,837 | 54,207 | 14,489 | 39,719 |
| Top (.068): |  |  |  |  |  |  |  |  |
| 4_0 | 4,246 | . 1 | 64,346 | 14,661 | 49,686 |  |  |  |
| 4_1 | 20,143 | . 6 | 69,334 | 12,984 | 56,350 |  |  |  |
| 4_2 | 32,524 | . 9 | 64,867 | 13,923 | 50,943 | 2,927 | -123 | 3,050 |
| 4_3 | 812,972 | 23.2 | 54,592 | 12,472 | 42,120 | 36,813 | 8,389 | 28,424 |
| 4_4 | 2,636,922 | 75.2 | 61,625 | 14,644 | 46,981 | 62,511 | 15,362 | 47,149 |
|  | Top Firm (21\%) |  |  |  |  |  |  |  |
| Bottom (.036): |  |  |  |  |  |  |  |  |
| 2_0 | 7,309 | 1.2 | 3,258 | 1,763 | 1,495 |  |  |  |
| 2_1 | 243,227 | 38.9 | 3,027 | 1,642 | 1,385 |  |  |  |
| 2 2 | 156,614 | 25.1 | 3,382 | 1,834 | 1,548 | 3,114 | 625 | 2,489 |
| 2_3 | 201,902 | 32.3 | 3,825 | 2,020 | 1,804 | 19,512 | 7,872 | 11,640 |
| 2_4 | 15,593 | 2.5 | 3,681 | 2,053 | 1,628 | 64,011 | 35,748 | 28,263 |

Table 10 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| Middle (.547): |  |  |  |  |  |  |  |  |
| 3_0 | 27,268 | . 3 | 25,229 | 13,304 | 11,925 |  |  |  |
| 3-1 | 520,030 | 5.5 | 20,967 | 11,452 | 9,514 |  |  |  |
| 3-2 | 350,961 | 3.7 | 22,339 | 11,765 | 10,573 | 3,224 | 715 | 2,509 |
| 3-3 | 7,391,254 | 78.7 | 31,965 | 16,295 | 15,670 | 32,082 | 15,736 | 16,346 |
| 3_4 | 1,107,423 | 11.8 | 38,199 | 20,579 | 17,620 | 55,738 | 30,184 | 25,553 |
| Top (.417): |  |  |  |  |  |  |  |  |
| 4_0 | 9,556 | . 1 | 70,452 | 41,322 | 29,130 |  |  |  |
| 4_1 | 70,437 | 1.0 | 70,076 | 42,343 | 27,733 |  |  |  |
| 4_2 | 61,125 | . 9 | 72,097 | 41,507 | 30,590 | 2,881 | 939 | 1,942 |
| 4_3 | 899,132 | 12.6 | 57,986 | 31,890 | 26,095 | 35,291 | 18,151 | 17,140 |
| 4_4 | 6,115,576 | 85.5 | 67,457 | 38,800 | 28,656 | 68,906 | 39,504 | 29,402 |

Note.-See table 9.
transition, the average low-skill worker at a low-, middle-, and high-paying firm earns $\$ 10,487, \$ 11,739$, and $\$ 15,047$, respectively. Most of the additional increase in earnings for workers employed at a top-paying employer in the previous year is due to working at a top-paying employer in the next year.

Table 10 supports a similar conclusion. Middle-skilled workers in the bottom of the overall-earnings distribution also have a greater chance of moving to the middle of the earnings distribution the higher the firm type for which they work. When they transition, their current-year earnings will also be greater the higher the firm type for which they work. The vast majority ( $62 \%$ ) of workers in the middle of the skill-type distribution are employed at middle-paying firms. The next most prevalent outcomes for such workers are employment at top- and bottom-paying firms, $21 \%$ and $17 \%$, respectively. However, in spite of the majority of earnings observations being in the middle of the overall-earnings distribution, average earnings differ substantially across firm types. A middle-skill worker in the middle (bin 3) of the overall-earnings distribution who stays in bin 3 of the overall distribution (a 3_3 flow) at a bottom-type firm has $t-1$ earnings of $\$ 15,820$, a middle-skill worker in a middle-type firm has $t-1$ earnings of $\$ 24,165$, and a middle-skill worker at a top firm has earnings of $\$ 31,965$. Most of the difference is due to a larger firm effect, although the nonfirm component declines as a middle-skill person is found in increasing firm types, giving back some of the gains. Another benefit of finding employment at a highpaying firm is a greater probability of moving to the top of the earnings distribution. For middle-skill workers in the middle bin of the overall-earnings distribution in the previous year, the relevant comparisons are as follows.

Table 11
Earnings Associated with Flows by Firm Bin for High-Skill Persons

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (21\%) |  |  |  |  |  |  |  |
| Bottom (.104): |  |  |  |  |  |  |  |  |
| 2_0 | 10,534 | 1.8 | 2,773 | -8,174 | 10,948 |  |  |  |
| 2_1 | 280,788 | 46.7 | 2,249 | -3,701 | 5,950 |  |  |  |
| 2 2 | 176,404 | 29.3 | 2,907 | -11,164 | 14,071 | 2,982 | -10,511 | 13,493 |
| 2_3 | 128,775 | 21.4 | 3,591 | -7,554 | 11,145 | 15,617 | -20,775 | 36,391 |
| 2_4 | 5247 | . 9 | 2,815 | -7,587 | 10,402 | 94,017 | -43,216 | 137,233 |
| Middle (.655): |  |  |  |  |  |  |  |  |
| 3_0 | 19,797 | . 5 | 20,605 | -33,443 | 54,048 |  |  |  |
| 3_1 | 160,196 | 4.2 | 18,005 | -23,558 | 41,563 |  |  |  |
| 3_2 | 129,284 | 3.4 | 17,280 | -29,586 | 46,865 | 3,576 | -7,467 | 11,043 |
| 3-3 | 3,287,634 | 87.0 | 27,830 | -35,576 | 63,405 | 28,061 | -34,972 | 63,033 |
| 3-4 | 181,857 | 4.8 | 38,233 | -46,714 | 84,946 | 57,343 | -64,656 | 121,999 |
| Top (.241): |  |  |  |  |  |  |  |  |
| 4_0 | 4,283 | . 3 | 94,022 | -135,507 | 229,529 |  |  |  |
| 4_1 | 13,507 | 1.0 | 95,299 | -176,061 | 271,360 |  |  |  |
| 4_2 | 6,970 | . 5 | 78,069 | -144,049 | 222,118 | 3,081 | -6,682 | 9,763 |
| 4_3 | 159,557 | 11.5 | 59,330 | -78,709 | 138,039 | 36,446 | -43,579 | 80,024 |
| 4-4 | 1,205,661 | 86.7 | 80,717 | -112,912 | 193,629 | 81,938 | -110,686 | 192,624 |
|  | Middle Firm (54\%) |  |  |  |  |  |  |  |
| Bottom (.038): |  |  |  |  |  |  |  |  |
| 2_0 | 9,555 | 1.7 | 3,485 | 58 | 3,427 |  |  |  |
| 2_1 | 324,938 | 57.2 | 3,172 | 40 | 3,132 |  |  |  |
| 2 _2 | 101,070 | 17.8 | 3,231 | -99 | 3,330 | 3,150 | -770 | 3,921 |
| 2_3 | 117,605 | 20.7 | 3,745 | -40 | 3,785 | 19,859 | -1,244 | 21,103 |
| 2_4 | 14,650 | 2.6 | 3,638 | 441 | 3,198 | 76,591 | 14,464 | 62,127 |
| Middle (.378): |  |  |  |  |  |  |  |  |
| 3_0 | 30,029 | . 5 | 25,036 | 572 | 24,463 |  |  |  |
| 3_1 | 463,428 | 8.2 | 20,864 | 1,649 | 19,215 |  |  |  |
| 3-2 | 150,873 | 2.7 | 22,473 | 308 | 22,165 | 3,521 | -658 | 4,179 |
| 3_3 | 4,210,520 | 74.1 | 33,479 | -1,789 | 35,268 | 33,621 | -2,337 | 35,958 |
| 3_4 | 826,287 | 14.5 | 37,799 | 3,338 | 34,461 | 59,210 | 6,969 | 52,240 |
| Top (.585): |  |  |  |  |  |  |  |  |
| 4_0 | 23,563 | . 3 | 113,825 | 18,140 | 95,686 |  |  |  |
| 4_1 | 99,260 | 1.1 | 94,122 | 17,584 | 76,539 |  |  |  |
| 4_2 | 35,671 | . 4 | 79,444 | 11,857 | 67,587 | 3,374 | -192 | 3,566 |
| 4_3 | 769,334 | 8.7 | 62,012 | 7,288 | 54,724 | 35,502 | 2,761 | 32,741 |
| 4-4 | 7,870,823 | 89.5 | 92,507 | 15,835 | 76,673 | 93,962 | 16,259 | 77,703 |
|  | Top Firm (25\%) |  |  |  |  |  |  |  |
| Bottom (.012): |  |  |  |  |  |  |  |  |
| 2_0 | 1,600 | 1.8 | 3,762 | 2,079 | 1,683 |  |  |  |
| 2_1 | 49,575 | 56.4 | 3,674 | 2,003 | 1,671 |  |  |  |
| 2_2 | 13,208 | 15.0 | 3,763 | 2,175 | 1,588 | 3,462 | 1,162 | 2,300 |
| 2_3 | 16,128 | 18.4 | 3,986 | 2,174 | 1,812 | 21,346 | 6,827 | 14,519 |
| 2_4 | 7,364 | 8.4 | 3,888 | 2,123 | 1,765 | 94,733 | 48,125 | 46,608 |

Table 11 (Continued)

| All Earnings <br> (Share), Flow | Average <br> Count |  | Percent |  |  |  | Total | Firm | Nonfirm |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |

Note.-See table 9 .

The estimated probability of a 3_4 transition for workers in a low-paying firm is $0.6 \%$. The estimated probability of the same transition for workers in a middle-paying firm is $2.6 \%$. Finally, the estimated probability of a transition to the top of the overall-earnings distribution for middle-skill workers in a top-paying firm is $11.8 \%$.

Table 11 shows that most of the high-skill workers are also in the top of the overall-earnings distribution, since the top bin of the overall-earnings distribution shows shares of $0.241,0.585$, and 0.891 for low-, middle-, and top-type firms, respectively. There is also a substantial minority in the middle of the overall-earnings distribution. Since transitions to the top of the overall-earnings distribution (3_4) are more likely at top-paying firms ( $32.7 \%$ ) than low- or middle-paying firms ( $4.8 \%$ and $14.5 \%$, respectively), we note that once again working at such a firm offers an advantage distinct from the worker's skill type. In the high-skill category, the earnings differences between working at a middle-type compared with a bottomtype firm after making a 3_4 transition are relatively small, but the earnings gains from working at a top-paying firm are very large. While working at a top-paying firm is clearly preferred and the gains are large, a typical worker in any part of the skill distribution would also have a strong preference for working at a middle-paying rather than a bottom-paying firm. Although the dollar gains may be relatively small, the difference in earnings for bottomand middle-paying firms is significant. For example, $78 \%$ of the low-skill persons employed at a bottom-paying firm are at the bottom of the over-all-earnings distribution, while only $38 \%$ of the low-skill persons employed at a middle-paying firm are at the bottom of the overall-earnings distribution. Overall earnings within the bottom bin are not dramatically different

Table 12
Within-Firm-Type and Within-Skill-Type Inequality

| Firm Type, Flow | Bottom Skill |  | Middle Skill |  | Top Skill |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Earnings | Ratio | Earnings | Ratio | Earnings | Ratio |
| Bottom firm: |  |  |  |  |  |  |
| 2_2 | 2,282 | . 185 | 2,774 | . 175 | 2,907 | . 104 |
| 3_3 | 12,342 |  | 15,820 |  | 27,830 |  |
| 4_4 | 66,745 | 5.408 | 63,707 | 4.027 | 80,717 | 2.900 |
| Middle firm: |  |  |  |  |  |  |
| 2_2 | 2,781 | . 160 | 3,077 | . 127 | 3,231 | . 097 |
| 3-3 | 17,361 |  | 24,165 |  | 33,479 |  |
| 4_4 | 62,989 | 3.628 | 61,625 | 2.550 | 92,507 | 2.763 |
| Top firm: |  |  |  |  |  |  |
| 2_2 | 2,979 | . 119 | 3,382 | . 106 | 3,763 | . 131 |
| 3_3 | 24,984 |  | 31,965 |  | 28,736 |  |
| 4_4 | 72,919 | 2.919 | 67,457 | 2.110 | 143,296 | 4.987 |

Note.-Estimates are based on the authors' calculations using only individuals who do not change cells in the overall-earnings distribution between years $t-1$ and $t$. "Flow" indicates the bin in the overall-earnings distribution that the individual occupied. For example, $2 \_2$ means the individual was in the bottom $20 \%$ of the income distribution in both years. "Earnings" is the average earnings for the indicated firm type, skill type, and flow cell. "Ratio" is the ratio of the earnings in the indicated row to the earnings in the $3 \_3$ cell of the same firm and skill type.
in this case, but workers in the middle bin of the overall-earnings distribution have noticeably higher earnings at a middle-paying firm $(\$ 17,361)$ than at a bottom-paying firm $(\$ 12,342)$. Somewhat surprisingly, there are a relatively large number of top-skill workers at bottom- and middle-type firms. On average, these workers, especially in the middle, are employed at worsepaying firms than middle-skill workers. ${ }^{52}$

Table 12 analyzes the earnings of individuals who do not move in the earnings distribution between consecutive years by firm and skill type. This table allows us to analyze the potential effects of redistributing the skill types across firm types or redistributing the firm types across skill types. For the bottom- and middle-skill types, there is almost no advantage to being employed in a higher-paying firm type, given their place in the earnings distribution. For example, a bottom-skill person in the top $20 \%$ of the earnings distribution earns $\$ 66,745$ in a bottom-paying firm and $\$ 72,919$ in a top-paying firm. But for a top-skill person, there is a big advantage to employment in a top-paying firm: $\$ 80,717$ compared with $\$ 143,736$ when in

[^25]the top $20 \%$ of the earnings distribution. The skill pay premium for all firms is approximately the same when considering a bottom-skill as opposed to a middle-skill worker-for example, $\$ 12,342$ versus $\$ 15,820$ for a bottom firm and $\$ 17,361$ versus $\$ 24,165$ for a middle firm. This is also the case for considering a middle-skill versus a top-skill worker except for the toppaying firms, where that premium is much greater than for middle- or low-paying firms- $\$ 67,457$ versus $\$ 143,296$ for the top-paying firm compared with $\$ 61,625$ versus $\$ 92,507$ for the middle-paying firm.

## VI. Conclusion

We use administrative earnings data from the LEHD infrastructure files to analyze the role of the employer in explaining the rise in earnings inequality in the United States from 2004 to 2013. To demonstrate the importance of carefully selecting the frame and defining the earnings universe under study, we supplement these earnings data with information from a variety of sources, which we analyze to establish the validity of our final analysis of changes in the earnings distribution.

We use SSA-supplied data to identify both invalid SSNs and the potentially fraudulent use of valid SSNs. This allows us to transform the found jobs data in the all-workers frame into the designed eligible-workers frame that references a consistent population over time. When comparing the evolution of the ratios of top to bottom percentiles of the earnings distribution between the two worker frames, we find that while both frames show a decrease in earnings inequality in the late 1990 s, their patterns diverge starting in 2000. The found frame of all workers shows little to no change in the earnings inequality since 2000 . On the other hand, on removing the immigrant candidates, the designed frame of eligible workers shows a rise in inequality starting in 2000 that is robust across several measures of earnings inequality. This difference highlights the need to be mindful of the sample of workers used when interpreting results from studies of earnings inequality. Furthermore, we compare these inequality results to data from the CPS and the ACS. We find that the trends in earnings inequality observed among the eligible workers in the LEHD data are very similar to those observed among the workers expected to be covered under UI in CPS/ACS.

Our results also suggest that, unlike in previous recessions, substantial numbers of persons employed prior to the Great Recession did not return to employment even 5 years or more after the start of that recession. While previous research focused primarily on employed persons or persons in the labor force, the large and persistent decrease in the employment-topopulation ratio for all workers and for covered workers only during and after the Great Recession argues strongly for an expansion of inequality measures to include at least some inactive but eligible workers. Using our
eligible-workers frame, we have shown that such persons are attached to the labor force, as evidenced by their dynamic employment histories, but the exclusion of their inactive periods from earnings inequality measures understates the degradation at the bottom of the distribution.

Using our designed frame, we assess the role firms play in the rise in earnings inequality. We decomposed earnings into firm and nonfirm components. Using a part of the nonfirm component that relates only to measured and unmeasured individual characteristics and controls for differences in labor force attachment and macroeconomic conditions, we characterize the individuals as low-, medium-, or high-skill type. Using the firm component, we characterize the firms as low-, medium-, or high-paying firm type. Using the model for changes in the earnings distribution that we constructed for the eligible-workers frame, we analyzed the role played by the position of the worker in the skill-type and firm-type distributions. We show that a typical worker of any skill type would benefit from working at a middle-paying firm relative to a low-paying firm, but it is the workers of any skill type employed at high-paying firms who benefit the most. These individuals not only make higher earnings, they also experience an increase in the probability of moving up the earnings distribution in the following year. While we make no structural claim for this relation between the firm type and placement in the overall-earnings distribution, it is clear that the influence of firms works through channels that are not the same as those through which the effects of individual differences operate.

## Appendix A

## Additional Data Source and Methods, Tables, and Figures

In Section II we discussed the construction of our eligible-workers frame. Here we provide further details on which workers are excluded from the allworkers frame to arrive at the eligible-workers frame and how this affects the earnings coverage of LEHD compared with NIPA.

## A1. All-Workers Frame

The all-workers frame contains earnings for all jobs reported on the UI data for each date regime in the relevant years from 1990 to 2013, as noted in figure 1 and summarized in table A1 below.

Using the person-level earnings, $e_{i t}$, an estimate of annual earnings for the all-workers frame in year $t$ is calculated as follows:

$$
E_{t}^{\mathrm{AW}}=\sum_{i \in \mathrm{AW}_{t}} e_{i t},
$$

where $\mathrm{AW}_{t}$ is the set of workers in the all-workers frame in year $t$.

Table A1
Longitudinal Employer-Household Dynamics Regimes

| Count | State | First Quarter | Last Quarter | Entry Order | \% 2012Q1 QCEW <br> Employment |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Regime 1: 1990Q1 to 2013Q4, 19.35\% of 2012Q1 QCEW Employment |  |  |  |  |
| 1 | Maryland | 1985Q2 | 2014Q3 | 1 | 1.83 |
| 2 | Alaska | 1990Q1 | 2014Q3 | 2 | . 22 |
| 3 | Colorado | 1990Q1 | 2014Q3 | 3 | 1.70 |
| 4 | Idaho | 1990Q1 | 2014Q3 | 4 | . 45 |
| 5 | Illinois | 1990Q1 | 2014Q3 | 5 | 4.38 |
| 6 | Indiana | 1990Q1 | 2014Q3 | 6 | 2.19 |
| 7 | Kansas | 1990Q1 | 2013Q4 | 7 | . 98 |
| 8 | Louisiana | 1990Q1 | 2014Q2 | 8 | 1.41 |
| 9 | Missouri | 1990Q1 | 2014Q3 | 9 | 1.99 |
| 10 | Washington | 1990Q1 | 2014Q3 | 10 | 2.12 |
| 11 | Wisconsin | 1990Q1 | 2014Q3 | 11 | 2.08 |


| Regime 2: 1995Q1 to 2013Q4, 48.28\% of 2012Q1 QCEW Employment |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| North Carolina | 1991Q1 | 2014Q3 | 1 | 2.92 |
| Oregon | 1991Q1 | 2014Q3 | 2 | 1.23 |
| Pennsylvania | 1991Q1 | 2014Q3 | 3 | 4.44 |
| California | 1991Q3 | 2014Q3 | 4 | 11.37 |
| Arizona | 1992Q1 | 2014Q3 | 5 | 1.85 |
| Wyoming | 1992Q1 | 2014Q3 | 6 | . 19 |
| Florida | 1992Q4 | 2014Q2 | 7 | 5.78 |
| Montana | 1993Q1 | 2014Q3 | 8 | . 31 |
| Georgia | 1994Q1 | 2014Q3 | 9 | 2.90 |
| South Dakota | 1994Q1 | 2014Q2 | 10 | . 30 |
| Minnesota | 1994Q3 | 2014Q3 | 11 | 2.05 |
| New York | 1995Q1 | 2014Q3 | 12 | 6.49 |
| Rhode Island | 1995Q1 | 2014Q3 | 13 | . 35 |
| Texas | 1995Q1 | 2014Q3 | 14 | 8.10 |


| Regime 3: 1998Q1 to 2013Q4, 17.66\% of 2012Q1 QCEW Employment |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| New Mexico | 1995Q3 | 2014Q3 | 1 | . 55 |
| Hawaii | 1995Q4 | 2014Q3 | 2 | . 44 |
| Connecticut | 1996Q1 | 2014Q3 | 3 | 1.26 |
| Maine | 1996Q1 | 2014Q3 | 4 | . 43 |
| New Jersey | 1996Q1 | 2014Q3 | 5 | 2.87 |
| Kentucky | 1996Q4 | 2014Q3 | 6 | 1.32 |
| West Virginia | 1997Q1 | 2014Q3 | 7 | . 52 |
| Michigan | 1998Q1 | 2014Q3 | 8 | 3.04 |
| Nevada | 1998Q1 | 2014Q3 | 9 | . 89 |
| North Dakota | 1998Q1 | 2014Q3 | 10 | . 31 |
| South Carolina | 1998Q1 | 2014Q3 | 11 | 1.35 |
| Tennessee | 1998Q1 | 2014Q3 | 12 | 2.03 |
| Virginia | 1998Q1 | 2014Q2 | 13 | 2.65 |


| Regime 4: 2004Q1 to 2013Q4, 14.71\% of 2012Q1 QCEW Employmen |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Delaware | 1998Q3 | 2014Q3 | 1 | . 31 |
| Iowa | 1998Q4 | 2014Q3 | 2 | 1.12 |
| Nebraska | 1999Q1 | 2014Q3 | 3 | . 69 |

Table A1 (Continued)

| Count | State | First Quarter | Last Quarter | Entry Order | \% 2012Q1 QCEW <br> Employment |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 42 | Utah | 1999Q1 | 2014Q3 | 4 | . 91 |
| 43 | Ohio | 2000Q1 | 2014Q3 | 5 | 3.93 |
| 44 | Oklahoma | 2000Q1 | 2014Q3 | 6 | 1.11 |
| 45 | Vermont | 2000Q1 | 2014Q3 | 7 | . 22 |
| 46 | Alabama | 2001Q1 | 2014Q3 | 8 | 1.34 |
| 47 | Massachusetts | 2002Q1 | 2014Q2 | 9 | 2.55 |
| 48 | District of Columbia | 2002Q2 | 2014Q3 | 10 | . 43 |
| 49 | Arkansas | 2002Q3 | 2014Q3 | 11 | . 86 |
| 50 | New Hampshire | 2003Q1 | 2014Q2 | 12 | . 47 |
| 51 | Mississippi | 2003Q3 | 2014Q3 | 13 | . 77 |

NOTE.-This table presents information on the states that make up each date regime. Each panel gives the first and last quarter of data available, the entry order, and the employment coverage (percentage of 2012Q1 private Quarterly Census of Employment and Wages [QCEW] employment) for each state in the regime. Office of Personnel Management data for federal workers are not shown in this table but are available beginning in 2000 Q 1 .


Fig. A1.-Immigrant candidates: excluded earnings records. This figure presents the count of earnings records excluded from the eligible-workers frame each year, disaggregated by the different eligibility requirements the record failed to meet: (i) records that are only on the unemployment insurance ("Invalid SSN" [Social Security number]), (ii) records where the SSN is valid but the age of the worker is less than 5 years old ("Age $<5$ "), (iii) records where the worker is between 5 and 13 years old (" $5 \leq$ Age $<13$ "), (iv) records where the worker is between 13 and 18 years old (" $13 \leq$ Age $<18$ "), (v) records where the worker is more than 70 years old ("Age $>70$ "), (vi) records where the worker has more than 12 jobs a year ("No. Jobs > 12"), and (vii) records that fail to meet the other eligibility requirements ("Other"), such as the year being greater than or equal to the SSN year of issue and less than the year of death (when available). A color version of this figure is available online.

Table A2
Immigrant Candidates-Excluded Earnings Records

| Year | Total | Invalid SSN | Age < 5 | $\begin{gathered} 5 \geq \text { Age } \\ <13 \end{gathered}$ | $\begin{gathered} 13 \leq \text { Age } \\ <18 \end{gathered}$ | Age > 70 | $\begin{gathered} \text { No. Jobs } \\ >12 \end{gathered}$ | Other |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1990 | 2,173,054 | 131,768 | 92,173 | 115,966 | 1,383,852 | 302,791 | 61,336 | 85,168 |
| 1991 | 2,029,041 | 156,980 | 96,503 | 110,535 | 1,228,937 | 300,232 | 53,311 | 43 |
| 1992 | 2,024,225 | 161,800 | 99,380 | 111,528 | 1,199,329 | 310,526 | 55,873 | 89 |
| 1993 | 2,227,908 | 204,299 | 123,925 | 122,587 | 1,294,809 | 333,303 | 59,024 | 89,961 |
| 1994 | 2,546,460 | 228,963 | 145,038 | 136,015 | 1,500,927 | 363,506 | 74,634 | 97,377 |
| 1995 | 9,875,811 | 1,240,177 | 939,315 | 676,532 | 4,536,074 | 1,695,371 | 337,545 | 450,797 |
| 1996 | 10,144,571 | 1,282,244 | 1,020,460 | 731,340 | 4,625,974 | 1,649,645 | 377,807 | 457,101 |
| 1997 | 10,560,373 | 1,318,787 | 1,051,685 | 773,013 | 4,802,606 | 1,737,019 | 408,080 | 469,183 |
| 1998 | 13,680,138 | 1,579,419 | 1,227,565 | 942,868 | 6,460,058 | 2,308,455 | 571,745 | 590,028 |
| 1999 | 14,850,424 | 1,801,636 | 1,328,052 | 1,059,582 | 6,864,218 | 2,559,284 | 617,195 | 620,457 |
| 2000 | 15,909,402 | 2,087,866 | 1,441,233 | 1,147,779 | 7,084,996 | 2,826,633 | 671,695 | 649,200 |
| 2001 | 15,142,444 | 2,313,768 | 1,354,067 | 1,109,587 | 6,313,180 | 2,864,144 | 565,342 | 622,356 |
| 2002 | 13,646,946 | 2,030,273 | 1,168,828 | 988,866 | 5,573,020 | 2,784,977 | 519,677 | 581,305 |
| 2003 | 13,105,529 | 2,260,426 | 1,059,202 | 965,151 | 4,979,593 | 2,776,405 | 493,455 | 571,297 |
| 2004 | 15,254,789 | 2,628,435 | 1,099,414 | 1,087,743 | 5,976,072 | 3,254,876 | 561,150 | 647,099 |
| 2005 | 16,109,360 | 2,881,580 | 1,030,810 | 1,240,576 | 6,271,025 | 3,383,095 | 626,426 | 675,848 |
| 2006 | 16,830,576 | 3,071,079 | 959,130 | 1,332,606 | 6,513,877 | 3,564,841 | 686,925 | 702,118 |
| 2007 | 16,464,027 | 3,109,359 | 860,258 | 1,254,957 | 6,233,964 | 3,605,470 | 712,999 | 687,020 |
| 2008 | 14,509,746 | 2,909,378 | 683,388 | 1,081,938 | 5,135,680 | 3,478,821 | 564,086 | 656,455 |
| 2009 | 11,701,711 | 2,484,829 | 471,798 | 884,181 | 3,620,311 | 3,240,941 | 390,427 | 609,224 |
| 2010 | 11,019,697 | 2,328,456 | 382,395 | 816,592 | 3,283,378 | 3,210,027 | 402,839 | 596,010 |
| 2011 | 10,942,606 | 2,307,310 | 315,743 | 767,636 | 3,269,325 | 3,224,106 | 450,244 | 608,242 |
| 2012 | 11,556,277 | 2,822,199 | 240,123 | 742,658 | 3,386,957 | 3,282,004 | 449,498 | 632,838 |
| 2013 | 13,216,695 | 4,157,518 | 178,979 | 671,775 | 3,622,084 | 3,409,276 | 492,710 | 684,353 |

[^26]
## A2. Comparison to NIPA

The BEA NIPA estimates are based primarily on the BLS QCEW, an alternative source of employment and earnings with similar coverage as the UI-based job level data used in this paper. A firm typically files a QCEW firm-level report in conjunction with the UI job-level data each quarter. The QCEW report is sent to BLS, where it undergoes edits and imputations before the final statistics are released. ${ }^{53}$ These data are then used by BEA as the primary input when estimating the wage and salary component of the NIPA tables. ${ }^{54}$

Table A3 presents a comparison of our estimates of annual earnings with the BEA NIPA data. Figure A2 plots this comparison. Our estimates of total annual earnings using the all-workers frame vary from $16.5 \%$ of NIPA wage and salary estimates in 1990, the beginning of LEHD date regime 1 ; to $60.1 \%$ in 1995 , the beginning of date regime 2 ; to $76.4 \%$ in 1998 , the beginning of date regime 3 ; to $90.6 \%$ in 2004, the beginning of date regime 4 . Once LEHD data are complete in 2004, the two series track almost exactly. By 2013, the all-workers estimate is about $91.7 \%$ of the NIPA wage and salary estimates. The eligible-workers estimates follow a pattern similar to that of the all-workers estimates, with about 2 percentage points lower coverage relative to the all-workers frame after 2004.

The coverage of both the all-workers frame and the eligible-workers frame is very low relative to the NIPA estimates in the early 1990s but increases dramatically in 1995 once the historical data for the more populous states (California, Florida, New York, and Texas) have entered the LEHD infrastructure files. When the frame is complete (date regime 4), there is an apparent coverage gap of about $8-9$ percentage points for the all-workers frame and 10-11 percentage points for the eligible-workers frame. About half of this gap is due to differences between the statutory-employer population for UI wage records and the NIPA definition of wage and salary income. When comparing frames with similar coverage definitions (UI wage records vs. QCEW), our results suggest that the gap between the two frames is about 4-5 percentage points for the all-workers frame and 5-6 percentage points for the eligible-workers frame.

[^27]Table A3
Earnings Measures-National Income and Product
Accounts (NIPA) versus Longitudinal EmployerHousehold Dynamics (LEHD) Data

| Year | NIPA Wage <br> and Salary | LEHD <br> Total | Eligible <br> Workers | Immigrant <br> Candidates |
| :---: | :---: | :---: | :---: | :---: |
| 1990 | $3,611.6$ | 594.7 | 587.4 | 7.3 |
| 1991 | $3,558.4$ | 593.2 | 585.7 | 7.5 |
| 1992 | $3,639.8$ | 611.2 | 603.8 | 7.4 |
| 1993 | $3,669.6$ | 609.3 | 601.6 | 7.7 |
| 1994 | $3,760.7$ | 642.6 | 633.9 | 8.7 |
| 1995 | $3,862.1$ | $2,319.3$ | $2,279.7$ | 39.6 |
| 1996 | $3,969.2$ | $2,336.3$ | $2,294.5$ | 41.8 |
| 1997 | $4,159.4$ | $2,494.2$ | $2,448.4$ | 45.8 |
| 1998 | $4,417.6$ | $3,374.6$ | $3,312.9$ | 61.7 |
| 1999 | $4,607.8$ | $3,539.3$ | $3,469.8$ | 69.5 |
| 2000 | $4,825.9$ | $3,770.5$ | $3,694.7$ | 75.8 |
| 2001 | $4,817.3$ | $3,785.9$ | $3,707.7$ | 78.2 |
| 2002 | $4,782.5$ | $3,743.2$ | $3,666.4$ | 76.8 |
| 2003 | $4,808.3$ | $3,739.8$ | $3,663.8$ | 76.0 |
| 2004 | $4,942.6$ | $4,478.7$ | $4,387.3$ | 91.4 |
| 2005 | $5,018.8$ | $4,565.8$ | $4,469.3$ | 96.5 |
| 2006 | $5,174.0$ | $4,716.5$ | $4,613.0$ | 103.5 |
| 2007 | $5,312.4$ | $4,842.3$ | $4,736.2$ | 106.1 |
| 2008 | $5,224.3$ | $4,767.6$ | $4,667.3$ | 100.3 |
| 2009 | $5,018.6$ | $4,579.8$ | $4,489.4$ | 90.4 |
| 2010 | $5,037.6$ | $4,593.4$ | $4,503.7$ | 89.7 |
| 2011 | $5,078.9$ | $4,630.1$ | $4,539.8$ | 90.3 |
| 2012 | $5,197.7$ | $4,750.8$ | $4,652.5$ | 98.3 |
| 2013 | $5,257.9$ | $4,822.0$ | $4,706.0$ | 116.0 |

Note.-This table compares total earnings as measured in the US Bureau of Economic Analysis (BEA) NIPA to earnings computed from LEHD. "LEHD Total" presents total annual earnings for the all-workers frame. This total is decomposed into earnings attributed to workers included in the eligible-workers frame ("Eligible Workers") and to workers who are not included ("Immigrant Candidates"). Units are in billions of real (2000) dollars, converted using the consumer price index for all urban consumers. The frame is complete from 2004 forward.


FIG. A2.-National income and product accounts (NIPA). This figure compares total earnings as measured in US Bureau of Economic Analysis (NIPA; solid line) to earnings computed from Longitudinal Employer-Household Dynamics (LEHD) using all workers (dashed line). A color version of this figure is available online.

## A3. Labor Force Attachment of Active Workers

Table A4
Labor Force Activity of Workers in Each Earnings Bin

| $\begin{array}{l}\text { Quarters Worked, } \\ \text { Longest Job }\end{array}$ | Workers |  |  | $\begin{array}{c}\text { Average } \\ \text { No. of Jobs }\end{array}$ |
| :--- | ---: | ---: | ---: | ---: | \(\left.\begin{array}{c}Average <br>

Earnings (\$)\end{array}\right]\)

Table A4 (Continued)

| Quarters Worked, <br> Longest Job | Workers |  | Average <br> No. of Jobs | Average <br> Earnings (\$) |
| :---: | :---: | :---: | :---: | :---: |
|  | Counts | Percent |  |  |
|  | Middle 60\% of Earnings Distribution |  |  |  |
| 1, 1 | 853,497 | 1.0 | 1.051 | 13,637 |
| 2, 1 | 489,513 | . 6 | 1.643 | 14,924 |
| 2, 2 | 2,697,567 | 3.2 | 1.176 | 14,375 |
| 3, 1 | 680,994 | . 8 | 1.475 | 19,879 |
| 3, 2 | 2,409,536 | 2.9 | 2.119 | 15,891 |
| 3, 3 | 4,976,450 | 5.9 | 1.233 | 17,446 |
| 4, 1 | 52,620 | . 1 | 3.726 | 17,579 |
| 4, 2 | 2,746,891 | 3.3 | 3.287 | 17,604 |
| 4,3 | 7,105,740 | 8.5 | 2.592 | 20,563 |
| 4, 4 | 841,481 | 1.0 | 2.109 | 19,230 |
| 4, 5 | 8,869,511 | 10.6 | 1.602 | 22,405 |
| 4, 6 | 52,012,001 | 62.1 | 1.212 | 26,107 |
|  | Top 20\% of Earnings Distribution |  |  |  |
| 1, 1 | 75,101 | . 3 | 1.038 | 146,574 |
| 2, 1 | 34,381 | . 1 | 1.361 | 138,531 |
| 2, 2 | 112,925 | . 4 | 1.096 | 102,246 |
| 3, 1 | 94,047 | . 3 | 1.178 | 92,110 |
| 3, 2 | 171,999 | . 6 | 1.605 | 95,079 |
| 3, 3 | 434,213 | 1.6 | 1.128 | 89,432 |
| 4, 1 | 7,589 | . 0 | 2.608 | 90,693 |
| 4, 2 | 312,325 | 1.1 | 2.752 | 84,965 |
| 4, 3 | 1,383,555 | 5.0 | 2.323 | 87,727 |
| 4, 4 | 139,347 | . 5 | 1.993 | 90,280 |
| 4, 5 | 2,493,150 | 8.9 | 1.500 | 92,054 |
| 4, 6 | 22,653,328 | 81.2 | 1.181 | 88,447 |

[^28]
## Appendix B

Inequality Trends in the LEHD All-Workers Frame (1990-2013)
In Section III we discussed the trends in earnings inequality observed in the eligible-workers frame. Here we detail the inequality trends in the allworkers frame and analyze how they differ from the trends observed in the eligible-workers frame.

With a better understanding of how the exclusion of specific workers affects the distribution of earnings, we then turn our attention to earnings inequality. We analyze how various measurements of the gap between the top and bottom of the earnings distribution have changed over time and how the trends change as we move from the all-workers to the eligible-workers frame.

Figure B1 plots selected percentiles for the two worker frames: the solid lines are the percentiles computed from the all-workers frame, while the dashed lines are the percentiles computed from the eligible-workers frame. Comparing the solid and dashed lines in figure B1, it is clear that the main consequence of shifting the frame from all workers to eligible workers is an increase in the percentile values, particularly at the bottom of the earnings distribution.
100,000
90,000
80,000
70,000
60,000
50,000
40,000
30,000
20,000
10,000
0


| 100,000 |  |
| :---: | :---: |
|  | ( |
| 90,000 |  |
| 80,000 | 0 |
| 70,000 | - $0.0 \cdot 0 \cdot 8$ |
|  | 8--8--8-9-g |
| 60,000 |  |
| 50,000 | $\Delta--A=-\Delta-A$ |
| 40,000 |  |
| 30,000 |  |
| 20,000 | $8--8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8--8--8-8--8--8$ |
| 10,000 |  |
|  |  |
|  |  |

Fig. B1.-Percentiles of the earnings distribution by worker frame. This figure plots the 10th, 20th, 50 th, 80 th, 90 th, and 95 th percentiles of the earnings distribution by worker frame and year. The solid lines are the percentiles of the earnings distribution of all workers (AW) by year. The dashed lines are the percentiles of the earnings distribution of eligible workers (EW) by year. A color version of this figure is available online.

Figure B2 plots the ratio of the 90th percentile to the 10 th percentile for each date regime using the all-workers frame. The figure confirms that there are some differences in the levels of these curves, but the trend analysis is largely unchanged.


Fig. B2.-Ratio of the 90 th to the 10 th percentile of the earnings distribution. This figure plots the ratio of the 90 th to the 10 th percentile for all workers by date regime. A color version of this figure is available online.

To see this more clearly, table B1 presents the average percentile values from 1995 to 2013 for both the all-workers frame and the eligible-workers frame, and the last row computes their ratio (eligible workers to all workers). First, notice that the ratio is always above 1, meaning that each percentile computed from the eligible-workers frame is greater than the equivalent percentile computed from the all-workers frame. Removing the immigrant candidates from the all-workers frame to construct the eligible-workers frame eliminates an unknown number of individuals who make very low earnings and, thus, tend to be at the bottom of the all-workers earnings distribution. For example, in 2006 immigrant candidates held about $8 \%$ of all jobs but contributed only about 2\% to total earnings. Furthermore, average earnings for immigrant candidates were about $\$ 6,150$ in 2006 compared with $\$ 32,865$ for eligible workers. Thus, the removal of these low-earnings workers from the all-workers frame makes the ratio of eligible-workers to all-workers percentiles in table B1 higher toward the bottom of the earnings distribution. Specifically, notice that the 1st percentile in the eligible-workers earnings distribution is, on average, about $32 \%$ greater than the 1 st percentile in the all-workers earnings distribution, that the 5th percentile is about $41 \%$ greater, that the 10th percentile is about $36 \%$ greater, and that the 20th percentile is about $26 \%$ greater. From the median onward, while the absolute differences in the percentile values are large, the relative differences are not as stark, with the percentiles in the eligible-workers earnings distribution being about $2 \%-8 \%$ greater than the corresponding percentile in the allworkers earnings distribution. Finally, notice that regardless of the worker
frame used, there is a large number of workers with very low earnings in LEHD, with the average 10th percentile at only $\$ 1,858$ in the all-workers frame and $\$ 2,527$ in the eligible-workers frame.

Table B1
Average Percentiles of the Earnings Distribution by Worker Frame (1995-2013)

|  | Percentile |  |  |  |  |  |  |  |  |
| :--- | :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1st | th | 10th | 20th | 50th | 80th | 90th | 95th | 99th |
| Frame | 100 | 713 | 1,858 | 5,141 | 20,093 | 43,741 | 62,277 | 84,012 | 173,847 |
| All workers | 132 | 1,005 | 2,527 | 6,463 | 21,762 | 45,343 | 64,021 | 86,108 | 178,304 |
| Eligible workers <br> Ratio of eligible work- <br> ers to all workers | 1.3195 | 1.4088 | 1.3605 | 1.2572 | 1.0831 | 1.0366 | 1.0280 | 1.0249 | 1.0256 |

Nоте.-The first row presents the average percentile values from the earnings distribution of all workers in all states from 1995 to 2013. The second row presents the average percentile values from the earnings distribution of eligible workers in all states from 1995 to 2013. The last row computes the ratio of each percentile from the eligible-workers frame to the all-workers frame.

Starting with the all-workers frame in figure B3, notice that all of the measures show a decline in earnings inequality from 1995 to 2000 . This can also be seen in table B2. The first row presents the average of each ratio from 1995 to 1999 . Notice that they are all above 1, meaning that earnings inequality was greater in the late 1990 s than in 2000 . Then, after 2000 , except for the 99/1 ratio (which has a slight upward trend), all other measures of earnings inequality remain relatively stable. The second row of table B2 presents the average of each ratio (relative to 2000) from 2001 to 2013. Notice that aside from the 99/1 ratio, which on average increased by about $5 \%$ after 2000, the other measures have remained around their 2000 levels. Thus, aside from differences at the very top or the very bottom of the earnings distribution, earnings inequality among all workers has apparently seen little or no change over the last 10 years.


Fig. B3.-Selected inequality measures from 1990 to 2013, relative to 2000 (all workers). The measures of earnings inequality considered are (i) the ratio of the 99th to the 1 st percentile ("P99 to P1"), (ii) the ratio of the 95th to the 5 th percentile ("P95 to P5"), (iii) the ratio of the 90th to the 10th percentile ("P90 to P10"), (iv) the ratio of the 80th to the 20th percentile ("P80 to P20"), and (v) the variance of log annual earnings ("Variance"). A color version of this figure is available online.

Table B2
Inequality Measures Relative to 2000 by Worker Frame

|  | Inequality Measures |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $99 / 1$ | $95 / 5$ | $90 / 10$ | $80 / 20$ | Variance |  |
|  | All Workers |  |  |  |  |  |
| Pre-2000 | 1.038 | 1.099 | 1.092 | 1.075 | 1.036 |  |
| Post-2000 | 1.050 | 1.010 | 1.004 | .983 | 1.004 |  |
| Pre-GR | 1.001 | 1.003 | 1.005 | .992 | 1.001 |  |
| GR | 1.059 | 1.009 | 1.005 | .978 | 1.006 |  |
| Post-GR | 1.131 | 1.022 | 1.002 | .968 | 1.007 |  |
|  | 1.085 | 1.119 | 1.103 | 1.080 | 1.047 |  |
| Pre-2000 | 1.154 | 1.136 | 1.114 | 1.064 | 1.054 |  |
| Post-2000 | 1.063 | 1.075 | 1.067 | 1.039 | 1.031 |  |
| Pre-GR | 1.209 | 1.181 | 1.151 | 1.084 | 1.073 |  |
| GR | 1.286 | 1.222 | 1.178 | 1.099 | 1.086 |  |
| Post-GR |  |  | Eligible Workers |  |  |  |

Note.-The top panel presents measures of earnings inequality for all workers in all states relative to 2000, while the bottom panel presents the same measures for eligible workers. The measures of earnings inequality considered are (i) the ratio of the 99th to the 1 st percentile ("99/1"), (ii) the ratio of the 95 th to the 5 th percentile (" $95 / 5$ "), (iii) the ratio of the 90 th to the 10 th percentile (" $90 / 10$ "), (iv) the ratio of the 80 th to the 20 th percentile (" $80 / 20$ "), and (v) the variance of $\log$ annual earnings ("Variance"). The values in the table are averages before and after 2000: 1995-9 ("Pre-2000") and 2001-13 ("Post-2000"). The post-2000 years are further subdivided into three periods: 2001-7 ("Pre-GR"), 2008-9 ("GR"), and 2010-3 ("Post-GR"). GR = Great Recession.


Fig. B4.-Selected inequality measures for the top and bottom of the earnings distribution from 1990 to 2013, relative to 2000 (all workers). $A$ and $B$ decompose the $99 / 1$ ratio, the $95 / 5$ ratio, the $90 / 10$ ratio, and the $80 / 20$ ratio for all workers in all states relative to 2000 from 1990 to 2013 relative to the median. $A$ plots the following ratios for the top half of the earnings distribution: (i) the ratio of the 99th to the 50 th percentile ("P99 to P50"), (ii) the ratio of the 95 th to the 50 th percentile ("P95 to P50"), (iii) the ratio of the 90th to the 50th percentile ("P90 to P50"), and (iv) the ratio of the 80 th to the 50 th percentile ("P80 to P50"). $B$ plots the following ratios for the bottom half of the earnings distribution: (i) the ratio of the 50th to the 1st percentile ("P50 to P1"), (ii) the ratio of the 50th to the 5th percentile ("P50 to P5"), (iii) the ratio of the 50th to the 10th percentile ("P50 to P10"), and (iv) the ratio of the 50th to the 20th percentile ("P50 to P20"). The estimates are based on the all-workers frame from the Longitudinal Employer-Household Dynamics infrastructure files. A color version of this figure is available online.


Fig. B5.-Percentile ratios of the earnings distribution by worker frame. This figure plots ratios of top and bottom percentiles for all workers (solid lines) and for eligible workers (dashed lines). $A$ plots the ratio of the 99 th to the 1 st percentile by worker frame. This ratio is decomposed into the ratio of the 99th to the 50 th percentile in $B$ and the ratio of the 50 th to the 1 st percentile in $C . D$ plots the ratio of the 95 th to the 5 th percentile by worker frame. This ratio is decomposed into the ratio of the 95th to the 50 th percentile in $E$ and the ratio of the 50th to the 5 th percentile in $F$. A color version of this figure is available online.


Fig. B5.-(Continued)


Fig. B6.-Percentile ratios of the earnings distribution by worker frame. This figure plots ratios of top and bottom percentiles for all workers (solid lines) and for eligible workers (dashed lines). A plots the ratio of the 90 th to the 10 th percentile by worker frame. This ratio is decomposed into the ratio of the 90th to the 50 th percentile in $B$ and the ratio of the 50 th to the 10 th percentile in $C . D$ plots the ratio of the 80th to the 20th percentile by worker frame. This ratio is decomposed into the ratio of the 80 th to the 50 th percentile in $E$ and the ratio of the 50 th to the 20th percentile in $F$. A color version of this figure is available online.


Fig. B6.-(Continued)

## Appendix C

## Comparison with Household Surveys

In Section III we discussed the trends in earnings inequality based on our analysis of the eligible-workers frame, which we constructed using the LEHD infrastructure data and supplementary information from the US Census Bureau's enhanced version of the SSA's Numident file. Section III.A discussed the highlights of the comparison of our data to the CPS and the ACS. To put our inequality measures in the context of a broader literature, we compare results based on the administrative data frame discussed in the main text with similar measures constructed using household survey data. ${ }^{55}$

## C1. Household Survey Data

To create our household survey analysis file, we use the following records from the CPS-ASEC (March) and the ACS:

- CPS-ASEC: all persons from survey years 1990-2004
- ACS: all persons from survey years 2000 to 2013

In the CPS-ASEC, the respondent is surveyed in March and reports earnings for the previous calendar year. We date the earnings accordingly. However, in the ACS the respondent reports earnings for the past 12 months, and the survey is in the field continuously throughout the year. Our approach in this case is to date the earnings with the calendar year containing the majority of the months covered by the response, with ties going to the more recent year. As in the LEHD data, nominal earnings are deflated to real 2000 dollars using the CPI-U. In all cases, we used the internal (confidential) versions of the CPS-ASEC and the ACS. None of the household survey data are top coded. We did not replace the US Census Bureau's edit and imputation routines with our own. We used the allocated values in the files.

Similar to the workers in LEHD, we consider two samples of individuals from the household surveys. The first includes all individuals. The second isolates workers whose employment should be covered under UI (including federal employees) and who should, therefore, appear in the LEHD administrative data. We designate a survey respondent as a "covered worker" if he or she meets the following conditions:

- person interviewed is not living in group quarters;
- individual is employed at a private firm or in local/state/federal government or is self-employed in an incorporated firm;

[^29]- labor earnings are positive; and
- individual is between 18 and 70 years old, inclusive.

The last two restrictions combined are included to match the earnings and age restrictions used to identify active eligible workers in the LEHD data.

Finally, in most of the results to follow we do not report results separately for CPS-ASEC and ACS individuals. Instead, in the overlapping years (2000-2003) we interpolate estimates computed from the CPS-ASEC and the ACS to create a single time series using the method in Abowd and Vilhuber (2011).

## C2. Comparison of Aggregate Summaries

We start by analyzing how the earnings distribution in household surveys compares to the one computed from administrative records. In the household survey data, the estimated percentile values tend to be greater for covered workers than for all workers. Figure C1 presents the percentiles of the earnings distribution for all and covered workers in CPS/ACS. Comparing these values to the ones estimated from the LEHD data, shown in figure B1, notice that for percentiles above the median the values from the eligible-workers frame are fairly close to the ones from the household surveys. Below the median, however, the differences are greater, with the percentiles estimated from the household surveys being much greater than the percentiles estimated from LEHD. For example, notice that earnings associated with the 10th percentile in the CPS/ACS data are close to the 20th percentile in LEHD.

FIg. C1.-Percentiles of the earnings distribution for all and covered workers by year. This figure plots the 10th, 20th, 50th, 80th, 90th, and 95th percentiles of the earnings distribution for all workers (ALL) and for covered workers (CW) in the Current Population Survey's Annual Social and Economic Supplement and the American Community Survey (2000-2013) by year. Covered workers include respondents whose employment relation should be covered as a statutory employee under state UI or as a federal employee and therefore appear in the Longitudinal Employer-Household Dynamics data. A color version of this figure is available online.

To see these differences in percentiles more clearly, figure C 2 plots the ratio of the percentiles of the earnings distribution measured using the LEHD eligible-workers frame to the same percentiles measured from the covered workers in the combined CPS/ACS data. First, notice that all of the ratios in figure C 2 are below 1, meaning that the percentiles estimated from the household surveys are always greater than the corresponding percentiles estimated from the administrative data. However, the magnitude of this difference varies greatly across the percentiles of the earnings distribution. Specifically, notice that the relative differences in the 95th, 90th, and 80th percentiles are very small compared with the relative differences in the 5th, 10th, and 20th percentiles.

Table 4 presents averages of the percentiles from 1995 to 2013 for CPS/ ACS and LEHD. Notice that on average the earnings associated with the 80th, 90 th, and 95 th percentiles are about $\$ 3,500$ less in the LEHD data than in CPS/ACS data. Furthermore, as can be seen in figure C2, this gap is decreasing over time, such that in 2013 the difference in the 95 th percentile is only $\$ 264$. In the bottom half of the earnings distribution, however, a CPS/ ACS covered worker earns about $\$ 4,000$ more than an LEHD worker at the same point in the earnings distribution. While this absolute difference may not seem that large, relatively, a CPS/ACS worker at the 10th percentile is making 2.54 times more than his LEHD counterpart and 3.40 times more for a CPS/ACS worker in the 5th percentile. This means that the survey data include more low-earning jobs that are not statutory employment relationships or are not reported as such to state UI systems. Last, notice that the percentiles in LEHD increase faster than their CPS/ACS counterparts since all of the ratios exhibit an upward trend, especially after the Great Recession.

FIG. C2.-Ratio of unemployment insurance (UI) earnings to household survey-reported earnings by percentile. This figure presents the ratio of earnings for eligible workers in Longitudinal Employer-Household Dynamics to the earnings reported by covered workers in the Current Population Survey/American Community Survey for the 5th, 10 th, 20 th, 50 th, 80 th, 90 th, and 95 th percentile. A color version of this figure is available online. HHLD $=$ household.

To see whether differences in the earnings distribution between workers in CPS/ACS and eligible workers in the LEHD data translate into differences in trends in inequality, we compute various measures of earnings inequality in CPS/ACS and compare them to their LEHD counterparts. In particular, we compute the $95 / 5,90 / 10$, and $80 / 20$ ratios and the variance of $\log$ annual earnings. We plot their time series in figure $5 A$ and $5 B$ for all workers and covered workers, respectively. Both the all-workers sample and the covered-workers sample show a decline in earnings inequality during the late 1990s that reverses after 2000. However, in the all-workers sample the magnitude of this increase in inequality in the post-2000 period strongly depends on the measure considered. For example, from 2000 to 2013 the $95 / 5$ ratio increased by $66 \%$, from 36.30 to 60.26 , while the $90 /$ 10 ratio increased by $42 \%$, from 12.95 to 18.35 . On the other hand, the $80 / 20$ ratio increased by $26 \%$, from 4.64 to 5.86 , while the variance of $\log$ earnings increased by only $5 \%$, from 1.23 to 1.26 . Thus, while the measures are all trending upward after 2000 in the all-workers sample, it is unclear whether this increase has been large or small. In the covered-workers sample, earning inequality has also been increasing after 2000; however, the magnitude of this increase is relatively consistent across the different measures of earnings inequality. The $95 / 5$ ratio increased by $32 \%$ from 2000 to 2013, while the $90 / 10$ ratio increased by $26 \%$. The $80 / 20$ ratio and the variance in log earnings increased less over this period, by about $13 \%$ and $14 \%$, respectively. On the other hand, notice that the decline in inequality in the 1990s is very similar across the various measures and samples.

These trends in earnings inequality are very similar to the ones observed among eligible workers in the LEHD data. Specifically, comparing the time series of earnings inequality for covered workers in CPS/ACS (fig. $5 B$ ) to the one for eligible workers in LEHD (fig. 3), notice that the general patterns are very similar. Both of these figures show a decline in inequality during the 1990s and a steady increase in inequality after 2000. The magnitude of this increase is also similar between the covered workers in CPS/ACS and the eligible workers in the LEHD data. Compare the second panel of table C 1 to the second panel of table B2. The second row in both tables shows the average of the $95 / 5$ ratio, the $90 / 10$ ratio, the $80 / 20$ ratio, and the variance of log earnings (relative to 2000) after 2000. Both the covered workers in CPS/ ACS and the eligible workers in LEHD saw an increase in the $95 / 5$ ratio and the $90 / 10$ ratio above $10 \%$ and an increase in the $80 / 20$ ratio and the variance of log earnings around $5 \%-6 \%$. Furthermore, most of this increase occurred during or after the Great Recession.

Table C1
Inequality Measures Relative to 2000 for Workers in Household Surveys

|  | Inequality Measures |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | ---: | :---: | :---: | :---: |
|  | $95 / 5$ | $90 / 10$ |  |  |  | $80 / 20$ | Variance |
|  | All Workers |  |  |  |  |  |  |
| Pre-2000 | 1.126 | 1.118 | 1.041 | 1.099 |  |  |  |
| Post-2000 | 1.406 | 1.273 | 1.174 | 1.001 |  |  |  |
| Pre-GR | 1.280 | 1.171 | 1.099 | .976 |  |  |  |
| GR | 1.429 | 1.331 | 1.231 | .998 |  |  |  |
| Post-GR | 1.616 | 1.422 | 1.278 | 1.047 |  |  |  |
|  | Covered Workers |  |  |  |  |  |  |
| Pre-2000 | 1.156 | 1.122 | 1.035 | 1.082 |  |  |  |
| Post-2000 | 1.168 | 1.129 | 1.056 | 1.064 |  |  |  |
| Pre-GR | 1.106 | 1.071 | 1.016 | 1.040 |  |  |  |
| GR | 1.135 | 1.147 | 1.060 | 1.044 |  |  |  |
| Post-GR | 1.293 | 1.221 | 1.125 | 1.117 |  |  |  |

Note.-The first panel presents measures of earnings inequality for all workers in Current Population Survey/American Community Survey, while the second panel presents the same measures for covered workers. The measures of earnings inequality considered are (i) the ratio of the 95 th to the 5 th percentile (" $95 / 5$ "), (ii) the ratio of the 90 th to the 10 th percentile (" $90 / 10$ "), (iii) the ratio of the 80 th to the 20 th percentile (" $80 / 20$ "), and (iv) the variance of $\log$ annual earnings ("Variance"). The values in the table are averages before and after 2000: 1995-9 ("Pre-2000") and 2001-13 ("Post-2000"). The post-2000 years are further subdivided into three periods: 2001-7 ("Pre-GR"), 2008-9 ("GR"), and 2010-13 ("Post-GR"). All measures are 1.00 in 2000 . $\mathrm{GR}=$ Great Recession.

To see whether it is changes in the top or bottom half of the earnings distribution that are driving these trends, we decompose these ratios around the median, as we did using the two worker frames from LEHD. Notice that since 2000 the ratio of the top percentiles to the median has been gradually increasing for both the all-workers sample and the covered-workers sample (fig. C3A, C3C). The bottom of the earnings distribution, however, has evolved differently across these two samples. In the all-workers sample, there has been a substantial rise in inequality (fig. C3B). Among the covered workers, the rise has been much more mild (fig. C3D). In fact, the trends in earnings inequality among the covered workers is very similar to those observed among the eligible workers in LEHD both in terms of the correlation of the times series and the magnitude of the changes. However, one notable difference is the change in earnings inequality around the Great Recession. In LEHD, inequality increased dramatically during the Great Recession. In CPS/ACS, inequality actually drops substantially just prior to the onset of the Great Recession. However, these gains are lost during the recession years as inequality quickly increases back to trend. Thus, while both the household surveys and the administrative data highlight the sensitivity of the bottom of the earnings distribution to the Great Recession, the precise cyclical patterns are not consistent across these two data sources.

Fig. C3.-Selected inequality measures from 1990 to 2013 for the top and bottom of the earnings distribution relative to 2000 (Current Population Survey [CPS]/American Community Survey [ACS]). $A$ and $B$ decompose the $99 / 1$ ratio, the $95 / 5$ ratio, the $90 / 10$ ratio, and the $80 / 20$ for all workers in CPS/ACS relative to 2000 from 1990 to 2013 relative to the median. $A$ plots the following ratios for the top half of the earnings distribution: (i) the ratio of the 95th to the 50th percentile ("P95 to P50"), (ii) the ratio of the 90th to the 50th percentile ("P90 to P50"), and (iii) the ratio of
 the 5 th percentile ("P50 to P5"), (ii) the ratio of the 50th to the 10th percentile ("P50 to P10"), and (iii) the ratio of the 50th to the 20th percentile ("P50 to P20"). C and D present the same decomposition for covered workers in CPS/ACS relative to 2000 from 1990 to 2013. A color version of this figure is available online.

$\begin{array}{lllll}8 & 8 & 8 & 8 & 0 \\ 8 & 8 & 8 & 8 & \\ 0 & 8 & 8 & \end{array}$

60,000
${ }^{\ldots \infty}$
80th Percentile (All Workers)
 (LEHD). This figure plots the 10th, 20th, 80th, and 90th percentiles of the earnings distributions from four samples of the ACS: (i) individuals with positive UI earnings but no reported ACS earnings (dashed line); (ii) individuals with positive reported ACS earnings but no UI earnings (solid line with diamonds); (iii) individuals with positive reported ACS earnings and positive UI earnings using ACS earnings to compute the earnings distribution (solid line); and (iv) individuals with positive reported ACS earnings and positive UI earnings using UI earnings to compute the earnings distribution (dashed line with circles). $A, B, C$, and $D$ are the percentiles for all workers in the ACS. $E, F, G$, and $H$ are the percentiles for the covered workers in the ACS. These are compared with the same percentiles from the eligible workers frame in LEHD (dashed line with squares). A color version of this figure is available online.

Fig. C4.-(Continued)

## C3. Detailed Analysis of Linked Records

To understand where the discrepancies between the administrative and household survey earnings distributions occur, we analyze the individual ACS records from 2005 to 2013, linking them to LEHD UI records from the eligible-workers frame using a crosswalk between the two person identifiers developed and maintained by the US Census Bureau. This allows us to see how earnings differ among workers who do and do not match to the LEHD individual data. We focus on records from 2005 forward because, for these years, both the ACS and LEHD are fully national.

For an individual in the ACS, there are three types of matches to the eligible-workers frame in the LEHD data: (i) reported earnings are positive in the ACS but UI earnings are zero; (ii) no reported earnings in the ACS but UI earnings are positive; and (iii) both ACS reported earnings and UI earnings are positive. We present these match results in table C2. The left panel presents the statistics for all individuals in the ACS, and the right panel presents the same statistics for covered workers in the ACS. When we include all individuals in the ACS, about $96 \%$ report positive earnings when surveyed in the ACS. However, $21 \%$ have no UI earnings. A very small fraction of the individuals in the ACS-the remaining 4\%-have positive UI earnings but did not report any earnings when surveyed. When we consider only covered ACS workers, all of these individuals should report positive earnings in the ACS. Of these covered workers, $85 \%$ also have positive UI earnings, and $15 \%$ do not match to any UI records.

Table C2
American Community Survey (ACS)/Unemployment Insurance (UI) Match Comparison

| All Individuals |  |  |  | Covered Workers |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ACS | UI | $\%$ |  | ACS | UI | $\%$ |
| earn $>0$ | earn $>0$ | 75 |  | earn $>0$ | earn $>0$ | 85 |
| earn $=0$ | earn $>0$ | 4 |  | earn $=0$ | earn $>0$ | 0 |
| earn $>0$ | earn $=0$ | 21 |  | earn $>0$ | earn $=0$ | 15 |

Note.-The first row reports the fraction of individuals in the ACS who report positive earnings when surveyed and match to the eligible-workers frame in the LEHD data and, therefore, have positive UI earnings. The second row reports the fraction of individuals in the ACS who do not report earnings when surveyed but match to the LEHD data and, therefore, have positive UI earnings. The third row reports the fraction of individuals in the ACS who do not match to the LEHD data. The left panel presents the statistics for all individuals in the ACS, and the right panel presents the same statistics for covered workers in the ACS.

Using these matched records, we compare the earnings distribution of four samples of ACS individuals in figure C5:

- individuals with positive UI earnings but no reported ACS earnings (dashed line);
- individuals with positive reported ACS earnings but no UI earnings (solid line with diamonds);
- individuals with positive reported ACS earnings and positive UI earnings using ACS earnings to compute the earnings distribution (solid line); and
- individuals with positive reported ACS earnings and positive UI earnings using UI earnings to compute the earnings distribution (dashed line with circles).

We compute these distributions for both all workers and covered workers in the ACS. Note that for covered workers, having only UI earnings is vanishingly rare, since all covered workers should report positive earnings in the ACS. The earnings distributions from these samples are compared with the one constructed from the eligible-workers frame in LEHD (dashed line with squares). Figure C5 plots the 5th, 50th, and 95th percentiles of these various earnings distributions. ${ }^{56}$

For workers whose earnings are both reported in the ACS and found in LEHD (matched workers), the percentiles computed using the ACS earnings are nearly identical to those computed using UI earnings. Specifically, notice that in figure C 5 the solid line and the dashed line with circles are very close to each other in all subplots, especially at and above the median. The differences in the CPS/ACS percentiles and the LEHD percentiles in figure C 2 are, therefore, very unlikely to be due to misreporting in household surveys. Instead, they must be due to differences in the workers who are surveyed and report earnings in the ACS and those who are found in LEHD. Workers who report positive ACS earnings but do not match to LEHD (ACS only) tend to have lower earnings than the workers who do match (solid lines with diamonds in fig. C5). However, this gap is less pronounced for workers at the top of the earnings distribution for both the allworkers sample and the covered-workers sample in the ACS.

While the ACS-only workers do not earn as much as the matched workers, they do earn significantly more than a large portion of workers in LEHD. This means that the LEHD eligible-workers frame captures more workers in the bottom half of the earnings distribution than the ACS. To see this, notice in figure C5B that the 95th percentiles of both the matched sample and the ACS-only sample are nearly identical to the 95th percentile of the eligibleworkers earnings distribution in LEHD. However, for the median and lower percentiles, the differences are not trivial. The median matched worker tends to make about $21.5 \%$ more than the median eligible-worker in LEHD

[^30]( $\approx \$ 4,770$ ), while the median ACS-only worker makes about $6.4 \%$ less $(\approx \$ 1,417)$. At the bottom, the differences in the 5th percentiles are most stark. A matched worker at the 5 th percentile tends to make about 3.22 times as much as an eligible worker at the 5 th percentile in LEHD ( $\approx \$ 2,649$ ). Even an ACS-only worker at the 5th percentile makes about 2.44 times as much as a corresponding eligible worker ( $\approx \$ 1,459$ ). Thus, the left tail of the earnings distribution in the ACS is much shorter than the one for eligible workers in the LEHD data, resulting in the LEHD percentiles being less than those computed from household surveys.


... U1 On
Fig. C5.-Comparison of percentiles in the American Community Survey (ACS) and Longitudinal Employer-Household Dynamics (LEHD). This figure plots the 5th, 50th, and 95th percentiles of the earnings distributions from four samples of the ACS: (i) individuals with positive UI earnings but no reported ACS earnings (dashed line); (ii) individuals with positive reported ACS earnings but no UI earnings (solid line with diamonds); (iii) individuals with positive reported ACS earnings and positive UI earnings using ACS earnings to compute the earnings distribution (solid line); and (iv) individuals with positive reported ACS earnings and positive UI earnings using UI earnings to compute the earnings distribution (dashed line with circles). $A, C$, and $E$ are the percentiles for all workers in the ACS. $B, D$, and $F$ are the percentiles for the covered workers in the ACS. These are compared with the same percentiles from the eligible-workers frame in the LEHD data (dashed line with squares). A color version of this figure is available online.

## Appendix D

## Inactive Workers and Inequality

In Section II.B we tracked both active and inactive workers in our eligibleworkers frame. In Section III.B we briefly discussed how the treatment of inactivity affects measures of earnings inequality. This appendix presents details supporting those analyses and conclusions.

In appendix B , we excluded inactive workers from the analysis so that we could focus on trends in the ratios of top and bottom percentiles over time. While some inactive workers, given the wages and employment terms on offer, choose to be nonparticipants, others are involuntarily excluded from the labor market. In this section, we present an analysis of how including inactive workers, especially those who were recently employed, affects earnings inequality measures. We begin by analyzing how inactivity has changed in recent years, considering comparisons with the employment-to-population ratio from the CPS/ACS data. Next, we turn our attention to the eligible workers in the LEHD data.

## D1. The Employment-to-Population Ratio

If the US labor market tends to stay relatively close to full employment except for brief periods after the start of a recession, the resultant implied rapid employment growth during a recovery should generate a quick increase in the employment-to-population ratio and a quick decline in the unemployment rate to prerecession levels. However, our results using annual CPS/ACS survey data show a different pattern around the Great Recession.

Figure D1 shows the estimated employment-to-population ratio by year from 1990 to 2013 for all workers (solid line) and covered workers (dashed line) in CPS/ACS. The NBER identifies three recessions during this period, beginning in the following years: 1990, 2001, and 2008 (December 2007). Both CPS/ACS series show a dip in 1993 and then a sustained increase until 1999, when the covered-worker sample employment-to-population ratio begins to decline while the all-workers sample remains relatively flat. Until 1999 the trends for both series are similar, but then the two series diverge, with a decline in the covered workers as a proportion of all workers, suggesting a movement of workers into self-employment. At the beginning of the Great Recession, all three series show a large sustained drop in the employment-to-population ratio, bottoming out in 2009/2010, with only a mild recovery during the ensuing years. These results suggest that unlike previous recessions, substantial numbers of persons employed prior to the Great Recession did not return to employment even 5 years or more after the start of the Great Recession. While previous research focused only on employed persons, the large and persistent decrease in the employment-to-population ratio for all workers and for covered workers only during
and after the Great Recession argues strongly for an expansion of inequality measures to include at least some inactive but eligible workers.


Fig. D1.-Employment-to-population ratio (household surveys). This figure plots the estimated employment-to-population ratio by year from 1990 to 2013 for all workers (solid line) and covered workers (dashed line) in the Current Population Survey (CPS)/American Community Survey. Estimates are based on the authors' calculations from the micro data. These are not the official statistics as released by the Bureau of Labor Statistics from the CPS. A color version of this figure is available online.

## D2. Inactivity-Adjusted Inequality Measures

We estimate three traditional measures of inequality (Gini, Hoover, and Theil), both with and without a category for inactive workers. Deciles of the earnings distribution, estimated as discussed in Section II.D, were used to compute each statistic, with an additional category added for eligible workers with no reported earnings (the inactive category). The earnings value for each person in the inactive category was set to $\$ 1$, a modification necessary to facilitate the consistent calculation of all measures (particularly the Theil index, which uses logarithms). ${ }^{57}$ We create three samples, each with a different set of eligible but inactive workers:

1. All eligible workers each year. This sample assumes that all eligible workers are at risk to be employed. Note that this sample is complete and has no dependence on previous years, but the majority of the inactive eligible workers are probably not in the labor force.
${ }^{57}$ The results for the Gini and Hoover measures using $\$ 0$ show very small differences in levels and identical trends compared with setting the earnings value to $\$ 1$.
2. Active workers and eligible workers most at risk to be employed. This sample includes all active workers and workers not active in the current year but who were active in at least one of the past 4 years. For years prior to 2008 we do not have complete data for every state. In particular, workers with jobs in Massachusetts, the District of Columbia, Arkansas, New Hampshire, and Mississippi will be slightly underrepresented (see table A1). Some of these workers will have earnings in the previous fours year that we do not observe. An upper bound of the impact of this exclusion might be $5 \%$ of the jobs in 2004, but the actual impact is likely much less since the largest state, Massachusetts, entered in 2002Q1 and is therefore missing only 2 years of history in 2004 Q1. In addition, employment in every state is at risk at some point during 2003, the year a worker not employed in 2004 is most likely to have previously been employed.
3. Only active workers. This sample includes only active workers, so no modifications are made to the standard formulas.

Table D1 shows the results. The top panel is for all eligible workers, while the middle panel shows results for workers most at risk to be eligible workers. The bottom panel includes only active eligible workers.

All three of the inequality measures increase substantially as the proportion of eligible workers included in the calculation increases. Not surprisingly, including a large block of workers with only $\$ 1$ of annual earnings greatly increases measured inequality. Comparing our results with another administrative data source, estimates of inequality using SSA data, we find that ours are somewhat larger, although the exact source of the difference is unclear due to coverage differences imposed on the SSA estimation sample. For example, in 2004 the estimated Gini coefficient using a restricted sample of currently eligible SSA recipients is 0.471 , while in our data the estimated Gini is 0.510 (Kopczuk et al. 2010).

Table D1
Inequality Measures with and without Inactive Workers

| Year | Persons | Gini | Hoover | Theil |
| :---: | :---: | :---: | :---: | :---: |
|  |  | All Eligible Workers |  |  |
| 2004 | $219,763,469$ | .696 | .538 | 2.379 |
| 2005 | $222,160,089$ | .697 | .538 | 2.379 |
| 2006 | $224,721,578$ | .698 | .539 | 2.377 |
| 2007 | $227,553,012$ | .699 | .540 | 2.386 |
| 2008 | $230,355,015$ | .702 | .544 | 2.416 |
| 2009 | $232,813,313$ | .714 | .558 | 2.535 |
| 2010 | $234,304,705$ | .720 | .564 | 2.576 |
| 2011 | $235,429,997$ | .720 | .563 | 2.563 |
| 2012 | $236,484,312$ | .719 | .560 | 2.547 |
| 2013 | $237,816,938$ | .716 | .558 | 2.532 |

Table D1 (Continued)

| Year | Persons |  | Gini | Hoover |
| :--- | :---: | :---: | :---: | :---: | Theil

Note.-This table presents traditional measures of inequality (Gini, Hoover, and Theil) for three samples of persons: (i) all eligible workers (top panel), (ii) most-at-risk eligible workers (middle panel), and (iii) only active workers (bottom panel).

Figure D2 shows the share of eligible workers who are inactive (solid line) and the share who are most at risk to be active (dashed line) relative to the base year 2004. The solid line represents the share of eligible workers not currently working each year-the difference between the number of workers in the top panel of table D1 and the number of workers in the bottom panel as a proportion of eligible workers. The dashed line represents the share of workers most at risk to be active not currently working each year-the difference between the number of workers in the middle panel of table D1 and the number of workers in the bottom panel. The dashed line is noticeably more responsive to changes in labor demand, suggesting that we chose a reasonable group to represent the workers most at risk to be active. However, a closer look at the source of the decline in the most-at-risk group (dashed line) from 2011 forward shows that the decline is due both to the growth in employment during the recovery and to a lack of growth in the number of workers most at risk to be active. Many of the at-risk workers who had positive earnings just prior to or at the start
of the Great Recession have not had positive earnings in the subsequent four years. By 2011, they are dropping out of the at-risk group. Although it is difficult to know the labor force status of these workers due to the limitations of administrative data, it does highlight the benefit of having multiple measures of inactive status for the eligible-workers population.


Fig. D2.-Share of inactive and at-risk eligible workers. This figure shows the share of eligible workers who are inactive (solid line) and the share who are "inactive and at risk" (dashed line) relative to the base year 2004. In a given year, a person is "inactive" if that person did not make positive earnings that year. In a given year, a person is inactive and at risk if that person did not make positive earnings that year but did make positive earnings sometime in the last 4 years. A color version of this figure is available online.

In Section III we documented the increase in inequality after 2000 using ratios of various percentiles of the earnings distribution. For the eligibleworkers frame, the increase in earnings of the top $20 \%$ relative to the bottom $20 \%$ of earners accelerates during the Great Recession, with annual earnings increases for workers at the 80th percentile and small declines or no increases for workers at the 20th percentile. The increases for the 99/ 1 ratio, the $95 / 5$ ratio, and the $90 / 10$ ratio are even larger, with the ratios increasing faster the more extreme the comparison (fig. 3). Here we have taken an alternative approach. Instead of comparing two specific points in the earnings distribution, the portmanteau inequality measures presented here weight the changes occurring across the earnings distribution and combine them to produce a single measure of overall inequality. Each measure uses different weights and combining rules; therefore, it is useful to compare each approach.

The relative changes in the Gini coefficients for each of the three samples are presented in figure D3. The results for the first two samples are almost identical. The Gini coefficients for the third sample, only active workers, grow faster before the Great Recession but do not show the increase in inequality at the start of the Great Recession present for the eligible-workers and at-risk-workers samples. Part of the reason for this difference is that the Gini coefficient is very sensitive to changes in earnings at the top of the distribution. At the beginning of the recession, earnings at the top of the distribution declined or stagnated. In spite of the large number of workers moving from active to inactive status at the beginning of the Great Recession, the Gini coefficient for the active-only sample shows inequality declining, although it does start to climb as earnings growth at the top of the distribution resumes in 2009. In contrast, the Gini coefficients for the all-eligible and most-at-risk samples show increasing inequality at the start of the Great Recession, similar to the $80 / 20$ ratio (also shown in the figure).


Fig. D3.-Inequality measures: Gini coefficient. This figure plots the Gini coefficient for three samples of eligible workers: (i) active and all inactive workers ("All Eligible Workers"), (ii) active workers and inactive workers who made positive earnings sometime in the last 4 years ("At Risk"), and (iii) only active workers ("Active Only"). The ratio of the 80th to the 20th percentile ("P80 to P20") is also plotted for reference. A color version of this figure is available online.

The results for the Hoover index, shown in figure D4, are similar to those for the Gini coefficient, although the relative increase in inequality during the Great Recession is larger when measured using the Hoover index. The increase before the Great Recession is also larger when using only active workers.


Fig. D4.-Inequality measures: Hoover index. This figure plots the Hoover index for three samples of eligible workers: (i) active and all inactive workers ("All Eligible Workers"), (ii) active workers and inactive workers who made positive earnings sometime in the last 4 years ("At Risk"), and (iii) only active workers ("Active Only"). The ratio of the 80th to the 20th percentile ("P80 to P20") is also plotted for reference. A color version of this figure is available online.

The final measure we consider is the symmetric Theil index. The results using this measure are shown in figure D5. Over the entire period, the Theil measure is more responsive to earnings distribution changes than either the Gini coefficient or the Hoover index, but it is especially responsive to the addition of inactive workers. The relative change in the Theil index computed using all eligible workers (sample 1) is almost identical to the $80 / 20$ ratio through 2009, with greater inequality after that reflecting the slow decline in inactive workers during the recovery. The relative change in the Theil index computed using only the most-at-risk workers (sample 2) could arguably be viewed as an exaggerated version of the 80/20 ratio. The inclusion of inactive at-risk workers in sample 2 introduces additional information into the Theil index calculation, magnifying the decline in inequality prior to the Great Recession, the increase during the Great Recession, and the decline during the recovery.


Fig. D5.-Inequality measures: Theil index. This figure plots the Theil index for three samples of eligible workers: (i) active and all inactive workers ("All Eligible Workers"), (ii) active workers and inactive workers who made positive earnings sometime in the last 4 years ("At Risk"), and (iii) only active workers ("Active Only"). The ratio of the 80th to the 20th percentile ("P80 to P20") is also plotted for reference. A color version of this figure is available online.

Introducing information about inactive but at-risk workers into the calculation of the Gini coefficient and Hoover index changes the trend, but the inequality levels in 2013 are largely the same relative to 2004 using either measure. The Theil index changes in similar ways with the addition of inactive but at-risk workers; however, the Theil index is much more sensitive to both changes in the earnings distribution and the addition of inactive workers. The growth in the Theil index using only active workers is larger than either the Gini index or the Hoover index. Similar to the Gini and Hoover indices, by not including inactive workers the Theil index fails to capture the increase in inequality at the start of the Great Recession. Adding inactive workers to the Theil index (sample 1) results in a measure similar to the 80/ 20 ratio through 2009; after 2009, the two measures diverge due to the slow decline in the number inactive workers during the recovery from the Great Recession. The Theil index for the most-at-risk workers (sample 2) shows the largest changes in inequality.

Although it is unclear which of the adjusted inequality measures correctly weights the inactive workers, it is worthwhile to consider adjusted measures that count at least some of the zero-earning workers as part of any general analysis of changes in earnings inequality.

## Appendix E

## Decomposing Changes in the Earnings Distribution

In Section IV we presented the evolution of the earnings/inactivity distribution in terms of the year-to-year flows of workers across different parts of the earnings distributions and into and out of active status.

## E1. Worker Flows

Starting in 2005, each year we calculate the change in the number of workers between the current and the previous year for the four earnings/inactivity categories. The year-to-year change in the number of workers in a specific category is driven by changes in the number of workers entering (inflows) and the number of workers leaving (outflows). Specifically, to compute the flows between two employment states, let $A$ and $B$ be arrays of counts for each category in years $t-1$ and $t$, respectively:

$$
\begin{aligned}
& \text { year } t-1: A=\left[\begin{array}{llll}
a_{0} & a_{1} & a_{2} & a_{3}
\end{array} a_{4}\right] \text {, } \\
& \text { year } t: B=\left[\begin{array}{lllll}
b_{0} & b_{1} & b_{2} & b_{3} & b_{4}
\end{array}\right] \text {. }
\end{aligned}
$$

To complete the decomposition and capture all possible transitions, we must add an additional category, zero, representing workers who are not eligible to work in one of the two periods but who are eligible to work in the other. Let $C_{A B}$ be the transition matrix of counts:

$$
C_{A B}=\left[\begin{array}{lllll}
c_{00} & c_{01} & c_{02} & c_{03} & c_{04} \\
c_{10} & c_{11} & c_{12} & c_{13} & c_{14} \\
c_{20} & c_{21} & c_{22} & c_{23} & c_{24} \\
c_{30} & c_{31} & c_{32} & c_{33} & c_{34} \\
c_{40} & c_{41} & c_{42} & c_{43} & c_{44}
\end{array}\right] .
$$

The rows of the transition matrix represent the origin state $(A)$, and the columns represent the destination state $(B)$. For example, $c_{21}$ is the number of workers who were in the bottom $20 \%$ of the overall-earnings distribution in year $t-1$ and transition to the eligible but no-reported-earnings category in year $t$.

To compute the total net inflows into an employment category, we first introduce some notation. Let $\iota$ be a $(5 \times 1)$ column vector of ones. Then

$$
\begin{aligned}
& C_{A} \cdot=C_{A B} \cdot \iota=\text { outflows }+ \text { stayers }, \\
& C_{\cdot B}=C_{A B}^{T} \cdot \iota=\text { inflows }+ \text { stayers }
\end{aligned}
$$

Net inflows into each employment state $\Delta_{A B}^{C}$ are defined as

$$
\begin{align*}
\Delta_{A B}^{C} & \equiv B-A \\
& =C_{\cdot B}-C_{A} \cdot \\
& =\underbrace{C_{A B}^{T} \cdot \iota}_{\text {inflows }+ \text { stayers }}-\underbrace{C_{A B} \cdot \iota}_{\text {ouflows }+ \text { stayers }}  \tag{E1}\\
& =\underbrace{\left(C_{A B}^{T}-C_{A B}\right) \cdot \iota}_{\text {inflows }- \text { outlows }=\text { net inflows }} .
\end{align*}
$$

Note the position of the stayers on the main diagonal. When we take the difference between $C_{A B}^{T}$ and $C_{A B}$, the resulting matrix will have zeros on the main diagonal, showing that the stayers do not directly affect the earnings distribution except through changes in average earnings. It should also be noted there is a direct relationship between the number of outflows and the number of stayers. If more workers leave a given category, then there will be fewer stayers, ceteris paribus.

Table E1 provides descriptive statistics on the individuals in each earnings category. It is expanded in the main text in table 5, which shows the net change in workers between the previous year and the current year from 2005 to 2013.

The flows of workers affect the earnings distribution, but the average earnings of each category and the change in average earnings for stayers also affect the change in the earnings distribution. Here we show the complete decomposition of the change in the earnings distribution. Table E2 shows the earnings changes we decompose here. Unlike table 5, the decomposition for earnings does not include net inflows into the eligible-worker frame or net inflows to inactive status. As we show below, these flows have no associated earnings and therefore have a weight of zero.

The corresponding earnings transition matrix for a given transition matrix of counts $C_{A B}$ is

$$
E_{A B}=\left[\begin{array}{ccccc}
0 & 0 & e_{02} & e_{03} & e_{04} \\
0 & 0 & e_{12} & e_{13} & e_{14} \\
e_{20} & e_{21} & e_{22} & e_{23} & e_{24} \\
e_{30} & e_{31} & e_{32} & e_{33} & e_{34} \\
e_{40} & e_{41} & e_{42} & e_{43} & e_{44}
\end{array}\right] \text {. }
$$

Unlike the transition matrix of counts, each element of the transition matrix of earnings has two associated total earnings values, the total earnings for the workers in period $A$ and the total earnings for those same workers
in period $B$. Each element of the earnings transition matrix is an ordered pair of elements. For example, $e_{23}=\left\{e_{23}^{A}, e_{23}^{B}\right\}$ represents the earnings of workers moving from the bottom $20 \%$ to the middle $60 \%$ of the earnings distribution. The first element is the total earnings in the previous period (when each worker is in the bottom 20\%), and the second element is the total earnings in the current period (when each worker is in the middle 60\%). Elements with an ordered pair of two zeros are shown as zeros in the earnings transition matrix.

Applying the net inflow formulas for the counts to the earnings transition matrix,

$$
\begin{equation*}
\Delta_{A B}^{E}=\underbrace{\left(E_{A B}^{\prime}-E_{A B}\right) \cdot i}_{\text {net inflows }}, \tag{E2}
\end{equation*}
$$

and choosing the appropriate earnings value from each tuple, using an $A$ or $B$ superscript to indicate the first or second element chosen, respectively, we have

$$
\Delta_{A B}^{E}=\left[\begin{array}{ccccc}
(0-0) & (0-0) & \left(e_{20}^{B}-e_{02}^{A}\right) & \left(e_{30}^{B}-e_{03}^{A}\right) & \left(e_{40}^{B}-e_{04}^{A}\right) \\
(0-0) & (0-0) & \left(e_{21}^{B}-e_{12}^{A}\right) & \left(e_{31}^{B}-e_{13}^{A}\right) & \left(e_{41}^{B}-e_{14}^{A}\right) \\
\left(e_{02}^{B}-e_{20}^{A}\right) & \left(e_{12}^{B}-e_{21}^{A}\right) & \left(e_{22}^{B}-e_{22}^{A}\right) & \left(e_{32}^{B}-e_{23}^{A}\right) & \left(e_{42}^{B}-e_{24}^{A}\right) \\
\left(e_{03}^{B}-e_{30}^{A}\right) & \left(e_{13}^{B}-e_{31}^{A}\right) & \left(e_{23}^{B}-e_{32}^{A}\right) & \left(e_{33}^{B}-e_{33}^{A}\right) & \left(e_{43}^{B}-e_{34}^{A}\right) \\
\left(e_{04}^{B}-e_{40}^{A}\right) & \left(e_{14}^{B}-e_{41}^{A}\right) & \left(e_{24}^{B}-e_{42}^{A}\right) & \left(e_{34}^{B}-e_{43}^{A}\right) & \left(e_{44}^{B}-e_{44}^{A}\right)
\end{array}\right] \cdot i .
$$

Table E1
Descriptive Statistics by Earnings Categories

|  | Eligible, No <br> Earn <br> $(1)$ | Bottom <br> $20 \%$ <br> $(2)$ | Middle $60 \%$ <br> $(3)$ | Top 20\% <br> $(4)$ | Total <br> $(5)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Number of Eligible Workers |  |  |  |  |  |
|  | $83,200,954$ | $27,062,314$ | $82,821,341$ | $26,678,860$ | $219,763,469$ |  |
| 2004 | $83,819,319$ | $27,376,301$ | $84,079,363$ | $26,885,106$ | $222,160,089$ |  |
| 2005 | $84,357,718$ | $27,598,826$ | $84,946,369$ | $27,818,665$ | $224,721,578$ |  |
| 2006 | $85,518,594$ | $27,800,774$ | $85,576,064$ | $28,657,580$ | $227,553,012$ |  |
| 2007 | $88,245,425$ | $28,120,283$ | $85,548,690$ | $28,440,617$ | $230,355,015$ |  |
| 2008 | $94,864,949$ | $28,119,169$ | $81,894,162$ | $27,935,033$ | $232,813,313$ |  |
| 2009 | $96,959,047$ | $28,154,014$ | $81,314,722$ | $27,876,922$ | $234,304,705$ |  |
| 2010 | $96,619,700$ | $28,498,111$ | $82,538,961$ | $27,773,225$ | $235,429,997$ |  |
| 2011 | $96,068,987$ | $28,269,636$ | $83,930,862$ | $28,214,827$ | $236,484,312$ |  |
| 2012 | $96,151,327$ | $28,119,381$ | $84,707,469$ | $28,838,761$ | $237,816,938$ |  |
| 2013 |  |  |  |  |  |  |

Table E1 (Continued)

| Year | Eligible, No Earn <br> (1) | Bottom 20\% (2) | Middle 60\% <br> (3) | Top 20\% <br> (4) | Total <br> (5) |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Total Earnings (Millions of Real [2000] Dollars) |  |  |  |  |
| 2004 |  | 76,178 | 1,959,201 | 2,351,882 | 4,387,260 |
| 2005 |  | 77,118 | 1,984,925 | 2,407,259 | 4,469,302 |
| 2006 |  | 77,653 | 2,006,111 | 2,529,269 | 4,613,033 |
| 2007 |  | 78,142 | 2,021,497 | 2,636,516 | 4,736,155 |
| 2008 |  | 78,716 | 2,012,397 | 2,576,185 | 4,667,298 |
| 2009 |  | 77,793 | 1,923,326 | 2,488,291 | 4,489,410 |
| 2010 |  | 77,788 | 1,901,588 | 2,524,307 | 4,503,683 |
| 2011 |  | 79,000 | 1,918,544 | 2,542,238 | 4,539,782 |
| 2012 |  | 78,880 | 1,947,808 | 2,625,836 | 4,652,524 |
| 2013 |  | 78,850 | 1,969,953 | 2,657,238 | 4,706,041 |
|  | Average Earnings per Worker ( $e_{i t}>0$ ) |  |  |  |  |
| 2004 |  | 2,815 | 23,656 | 88,155 | 32,126 |
| 2005 |  | 2,817 | 23,608 | 89,539 | 32,306 |
| 2006 |  | 2,814 | 23,616 | 90,920 | 32,865 |
| 2007 |  | 2,811 | 23,622 | 92,001 | 33,345 |
| 2008 |  | 2,799 | 23,523 | 90,581 | 32,843 |
| 2009 |  | 2,767 | 23,486 | 89,074 | 32,544 |
| 2010 |  | 2,763 | 23,386 | 90,552 | 32,791 |
| 2011 |  | 2,772 | 23,244 | 91,536 | 32,705 |
| 2012 |  | 2,790 | 23,207 | 93,066 | 33,134 |
| 2013 |  | 2,804 | 23,256 | 92,141 | 33,219 |
|  | Cumulative Change (2004-13) |  |  |  |  |
| Variable |  |  |  |  |  |
| Number of workers | 12,950,373 | 1,057,067 | 1,886,128 | 2,159,901 | 18,053,469 |
| Percent | 14.4 | 3.8 | 2.3 | 7.8 | 7.9 |
| Total Earnings |  | 2,671 | 10,752 | 305,357 | 318,780 |
| Percent |  | 3.4 | . 5 | 12.2 | 7.0 |
| Average Earnings |  | -11 | -400 | 3,986 | -175 |
| Percent |  | -. 4 | -1.7 | 4.4 | -. 9 |

NOTE.-The cumulative change in average earnings includes workers with $e_{i t}=0$ (col. 1 ) in the denominator. The overall change for the entire period for workers with $e_{i t}>0$ is $3.3 \%$.

Table E2
Earnings Associated with Exit from and Entry into Each Earnings Category

| Year | $\begin{aligned} & \text { Earn } \\ & t-1 \end{aligned}$ | Earn $t$ | Net Change | Stayers | Outflows | Inflows | Inflows Outflows | Net Change |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bottom 20\% of the Overall UI Earnings Distribution |  |  |  |  |  |  |  |
| 2005 | 76,178 | 77,118 | 939 | 1,625 | 41,849 | 41,164 | -685 | 939 |
| 2006 | 77,118 | 77,653 | 535 | 1,752 | 42,340 | 41,123 | -1,217 | 535 |
| 2007 | 77,653 | 78,142 | 489 | 1,553 | 42,415 | 41,351 | -1,065 | 489 |
| 2008 | 78,142 | 78,716 | 575 | 337 | 41,662 | 41,900 | 237 | 575 |
| 2009 | 78,716 | 77,793 | -923 | -1,193 | 41,681 | 41,951 | 270 | -923 |
| 2010 | 77,793 | 77,788 | -5 | 1,401 | 42,571 | 41,165 | -1,406 | -5 |
| 2011 | 77,788 | 79,000 | 1,212 | 1,948 | 42,359 | 41,622 | -736 | 1,212 |
| 2012 | 79,000 | 78,880 | -120 | 2,680 | 43,350 | 40,550 | -2,800 | -120 |
| 2013 | 78,880 | 78,850 | -30 | 2,637 | 42,914 | 40,246 | -2,668 | -30 |
|  | Middle 60\% of the Overall UI Earnings Distribution |  |  |  |  |  |  |  |
| 2005 | 1,959,201 | 1,984,925 | 25,725 | 37,258 | 278,555 | 267,021 | -11,534 | 25,725 |
| 2006 | 1,984,925 | 2,006,111 | 21,186 | 55,382 | 292,830 | 258,634 | -34,196 | 21,186 |
| 2007 | 2,006,111 | 2,021,497 | 15,386 | 53,012 | 296,600 | 258,975 | -37,626 | 15,386 |
| 2008 | 2,021,497 | 2,012,397 | -9,101 | 15,411 | 288,018 | 263,506 | -24,512 | -9,101 |
| 2009 | 2,012,397 | 1,923,326 | -89,071 | 4,842 | 331,453 | 237,541 | -93,912 | -89,071 |
| 2010 | 1,923,326 | 1,901,588 | -21,738 | 23,095 | 289,271 | 244,438 | -44,833 | -21,738 |
| 2011 | 1,901,588 | 1,918,544 | 16,956 | 22,643 | 263,326 | 257,639 | -5,687 | 16,956 |
| 2012 | 1,918,544 | 1,947,808 | 29,264 | 47,349 | 266,666 | 248,581 | -18,085 | 29,264 |
| 2013 | 1,947,808 | 1,969,953 | 22,144 | 58,469 | 273,520 | 237,196 | -36,324 | 22,144 |

Top 20\% of the Overall UI Earnings Distribution

| 2005 | $2,351,882$ | $2,407,259$ | 55,377 | 64,813 | 245,494 | 236,058 | $-9,436$ | 55,377 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2006 | $2,407,259$ | $2,529,269$ | 122,010 | 88,284 | 227,727 | 261,453 | 33,726 | 122,010 |
| 2007 | $2,529,269$ | $2,636,516$ | 107,247 | 86,390 | 240,848 | 261,705 | 20,857 | 107,247 |
| 2008 | $2,636,516$ | $2,576,185$ | $-60,330$ | $-15,291$ | 271,995 | 226,955 | $-45,040$ | $-60,330$ |
| 2009 | $2,576,185$ | $2,488,291$ | $-87,894$ | $-22,790$ | 291,186 | 226,082 | $-65,104$ | $-87,894$ |
| 2010 | $2,488,291$ | $2,524,307$ | 36,016 | 67,434 | 246,006 | 214,587 | $-31,418$ | 36,016 |
| 2011 | $2,524,307$ | $2,542,238$ | 17,931 | 44,185 | 230,451 | 204,197 | $-26,254$ | 17,931 |
| 2012 | $2,542,238$ | $2,625,836$ | 83,598 | 78,243 | 214,172 | 219,527 | 5,355 | 83,598 |
| 2013 | $2,625,836$ | $2,657,238$ | 31,403 | 28,123 | 217,801 | 221,081 | 3,280 | 31,403 |

Note.-The estimates are based on the authors' calculations using transitions into and out of the eligibleworkers frame and between categories of the earnings distributions, including inactive workers. Earnings values are in millions of real (2000) dollars.

The sum of each row in the matrix is the net inflow for each category of the earnings/inactivity distribution. The sum of the first two rows is zero; each element of the first two rows is zero, there are no earning when not eligible or eligible but inactive. Multiplying each element of the next three rows by a conformable vector of ones we can separate each total earnings value into the product of average earnings and the counts for that value. For example, the net inflows between period $A$ and period $B$ for earnings category two is

$$
\begin{align*}
\Delta_{A B}^{E 2}= & \left(\bar{e}_{02}^{B} \cdot c_{02}-\bar{e}_{20}^{A} \cdot c_{20}\right)+\left(\bar{e}_{12}^{B} \cdot c_{12}-\bar{e}_{21}^{A} \cdot c_{21}\right) \\
& +\left(\bar{e}_{22}^{B}-\bar{e}_{22}^{A}\right) \cdot c_{22}+\left(\bar{e}_{32}^{B} \cdot c_{32}-\bar{e}_{23}^{A} \cdot c_{23}\right)+\left(\bar{e}_{42}^{B} \cdot c_{42}-\bar{e}_{24}^{A} \cdot c_{24}\right) . \tag{E3}
\end{align*}
$$

The year-to-year change in the earnings associated with a given part of the earnings distribution is a linear function (weighted sum) of the average earnings and the transition counts. Table E2 shows the results after first grouping the stayers, inflows, and outflows together for the bottom $20 \%$, middle $60 \%$, and top $20 \%$ categories.
The change in earnings reduces to a simple (signed) sum of the counts if the average earnings is the same for each flow, that is, $\left(\bar{e}_{2}^{*}=\bar{e}_{02}^{B}=\bar{e}_{20}^{A}=\right.$ $\left.\bar{e}_{12}^{B}=\bar{e}_{21}^{A}=\bar{e}_{22}^{B}=\bar{e}_{22}^{A}=\bar{e}_{32}^{B}=\bar{e}_{23}^{A}=\bar{e}_{42}^{B}=\bar{e}_{24}^{A}\right)$.

$$
\begin{equation*}
\Delta_{A B}^{E 2}=\bar{e}_{2}^{*} \cdot[\underbrace{\left(c_{02}+c_{12}+c_{32}+c_{42}\right)}_{\text {inflows }}-\underbrace{\left(c_{20}+c_{21}+c_{23}+c_{24}\right)}_{\text {oufflows }}] . \tag{E4}
\end{equation*}
$$

Although the simple formula will rarely hold in practice, it is useful as the earnings change for each category is now a scaled function of the counts. For the data in this paper, a different constant average earnings value for each category does a reasonable job approximating the gross outflows and inflows. However, when using a constant the individual flows are not always scaled correctly, since the weights (average earnings) differ substantially in some cases. Even though there are level differences across flows, the average earnings values are for the most part stable over time, allowing the counts to proxy for the change in the earnings distribution over time once the appropriate scale factor is known for a given flow. Table E3 shows the average earnings and measures of variability for each of the flows.

Figures E1-E3 repeat the analysis shown in the main text in figures 1012.

Table E3
Average Earnings and Variability by Transition Type

|  | Flows from Bottom 20\% |  |  |  |  | Flows to Bottom 20\% |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | et_2_2_A et_2_0 et_2_1 et_2_3 et_2_4 |  |  |  |  | et_2_2_B | et_0_2 | et_1_2 | et_3_2 | et_4_2 |
| Mean | 2,706 | 2,620 | 2,053 | 3,631 | 3,377 | 2,814 | 2,427 | 2,202 | 3,474 | 2,963 |
| IQR | 22 | 17 | 30 | 48 | 15 | 24 | 244 | 14 | 20 | 67 |
| Minimum | 2,657 | 2,600 | 2,015 | 3,571 | 3,362 | 2,712 | 2,267 | 2,150 | 3,365 | 2,804 |
| Maximum | 2,802 | 2,678 | 2,087 | 3,747 | 3,399 | 2,873 | 2,569 | 2,227 | 3,518 | 3,041 |
|  | Flows from Middle 60\% |  |  |  |  | Flows to Middle 60\% |  |  |  |  |
|  | et_3_3_A et_3_0 et_3_1 et_3_2 et_3_4 et_3_3_B et_0_3 et_1_3 et_2_3 et_4_3 |  |  |  |  |  |  |  |  |  |
| Mean | 23,940 | 18,680 | 16,720 | 14,220 | 37,430 | 24,450 | 11,672 | 15,240 | 12,980 | 35,340 |
| IQR | 160 | 442 | 166 | 181 | 228 | 297 | 1,685 | 429 | 277 | 507 |
| Minimum | 23,540 | 18,110 | 16,560 | 13,850 | 36,910 | 24,220 | 10,370 | 14,950 | 12,540 | 34,260 |
| Maximum | 24,160 | 19,391 | 16,910 | 14,950 | 38,200 | 24,720 | 12,290 | 15,510 | 13,210 | 35,970 |
|  | Flows from Top 20\% |  |  |  |  | Flows to Top 20\% |  |  |  |  |
|  | et_4_4_A et_4_0 |  | et_4_1 | et_4_2 | et_4_3 | et_4_4_B | et_0_4 | et_1_4 | et_2_4 | et_3_4 |
| Mean | 94,160 | 113,200 | 107,220 | 80,970 | 60,900 | 96,080 | 96,160 | 94,320 | 73,770 | 57,510 |
| IQR | 1,922 | 3,219 | 8,788 | 2,596 | 1,117 | 2,086 | 6,893 | 1,409 | 3,017 | 152 |
| Minimum | 91,810 | 107,440 | 97,650 | 78,800 | 59,930 | 93,720 | 78,540 | 91,320 | 69,450 | 56,820 |
| Maximum | 96,100 | 118,500 | 117,400 | 82,800 | 61,790 | 98,010 | 108,200 | 98,800 | 81,490 | 57,780 |

Note.-Dominant flows are in bold. The estimates are the weighted annual mean, interquartile range (IQR), minimum, and maximum of the mean annual earnings in each category. Statistics are over nine pairs of years from 2004-2005 to 2012-2013.

categories of the earnings distribution, including inactivity. A color version of this figure is available online.

Fig. E2.-Earnings flows out of and into the middle $60 \%$. Estimates based on the authors' calculations using transitions into and out of categories of the earnings distribution, including inactivity. A color version of this figure is available online.

categories of the earnings distribution, including inactivity. A color version of this figure is available online.

## E2. AKM Decomposition

We estimate the following AKM model:

$$
\begin{equation*}
\ln y_{i j t}=x_{i t} \beta+\theta_{i}+\psi_{j}+\varepsilon_{i j t}, \tag{E5}
\end{equation*}
$$

where $y_{i j t}$ is $\log$ real annual earnings of person $i$ employed at firm $j$ in year $t, \theta_{i}$ is individual $i$ 's person effect, $\psi_{j}$ is firm $j$ 's fixed effect, and $x_{i t}$ includes controls for experience, labor force attachment, and aggregate labor market conditions detailed in table E4. Estimates of all of these controls are provided in table E7.

Table E4
AKM (Abowd-Kramarz-Margolis) Model Specification

```
Actual labor force experience:
    [exp, \(\left.\exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) female \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) black \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) Hispanic \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) female \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) black \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) Hispanic \(\} \times\left[\exp , \exp ^{2} / 10, \exp ^{3} / 100, \exp ^{4} / 1000\right]\)
Labor force attachment:
    weeks by hours categories ( 41 total, 40 hours by \(50-52\) weeks excluded)
    sixq dummies ( 9 total: sixq2-sixq6, sixq_4th, sixq_left, sixq_right, sixq_inter;
        sixq1 excluded)
    \(\mathbb{1}\{\) female \(\} \times[\) sixq dummies \(]\)
    \(\mathbb{1}\{\) black \(\} \times\) [sixq dummies]
    \(\mathbb{1}\{\) Hispanic \(\} \times\) [sixq dummies]
    \(\mathbb{1}\{\) foreign born \(\} \times[\) sixq dummies \(]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) female \(\} \times[\) sixq dummies \(]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{b\) back \(\} \times[\) sixq dummies \(]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) Hispanic \(\} \times\) [sixq dummies \(]\)
Aggregate labor market conditions:
    \(\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) female \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) black \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) Hispanic \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) female \(\} \times\left[u_{t}, 1\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) black \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
    \(\mathbb{1}\{\) foreign born \(\} \times \mathbb{1}\{\) Hispanic \(\} \times\left[u_{t}, \mathbb{1}\left\{u_{t}>u_{t-1}\right\} \times u_{t}\right]\)
Incomplete 2014Q1 data controls:
    [right: indicator for incomplete data in 2014Q1 in one state and the District of Columbia]
    \(\mathbb{1}\{\) female \(\} \times\) right \(]\)
    \(\mathbb{1}\{\) black \(\} \times[\) right \(]\)
```

Table E4 (Continued)

```
\mathbb{1}{H\mathrm{ Hspanic } }\times [right]
\mathbb{{}{\mathrm{ foreign born }\times[\mathrm{ right]}
\mathbb{{foreign born }}\times\mathbb{1}{\mathrm{ female } }\times[\mathrm{ right }]
\mathbb{1}{\mathrm{ foreign born }}\times\mathbb{1}{\mathrm{ black }}\times[\mathrm{ right]}
\mathbb{1}{foreign born}}\times\mathbb{1}{\mathrm{ Hispanic } }\times[\mathrm{ right ]
```

Note.-The dependent variable is the natural logarithm of real annual earnings. Before converting nominal to real earnings, the dependent variable was winsorized each year at the 0.01 and 99.99 percentiles. The winsorized data were used in the estimation of the AKM effects and in the calculation of bins in the overall, firm, nonfirm, and skill distributions. The specification also includes a fixed worker effect for each individual in the eligible-workers frame and a fixed firm effect for each employer in that frame. The AKM estimation occurs only during date regime 4 , which is the complete population; however, our labor force attachment variables require an additional quarter to calculate (2014Q1), which is missing for one state and the District of Columbia. There are two sets of labor force attachment controls. See table E5 for definitions of the weeks worked and the usual weekly hours categories, and see table E6 for the definitions of the sixq dummies. The "right" variable controls for the case where a sixq variable is set to zero due to data availability instead of actual labor force attachment.

Table E5
Weeks Worked and Usual Weekly Hours Categories

|  | Weeks Worked | Usual Weekly Hours |
| :--- | :---: | :---: |
| 1 | $1-13$ | $1-19$ |
| 2 | $14-26$ | $20-29$ |
| 3 | $27-39$ | $30-34$ |
| 4 | $40-47$ | $35-39$ |
| 5 | $48-49$ | 40 |
| 6 | $50-52$ | $41-49$ |
| 7 |  | $\geq 50$ |

Note.-This table provides the definitions of the weeks worked and usual weekly hours categories used as controls in the model specified in table E4.

Table E6 Quarterly Employment Pattern Variable Definitions

| Variable | Definition |
| :--- | :--- |
| sixq1 | Dummy for working 1 of 6 quarters in sixq window |
| sixq2 | Dummy for working 2 of 6 quarters in sixq window |
| sixq3 | Dummy for working 3 of 6 quarters in sixq window |
| sixq4 | Dummy for working 4 of 6 quarters in sixq window |
| sixq5 | Dummy for working 5 of 6 quarters in sixq window |
| sixq6 | Dummy for working 6 of 6 quarters in sixq window |
| sixq_4th | Dummy for working in fourth quarter of current year |
| sixq_left | Dummy for if sixq in (100000, 110000, 111000, 111100, 111110, 111111) |
| sixq_right | Dummy for if sixq in (000001,000011,000111,001111,011111,111111) |
| sixq_inter | Dummy for if sixq in (10111, 110111, 111011,111101,100111,110011, |
|  | $111001,100011,110001)$ |

Note.-This table provides the definitions of the sixq dummies used as controls in the model specified in table E4.

Table E7
AKM (Abowd-Kramarz-Margolis) Model Estimates

|  | Control | Estimate |  | Control | Estimate |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | experience | . 0973 | 86 | female_sixq5 | . 0474 |
| 2 | experience_2 | -. 0379 | 87 | female_sixq6 | . 0545 |
| 3 | experience_3 | . 0070 | 88 | female_sixq_4th | -. 0149 |
| 4 | experience_4 | -. 0006 | 89 | female_sixq_left | -. 0028 |
| 5 | female_experience | -. 0122 | 90 | female_sixq-right | . 0333 |
| 6 | female_experience_2 | . 0044 | 91 | female_sixq_inter | . 0265 |
| 7 | female_experience_3 | -. 0005 | 92 | black_sixq2 | . 0896 |
| 8 | female_experience_4 | . 0000 | 93 | black_sixq3 | . 1388 |
| 9 | black_experience | -. 0470 | 94 | black_sixq4 | . 1584 |
| 10 | black_experience_2 | . 0211 | 95 | black_sixq5 | . 1445 |
| 11 | black_experience_3 | -. 0046 | 96 | black_sixq6 | . 2161 |
| 12 | black_experience_4 | . 0004 | 97 | black_sixq_4th | . 0250 |
| 13 | hispanic_experience | -. 0372 | 98 | black_sixq_left | -. 1004 |
| 14 | hispanic_experience_2 | . 0201 | 99 | black_sixq_right | -. 0761 |
| 15 | hispanic_experience_3 | -. 0049 | 100 | black_sixq_inter | -. 0829 |
| 16 | hispanic_experience_4 | . 0005 | 101 | hispanic_sixq2 | . 0962 |
| 17 | fbstat_experience | -. 0424 | 102 | hispanic_sixq3 | . 1280 |
| 18 | fbstat_experience_2 | . 0238 | 103 | hispanic_sixq4 | . 1386 |
| 19 | fbstat_experience_3 | -. 0058 | 104 | hispanic_sixq5 | . 1101 |
| 20 | fbstat_experience_4 | . 0005 | 105 | hispanic_sixq6 | . 1990 |
| 21 | female_fbstat_experience | . 0007 | 106 | hispanic_sixq_4th | . 0269 |
| 22 | female_fbstat_experience_2 | . 0008 | 107 | hispanic_sixq_left | -. 0927 |
| 23 | female_fbstat_experience_3 | -. 0004 | 108 | hispanic_sixq_right | -. 0933 |
| 24 | female_fbstat_experience_4 | . 0000 | 109 | hispanic_sixq_inter | -. 1123 |
| 25 | black_fbstat_experience | . 0179 | 110 | fbstat_sixq2 | -. 0108 |
| 26 | black_fbstat_experience_2 | -. 0086 | 111 | fbstat_sixq3 | -. 0361 |
| 27 | black_fbstat_experience_3 | . 0021 | 112 | fbstat_sixq4 | -. 0602 |
| 28 | black_fbstat_experience_4 | -. 0002 | 113 | fbstat_sixq5 | -. 1155 |
| 29 | hispanic_fbstat .experience | . 0146 | 114 | fbstat_sixq6 | -. 1533 |
| 30 | hispanic_fbstat_experience_2 | -. 0140 | 115 | fbstat_sixq_4th | . 0377 |
| 31 | hispanic_fbstat_experience_3 | . 0044 | 116 | fbstat _sixq _left | . 0292 |
| 32 | hispanic_fbstat_experience_4 | -. 0005 | 117 | fbstat_sixq_right | . 0079 |
| 33 | WKS1 and HRS1 | -. 3017 | 118 | fbstat _sixq_inter | . 0724 |
| 34 | WKS1 and HRS2 | -. 2561 | 119 | female_fbstat_sixq2 | -. 0245 |
| 35 | WKS1 and HRS3 | -. 2044 | 120 | female_fbstat_sixq3 | -. 0390 |
| 36 | WKS1 and HRS4 | -. 1260 | 121 | female_fbstat_sixq4 | -. 0308 |
| 37 | WKS1 and HRS5 | -. 0625 | 122 | female_fbstat_sixq5 | -. 0262 |
| 38 | WKS1 and HRS6 | . 0782 | 123 | female_fbstat_sixq6 | -. 0374 |
| 39 | WKS1 and HRS7 | . 1381 | 124 | female_fbstat_sixq_4th | . 0067 |
| 40 | WKS2 and HRS1 | -. 2907 | 125 | female_fbstat_sixq_left | . 0100 |
| 41 | WKS2 and HRS2 | -. 1951 | 126 | female_fbstat_sixq_right | -. 0028 |
| 42 | WKS2 and HRS3 | -. 1122 | 127 | female_fbstat_sixq_inter | . 0041 |
| 43 | WKS2 and HRS4 | -. 0100 | 128 | black_fbstat_sixq2 | . 0007 |
| 44 | WKS2 and HRS5 | . 0831 | 129 | black_fbstat_sixq3 | . 0243 |
| 45 | WKS2 and HRS6 | . 1570 | 130 | black_fbstat_sixq4 | . 0403 |
| 46 | WKS2 and HRS7 | . 1734 | 131 | black_fbstat_sixq5 | . 0770 |
| 47 | WKS3 and HRS1 | -. 3176 | 132 | black_fbstat_sixq6 | . 0787 |
| 48 | WKS3 and HRS2 | -. 1633 | 133 | black_fbstat_sixq_4th | -. 0270 |

Table E7 (Continued)

|  | Control | Estimate |  | Control | Estimate |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | WKS3 and HRS3 | -. 0929 | 134 | black_fbstat_sixq_left | . 0341 |
| 50 | WKS3 and HRS4 | -. 0090 | 135 | black_fbstat_sixq_right | . 0483 |
| 51 | WKS3 and HRS5 | . 0628 | 136 | black_fbstat_sixq_inter | . 0437 |
| 52 | WKS3 and HRS6 | . 1167 | 137 | hispanic_fbstat_sixq2 | . 0099 |
| 53 | WKS3 and HRS7 | . 1404 | 138 | hispanic_fbstat_sixq3 | -. 0025 |
| 54 | WKS4 and HRS1 | -. 3661 | 139 | hispanic_fbstat_sixq4 | . 0027 |
| 55 | WKS4 and HRS2 | -. 2028 | 140 | hispanic_fbstat_sixq5 | . 0529 |
| 56 | WKS4 and HRS3 | -. 1196 | 141 | hispanic_fbstat_sixq6 | . 0141 |
| 57 | WKS4 and HRS4 | -. 0685 | 142 | hispanic_fbstat_sixq_4th | -. 0252 |
| 58 | WKS4 and HRS5 | -. 0223 | 143 | hispanic_fbstat_sixq_left | . 0414 |
| 59 | WKS4 and HRS6 | . 0011 | 144 | hispanic_fbstat_sixq_right | . 0278 |
| 60 | WKS4 and HRS7 | . 0161 | 145 | hispanic_fbstat_sixq_inter | . 0434 |
| 61 | WKS5 and HRS1 | -. 3451 | 146 | urate | -. 0095 |
| 62 | WKS5 and HRS2 | -. 1839 | 147 | urate_up | . 0017 |
| 63 | WKS5 and HRS3 | -. 0999 | 148 | female_urate | . 0034 |
| 64 | WKS5 and HRS4 | -. 0550 | 149 | female_urate_up | . 0006 |
| 65 | WKS5 and HRS5 | -. 0145 | 150 | black_urate | . 0045 |
| 66 | WKS5 and HRS6 | . 0028 | 151 | black_urate_up | -. 0001 |
| 67 | WKS5 and HRS7 | . 0183 | 152 | hispanic_urate | . 0015 |
| 68 | WKS6 and HRS1 | -. 3237 | 153 | hispanic_urate_up | . 0005 |
| 69 | WKS6 and HRS2 | -. 1716 | 154 | fbstat _urate | -. 0000 |
| 70 | WKS6 and HRS3 | -. 0929 | 155 | fbstat _urate_up | . 0003 |
| 71 | WKS6 and HRS4 | -. 0361 | 156 | female_fbstat_urate | -. 0004 |
| 72 | WKS6 and HRS6 | . 0223 | 157 | female_fbstat_urate_up | -. 0001 |
| 73 | WKS6 and HRS7 | . 0320 | 158 | black_fbstat_urate | -. 0059 |
| 74 | sixq2 | 1.1170 | 159 | black_fbstat_urate_up | . 0009 |
| 75 | sixq3 | 2.2170 | 160 | hispanic_fbstat_urate | -. 0032 |
| 76 | sixq4 | 2.7750 | 161 | hispanic_fbstat_urate_up | -. 0003 |
| 77 | sixq5 | 3.2910 | 162 | right | . 2083 |
| 78 | sixq6 | 3.6920 | 163 | female_right | . 0319 |
| 79 | sixq_4th | . 0323 | 164 | black_right | -. 0181 |
| 80 | sixq_left | -. 2940 | 165 | hispanic_right | -. 0051 |
| 81 | sixq_right | -. 1401 | 166 | fbstat _right | . 0060 |
| 82 | sixq_inter | -. 7029 | 167 | female_fbstat _right | -. 0273 |
| 83 | female_sixq2 | . 0250 | 168 | black _fbstat _right | . 0545 |
| 84 | female_sixq3 | . 0563 | 169 | hispanic_fbstat_right | -. 0139 |
| 85 | female_sixq4 | . 0544 |  |  |  |

Note.-The table presents the coefficient estimates of all of the controls listed in table E4. $N=$ $2,014,000,000$, jobs $=825,900,000$, persons $=200,700,000$, firms $=14,650,000$, and intercept $=6.098$, calculated after estimation. The equation includes one person effect for each person and firm effects for all firms, save one. Estimation and identification are performed as described in Abowd, Creecy, and Kramarz (2002). All observations in the complete frame, which has universal coverage over the period 2004-13, were used. Finite population standard errors are zero. The estimates and their associated standard errors have not been corrected for edit, imputation, and postprocessing uncertainty.

## E3. Analyzing Earnings Inequality Changes Using Only Firm Type and Nonfirm Type

In Section V, we use the AKM decomposition to create firm, nonfirm, and skill components of earnings. These components are used to create
firm-type, nonfirm-type, and skill-type bins that we subsequently employ to characterize the worker and firm contributions to changes in earnings inequality.

An earlier version of this paper used the nonfirm-type bins in a manner similar to the use of the skill-type bins in the main text. We discuss these results here for each nonfirm-type separately. We remind the reader that the nonfirm component contains the effects of changes in the labor force attachment, macroeconomic conditions, date regime boundaries, and the residual, all of which are excluded from the skill type in the main text.

Table E8 presents outcomes for workers in the bottom bin of the nonfirm component. Table E9 presents outcomes for workers in the middle bin of the nonfirm component distribution. Table E10 presents outcomes for workers in the top bin of the nonfirm component distribution.

The tables were created as follows. They are based on classifying workers in the previous year, that is, year $t-1$. Beginning in 2004 and ending in 2012, for every year that an eligible worker has positive earnings a single observation is added to one of the three tables. The appropriate table classification for each observation is determined by the nonfirm type for that year, which can vary over time as workers accumulate experience, work more or fewer hours during the quarter, receive a positive or negative aggregate demand shock, or have a large positive or negative residual. Within each nonfirm type, the earnings record is further classified based on the firm type, resulting in each earnings observation being classified into one of nine possible cells. ${ }^{58}$ Within each of the nonfirm-type $\times$ firm-type cells, we break down the results by the three possible overall-earnings outcomes (bottom, middle, and top). There are, thus, 27 cells for which we present information on the number of workers, average earnings for the previous year $(t-1)$, and average earnings for the current year $(t)$ by flow type. ${ }^{59}$

To fix ideas, we will take a detailed look at two rows in table E8. To be recorded in this table, the person must have been in the bottom bin (lowest bin) of the nonfirm-component distribution in the previous year, that is, $t-1$.

Consider the first row of the table. This row is in the panel labeled "Bottom Firm," indicating that this person is employed at a firm in the bottom bin of the firm component distribution in $t-1$. Persons in this row are also in the bottom bin of the overall-earnings distribution in year $t-1$, and the share of such persons (relative to those in the middle or top of the overallearnings distribution) is 1.000 , indicating that no person in the bottom of the nonfirm component distribution and the bottom of the firm component distribution is employed outside of the bottom bin of the overall-earnings

[^31]distribution. The flow labeled 2_0 is the movement from the bottom of the overall-earnings distribution (bin 2) to ineligible; that is, this is the flow out of the frame for persons at the bottom of the overall-earnings distribution. There were, on average, 59,554 such persons each previous year $(t-1)$. They represent $0.7 \%$ of the flows from bin 2 of the overall-earnings distribution. Average earnings in $t-1$ were $\$ 1,381$, of which $-\$ 1,463$ are attributed to the firm component of our decomposition and $\$ 2,844$ are attributed to the nonfirm component of our decomposition. There were no earnings in the current year $(t)$ because the person has moved out of the frame in $t$.

Next, consider the row labeled "Middle" in the "All Earnings" column in the "Middle Firm" panel with a 3_3 flow. All persons in this row were, once again, at the bottom of the nonfirm component distribution in year $t-1$. Of all such persons, $56 \%$ are employed by a firm in the middle of the firm component distribution. Of all persons at the bottom of the nonfirm component distribution and in the middle of the firm component distribution in year $t-1$, the proportion 0.159 were in the middle of the overall-earnings distribution. Among such persons, the 3_3 row shows those who remain in the middle of the overall-earnings distribution in the current year, $t$, of which there were, on average, $1,470,659$ in the nine pairs of years for which the table was constructed. Those who stayed in the middle of the overallearnings distribution represented $58.9 \%$ of all persons who were in the middle of the overall-earnings distribution in year $t-1$, on average. In year $t-1$, their earnings averaged $\$ 8,498$, of which $\$ 2,180$ is attributed to the firm component in our decomposition and $\$ 6,318$ is attributed to the nonfirm component. In the current year, year $t$, average earnings were $\$ 15,688$, of which $\$ 3,555$ is associated with the firm component and $\$ 12,132$ is associated with the nonfirm component.

We use these tables to investigate worker sorting directly by looking at the interaction of the nonfirm and firm type for each worker-year-earnings observation. If there were no sorting, the distribution of earnings observations across firm types would be similar for all three tables because outcomes would be unaffected by which part of the nonfirm component distribution an individual occupied given his place in the overall-earnings distribution. This hypothesis is clearly not supported by the data. For example, again using table E8 showing the bottom of the nonfirm-type distribution, about $33 \%$ of the earnings observations are in firms at the bottom of the firm-type distribution, $56 \%$ are in firms of the middle type, and only $11 \%$ are in top firms. In comparison, tables E9 and E10 show that persons in the middle and top of the nonfirm-type distributions are much less likely to be employed at firms in the bottom type ( $14 \%$ and $24 \%$, respectively) and much more likely to be employed at top firms ( $23 \%$ and $20 \%$, respectively). Interestingly, the relationship is not monotonic; workers in the middle are more likely to work at both middle and top firms relative to top workers.

Next, we focus on each nonfirm type in turn, starting with the earnings observations for workers in the bottom of the nonfirm component distribution in table E8. For workers at the bottom of the nonfirm component distribution, working at a high-paying firm has two advantages: higher earnings than otherwise and a greater chance of moving to a higher bin in the overall-earnings distribution. For example, a worker at the bottom of the nonfirm-component and overall-earnings distributions has a probability of moving to the middle of the overall-earnings distribution of $18 \%$ at a low-paying firm, $29.5 \%$ at a middle-paying firm, and $27.5 \%$ at a high-paying firm. Prior to the transition, the average worker with a low nonfirm component at a low-, middle-, and high-paying firm earns $\$ 2,084, \$ 3,556$, and $\$ 3,806$, respectively. ${ }^{60}$ After the transition, the average worker at a low-, mid-dle-, and high-paying firm earns $\$ 11,640, \$ 13,752$, and $\$ 18,017$, respectively. Most of the additional increase in earnings for workers employed at a toppaying employer in the previous year is due to working at a top-paying employer in the next year.

The vast majority ( $63 \%$ ) of workers in the middle of the nonfirm component distribution are employed at middle-paying firms, as table E9 shows. The next most prevalent outcomes for such workers are employment at topand bottom-paying firms, $23 \%$ and $14 \%$, respectively. Similar to workers at the bottom of the nonfirm type distribution, who also generally appear at the bottom of the overall-earnings distribution ( $84 \%$ ) when employed by middle-paying firms, the majority of workers in the middle of the nonfirm type distribution, no matter the firm type, are in the middle of the overallearnings distribution. However, in spite of the majority of earnings observations being in the middle of the overall-earnings distribution, average earnings differ substantially across firm types. A middle-type worker in bin 3 of the overall-earnings distribution who stays in bin 3 of the overall distribution (a 3_3 flow) at a bottom-type firm has $t-1$ earnings of $\$ 12,356$, a middle-type worker in a middle-type firm has $t-1$ earnings of $\$ 22,978$, and a middle-type worker at a top firm has $t-1$ earnings of $\$ 32,321$. Most of the difference is due to a larger firm effect, although the nonfirm component declines somewhat as a middle-type person is found in increasing firm types, giving back some of the gains. Similar to bottomtype workers, one of the additional benefits of finding employment at a high-paying firm is a greater probability of moving to the top of the earnings distribution ( $0.2 \%$ vs. $2.7 \%$ vs. $11.9 \%$ in rows 10,25 , and 40 , respectively).

[^32]Similar to bottom and middle nonfirm-type workers, table E10 shows that about $64 \%$ of top nonfirm-type workers are also in the top of the overallearnings distribution, but there is also a substantial minority in the middle. The differences between working at a middle- compared with a bottom-type firm are relatively small, but the gains from working at a top-type firm are very large. Somewhat surprisingly perhaps, there are a relatively large number of top-type workers at bottom- and middle-type firms. On average, these workers, especially in the middle, are employed at worse-paying firms than middle nonfirm-type workers.

Table E8
Earnings Associated with Flows by Firm Bin for Persons in the Bottom-Type Nonfirm Category

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (33\%) |  |  |  |  |  |  |  |
| Bottom (1.000): |  |  |  |  |  |  |  |  |
| 2_0 | 59,554 | . 7 | 1,381 | -1,463 | 2,844 |  |  |  |
| 2_1 | 2,441,375 | 26.8 | 1,102 | $-1,099$ | 2,201 |  |  |  |
| 2 _2 | 4,962,828 | 54.5 | 1,635 | -1,588 | 3,223 | 2,466 | -1,981 | 4,447 |
| 2_3 | 1,641,446 | 18.0 | 2,084 | -1,738 | 3,823 | 11,640 | -4,017 | 15,657 |
| 2_4 | 8,640 | . 1 | 1,513 | $-1,558$ | 3,071 | 78,157 | 8,958 | 69,199 |
| Middle (.000): |  |  |  |  |  |  |  |  |
| 3_0 | 0 | . 0 |  |  |  |  |  |  |
| 3_1 | 0 | . 0 |  |  |  |  |  |  |
| 3-2 | 0 | . 0 |  |  |  |  |  |  |
| 3_3 | 0 | . 0 |  |  |  |  |  |  |
| 3_4 | 0 | . 0 |  |  |  |  |  |  |
| Top (.000): |  |  |  |  |  |  |  |  |
| 4_0 | 0 | . 0 |  |  |  |  |  |  |
| 4_1 | 0 | . 0 |  |  |  |  |  |  |
| 4_2 | 0 | . 0 |  |  |  |  |  |  |
| 4_3 | 0 | . 0 |  |  |  |  |  |  |
| 4_4 | 0 | . 0 |  |  |  |  |  |  |
|  | Middle Firm (56\%) |  |  |  |  |  |  |  |
| Bottom (.841): |  |  |  |  |  |  |  |  |
| 2 _0 | 116,724 | . 9 | 2,660 | 72 | 2,588 |  |  |  |
| 2_1 | 3,613,606 | 27.3 | 2,289 | 42 | 2,247 |  |  |  |
| 2_2 | 5,565,538 | 42.0 | 2,784 | -145 | 2,929 | 2,799 | -594 | 3,392 |
| 2_3 | 3,911,555 | 29.5 | 3,556 | -27 | 3,583 | 13,752 | 561 | 13,191 |
| 2_4 | 36,073 | . 3 | 3,392 | 469 | 2,923 | 69,402 | 19,672 | 49,730 |
| Middle (.159): |  |  |  |  |  |  |  |  |
| 3-0 | 21,191 | . 8 | 8,381 | 2,189 | 6,193 |  |  |  |
| 3_1 | 428,729 | 17.2 | 8,384 | 2,249 | 6,135 |  |  |  |
| 3_2 | 554,068 | 22.2 | 8,153 | 1,893 | 6,260 | 3,321 | -14 | 3,336 |
| 3_3 | 1,470,659 | 58.9 | 8,498 | 2,180 | 6,318 | 15,688 | 3,555 | 12,132 |
| 3_4 | 21,549 | . 9 | 8,955 | 2,823 | 6,132 | 64,566 | 22,919 | 41,647 |

Table E8 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| Top (.000): |  |  |  |  |  |  |  |  |
| 4_0 | 0 | . 0 |  |  |  |  |  |  |
| 4_1 | 0 | . 0 |  |  |  |  |  |  |
| 4_2 | 0 | . 0 |  |  |  |  |  |  |
| 4_3 | 0 | . 0 |  |  |  |  |  |  |
| 4_4 | 0 | . 0 |  |  |  |  |  |  |
|  | Top Firm (11\%) |  |  |  |  |  |  |  |
| Bottom (.396): |  |  |  |  |  |  |  |  |
| 2_0 | 17,420 | 1.4 | 2,913 | 1,598 | 1,314 |  |  |  |
| 2_1 | 469,324 | 38.3 | 2,758 | 1,515 | 1,243 |  |  |  |
| 2_2 | 377,303 | 30.8 | 3,174 | 1,740 | 1,433 | 2,905 | 806 | 2,099 |
| 2_3 | 337,787 | 27.5 | 3,806 | 2,034 | 1,771 | 18,017 | 7,482 | 10,535 |
| 2_4 | 24,607 | 2.0 | 3,701 | 2,058 | 1,642 | 76,278 | 41,316 | 34,962 |
| Middle (.596): |  |  |  |  |  |  |  |  |
| 3-0 | 16,910 | . 9 | 12,121 | 7,299 | 4,822 |  |  |  |
| 3_1 | 375,155 | 20.3 | 12,082 | 7,280 | 4,802 |  |  |  |
| 3_2 | 243,668 | 13.2 | 11,573 | 6,756 | 4,817 | 3,134 | 774 | 2,360 |
| 3_3 | 1,108,356 | 60.0 | 13,551 | 8,484 | 5,067 | 20,030 | 10,749 | 9,281 |
| 3_4 | 102,240 | 5.5 | 15,785 | 10,529 | 5,255 | 70,117 | 42,636 | 27,481 |
| Top (.008): |  |  |  |  |  |  |  |  |
| 4_0 | 172 | . 7 | 97,790 | 93,786 | 4,005 |  |  |  |
| 4_1 | 1,924 | 7.6 | 96,408 | 92,599 | 3,809 |  |  |  |
| 4_2 | 498 | 2.0 | 93,690 | 89,588 | 4,103 | 2,376 | -53 | 2,430 |
| 4_3 | 4,217 | 16.7 | 65,091 | 60,669 | 4,422 | 32,200 | 28,313 | 3,887 |
| 4_4 | 18,478 | 73.1 | 108,698 | 104,482 | 4,216 | 117,522 | 110,839 | 6,683 |

Note.-See table 9.

Table E9
Earnings Associated with Flows by Firm Bin for Persons in the Middle-Type Nonfirm Category

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (14\%) |  |  |  |  |  |  |  |
| Bottom (.313): |  |  |  |  |  |  |  |  |
| 2_0 | 26,241 | . 7 | 4,596 | -7,583 | 12,179 |  |  |  |
| 2_1 | 352,516 | 9.4 | 4,627 | -6,141 | 10,768 |  |  |  |
| 2_2 | 2,005,303 | 53.6 | 4,676 | -6,627 | 11,303 | 3,590 | -4,861 | 8,452 |
| 2_3 | 1,352,780 | 36.2 | 5,199 | -5,937 | 11,137 | 11,278 | -7,815 | 19,093 |
| 2_4 | 4,255 | . 1 | 4,649 | -7,524 | 12,173 | 79,652 | $-16,894$ | 96,546 |
| Middle (.687): |  |  |  |  |  |  |  |  |
| 3-0 | 39,797 | . 5 | 11,198 | -9,855 | 21,053 |  |  |  |
| 3-1 | 312,400 | 3.8 | 10,551 | -8,857 | 19,408 |  |  |  |

Table E9 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| 3_2 | 1,331,161 | 16.2 | 9,726 | -8,550 | 18,275 | 3,798 | -3,326 | 7,124 |
| 3_3 | 6,493,717 | 79.2 | 12,356 | -9,762 | 22,118 | 14,200 | -9,400 | 23,600 |
| 3_4 | 18,706 | . 2 | 14,081 | -10,636 | 24,717 | 70,391 | -30,622 | 101,013 |
| Top (.000): |  |  |  |  |  |  |  |  |
| 4_0 | 0 | . 0 |  |  |  |  |  |  |
| 4_1 | 0 | . 0 |  |  |  |  |  |  |
| 4_2 | 0 | . 0 |  |  |  |  |  |  |
| 4_3 | 0 | . 0 |  |  |  |  |  |  |
| 4_4 | 0 | . 0 |  |  |  |  |  |  |
|  | Middle Firm (63\%) |  |  |  |  |  |  |  |
| Bottom (.010): |  |  |  |  |  |  |  |  |
| 2_0 | 3,160 | . 6 | 6,108 | -2,046 | 8,154 |  |  |  |
| 2_1 | 56,529 | 10.7 | 6,093 | -2,039 | 8,132 |  |  |  |
| 2_2 | 211,504 | 39.9 | 6,079 | -2,081 | 8,160 | 3,753 | -1,489 | 5,242 |
| 2_3 | 257,664 | 48.7 | 6,122 | -2,062 | 8,185 | 12,008 | -2,577 | 14,585 |
| 2_4 | 730 | . 1 | 6,121 | -2,031 | 8,152 | 68,020 | 5,440 | 62,580 |
| Middle (.958): |  |  |  |  |  |  |  |  |
| 3_0 | 170,775 | . 3 | 18,829 | 1,971 | 16,858 |  |  |  |
| 3_1 | 1,789,911 | 3.6 | 16,909 | 2,210 | 14,699 |  |  |  |
| 3-2 | 3,467,732 | 6.9 | 15,078 | 884 | 14,194 | 3,439 | -520 | 3,958 |
| 3-3 | 43,259,502 | 86.4 | 22,978 | 3,475 | 19,503 | 23,517 | 3,506 | 20,012 |
| 3-4 | 1,370,036 | 2.7 | 35,902 | 10,130 | 25,772 | 57,122 | 16,550 | 40,572 |
| Top (.031): |  |  |  |  |  |  |  |  |
| 4_0 | 2,532 | . 2 | 51,159 | 18,825 | 32,335 |  |  |  |
| 4_1 | 17,159 | 1.0 | 51,191 | 19,006 | 32,185 |  |  |  |
| 4_2 | 13,212 | . 8 | 50,902 | 18,745 | 32,156 | 3,202 | 569 | 2,632 |
| 4_3 | 437,317 | 26.6 | 49,933 | 17,999 | 31,934 | 37,792 | 13,081 | 24,711 |
| 4_4 | 1,174,019 | 71.4 | 51,694 | 19,249 | 32,445 | 55,357 | 20,583 | 34,775 |
|  | Top Firm (23\%) |  |  |  |  |  |  |  |
| Bottom (.000): |  |  |  |  |  |  |  |  |
| 2_0 | 0 | . 0 |  |  |  |  |  |  |
| 2_1 | 0 | . 0 |  |  |  |  |  |  |
| 2_2 | 0 | . 0 |  |  |  |  |  |  |
| 2_3 | 0 | . 0 |  |  |  |  |  |  |
| 2 -4 | 0 | . 0 |  |  |  |  |  |  |
| Middle (.569): |  |  |  |  |  |  |  |  |
| 3_0 | 30,130 | . 3 | 29,438 | 15,459 | 13,980 |  |  |  |
| 3_1 | 445,548 | 4.0 | 27,758 | 14,834 | 12,923 |  |  |  |
| 3-2 | 343,349 | 3.1 | 27,352 | 14,186 | 13,166 | 3,111 | 789 | 2,322 |
| 3-3 | 8,891,952 | 80.7 | 32,321 | 16,549 | 15,772 | 31,657 | 15,654 | 16,003 |
| 3_4 | 1,306,028 | 11.9 | 38,938 | 20,918 | 18,021 | 58,297 | 31,112 | 27,185 |
| Top (.431): |  |  |  |  |  |  |  |  |
| 4_0 | 12,388 | . 1 | 64,410 | 38,198 | 26,213 |  |  |  |
| 4_1 | 129,141 | 1.5 | 64,268 | 39,009 | 25,258 |  |  |  |
| 4_2 | 69,540 | . 8 | 61,384 | 35,782 | 25,602 | 2,939 | 974 | 1,965 |

Table E9 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| 4_3 | 1,055,443 | 12.6 | 56,162 | 31,142 | 25,020 | 34,895 | 17,929 | 16,965 |
| 4_4 | 7,085,455 | 84.8 | 64,675 | 37,688 | 26,987 | 68,632 | 39,649 | 28,983 |

Note.-See table 9 .

Table E10
Earnings Associated with Flows by Firm Bin for Persons in the High-Type Nonfirm Category

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
|  | Bottom Firm (24\%) |  |  |  |  |  |  |  |
| Bottom (.005): |  |  |  |  |  |  |  |  |
| 2_0 | 679 | 2.0 | 4,353 | -62,991 | 67,344 |  |  |  |
| 2_1 | 2,485 | 7.2 | 4,316 | -64,774 | 69,090 |  |  |  |
| 2_2 | 23,108 | 67.2 | 4,275 | -64,476 | 68,750 | 3,484 | -51,189 | 54,673 |
| 2_3 | 7,784 | 22.7 | 5,099 | -60,143 | 65,241 | 12,205 | -94,469 | 106,674 |
| 2_4 | 307 | . 9 | 3,928 | -91,664 | 95,592 | 193,962 | -307,444 | 501,406 |
| Middle (.768): |  |  |  |  |  |  |  |  |
| 3_0 | 16,791 | . 3 | 24,421 | -41,367 | 65,788 |  |  |  |
| 3_1 | 93,523 | 1.8 | 25,157 | -38,303 | 63,460 |  |  |  |
| 3_2 | 162,321 | 3.2 | 21,323 | -37,554 | 58,877 | 3,476 | -8,143 | 11,619 |
| 3-3 | 4,657,816 | 90.6 | 28,233 | -34,400 | 62,633 | 27,573 | -31,979 | 59,552 |
| 3_4 | 211,635 | 4.1 | 39,258 | -46,667 | 85,925 | 56,165 | -60,567 | 116,732 |
| Top (.227): |  |  |  |  |  |  |  |  |
| 4_0 | 4,499 | . 3 | 92,980 | -133,477 | 226,457 |  |  |  |
| 4_1 | 15,036 | 1.0 | 93,061 | -171,801 | 264,862 |  |  |  |
| 4_2 | 9,282 | . 6 | 80,095 | -133,162 | 213,257 | 3,008 | -6,393 | 9,401 |
| 4_3 | 192,250 | 12.6 | 58,951 | -75,598 | 134,549 | 36,197 | -41,533 | 77,730 |
| 4_4 | 1,299,404 | 85.5 | 79,502 | -109,491 | 188,992 | 80,704 | -107,069 | 187,773 |
|  | Middle Firm (56\%) |  |  |  |  |  |  |  |
| Bottom (.000): |  |  |  |  |  |  |  |  |
| 2_0 | 0 | . 0 |  |  |  |  |  |  |
| 2_1 | 0 | . 0 |  |  |  |  |  |  |
| 2_2 | 0 | . 0 |  |  |  |  |  |  |
| 2_3 | 0 | . 0 |  |  |  |  |  |  |
| 2_4 | 0 | . 0 |  |  |  |  |  |  |
| Middle (.310): |  |  |  |  |  |  |  |  |
| 3_0 | 9,579 | . 2 | 37,680 | -5,362 | 43,042 |  |  |  |
| 3-1 | 58,065 | 1.2 | 37,365 | -5,593 | 42,957 |  |  |  |
| 3-2 | 61,221 | 1.3 | 36,524 | -5,940 | 42,464 | 3,195 | -1,035 | 4,230 |
| 3-3 | 4,173,530 | 85.7 | 37,519 | -5,487 | 43,005 | 35,402 | -5,028 | 40,430 |
| 3_4 | 570,086 | 11.7 | 42,684 | -2,446 | 45,130 | 54,161 | -1,779 | 55,940 |
| Top (.690): |  |  |  |  |  |  |  |  |
| 4_0 | 25,565 | . 2 | 111,359 | 17,448 | 93,911 |  |  |  |
| 4_1 | 103,830 | 1.0 | 96,076 | 16,375 | 79,701 |  |  |  |

Table E10 (Continued)

| All Earnings (Share), Flow | Average Count | Percent | Previous Year Earnings |  |  | Current Year Earnings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | Firm | Nonfirm | Total | Firm | Nonfirm |
| 4_2 | 60,924 | . 6 | 76,673 | 11,055 | 65,618 | 3,037 | -346 | 3,383 |
| 4_3 | 1,192,613 | 11.0 | 61,122 | 7,031 | 54,091 | 35,535 | 2,971 | 32,564 |
| 4_4 | 9,463,943 | 87.3 | 88,559 | 15,037 | 73,522 | 89,570 | 15,434 | 74,136 |
|  | Top Firm (20\%) |  |  |  |  |  |  |  |
| Bottom (.000): |  |  |  |  |  |  |  |  |
| 2_0 | 0 | . 0 |  |  |  |  |  |  |
| 2_1 | 0 | . 0 |  |  |  |  |  |  |
| 2_2 | 0 | . 0 |  |  |  |  |  |  |
| 2_3 | 0 | . 0 |  |  |  |  |  |  |
| 2_4 | 0 | . 0 |  |  |  |  |  |  |
| Middle (.000): |  |  |  |  |  |  |  |  |
| 3 -0 | 0 | . 0 |  |  |  |  |  |  |
| 3_1 | 0 | . 0 |  |  |  |  |  |  |
| 3-2 | 0 | . 0 |  |  |  |  |  |  |
| 3_3 | 0 | . 0 |  |  |  |  |  |  |
| 3_4 | 0 | . 0 |  |  |  |  |  |  |
| Top (1.000): |  |  |  |  |  |  |  |  |
| 4_0 | 9,962 | . 2 | 203,735 | 115,510 | 88,225 |  |  |  |
| 4_1 | 73,693 | 1.4 | 214,392 | 127,870 | 86,521 |  |  |  |
| 4_2 | 27,036 | . 5 | 155,772 | 88,384 | 67,388 | 2,733 | 610 | 2,123 |
| 4_3 | 163,477 | 3.0 | 121,408 | 66,733 | 54,675 | 29,337 | 13,458 | 15,879 |
| 4_4 | 5,145,974 | 94.9 | 158,370 | 90,525 | 67,845 | 158,948 | 90,228 | 68,720 |

Note.-See table 9 .

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[^1]:    ${ }^{4}$ Blackburn and Bloom (1987) made a related point when analyzing earnings inequality from 1967 to 1985 in the CPS-ASEC. They noted that the patterns in earnings inequality observed in the data depended on various factors, including which individuals were included in the earnings distribution. More recently, Spletzer (2014) noticed a similar difference when comparing trends in inequality observed in the CPS vs. the LEHD data.
    ${ }^{5}$ Numerous studies have documented that workers face large earnings losses on job loss (Jacobson, Lalonde, and Sullivan 1993; Stevens 1997) and that layoffs are highly countercyclical (Hall 2005). However, while there are studies that allow the probability of experiencing unemployment spells to differ across income groups (Castañeda, Díaz-Giménez, and Ríos-Rull 1998) and some that explicitly take into account the effect of job loss when estimating models of earnings dynamics (Altonji, Smith, and Vidangos 2013), there is no consensus in the literature on the best method for incorporating inactive workers into a study of earnings inequality.
    ${ }^{6}$ While many studies have documented a rise in earnings inequality during recessions (e.g., Castañeda et al. 1998), other studies have noted that this relationship may not always hold. In particular, Barlevy and Tsiddon (2006) note that the cycli-

[^2]:    ${ }^{7}$ See, e.g., Katz and Murphy (1992), Levy and Murnane (1992), Juhn, Murphy, and Pierce (1993), and Katz and Autor (1999).
    ${ }^{8}$ See Autor, Katz, and Kearney (2008) and Acemoglu and Autor (2011) for a summary of more recent work on wage polarization. These studies usually define the "wage rate" as the earnings of full-time, full-year workers.
    ${ }^{9}$ Researchers have also used administrative data from other countries to study earnings inequality. Baker and Solon (2003) use longitudinal income tax records

[^3]:    ${ }^{14}$ Spletzer (2014) notes that the scope of coverage of the CPS-ASEC is previous year income from all jobs for all persons aged 15 and over currently residing in the household. To get comparable estimates from the LEHD, he computes annual earnings from all jobs for all workers aged 15 and over. While we impose no age restriction on our found frame, the results in Spletzer (2014) are very comparable. Furthermore, it is interesting to note that just imposing an age restriction, as is done in many studies, is not sufficient to reconcile the differences in earnings inequality trends observed in the CPS-ASEC and LEHD when using the underlying LEHD data without adjustments to their frame.
    ${ }^{15}$ A number of papers in this issue use or analyze the AKM decomposition. Barth, Davis, and Freeman (2018) directly apply the AKM method to the LEHD data using the all-workers frame we discuss below. Card et al. (2018) develop a full economic model that interprets AKM in the equilibrium and apply that model to data from Portugal. Bender et al. (2018) use AKM worker and firm effects to augment their analysis of German employers. Haltiwanger, Hyatt, and McEntarfer (2018) use the LEHD data in the all-workers frame, relying on observable firm characteristics rather than the AKM decomposition to study the employer's contribution. Juhn et al. (2018) measure earnings volatility from the LEHD data using the all-workers frame and require two consecutive years of positive earnings to study whether firm revenue shocks are transmitted to workers.

[^4]:    ${ }^{16}$ See Abowd et al. (2009) for a detailed summary of the construction of the LEHD infrastructure.
    ${ }^{17}$ See US Office of Personnel Management (2014) for a list of agency codes.

[^5]:    ${ }^{18}$ See Abowd and Vilhuber (2011) for a description of how these modeling assumptions were used to construct national gross worker and job flow estimates.

[^6]:    ${ }^{19}$ See Hirsch and Husain (2016) and the references therein for a summary of the literature on the cyclical movements of multiple job holding. The authors find that the multiple job-holding rate is procyclical, declining during recessions because of the increased slackness in the labor market.

[^7]:    ${ }^{20}$ The use of SSNs not originally issued to the person using the SSN has been documented and studied by Brown, Hotchkiss, and Quispe-Agnoli (2013) and others.

[^8]:    Note.-The table presents counts of the number of persons and jobs in the eligible-workers frame and in the immigrant-candidates file. The sum of these two components is the all-workers frame. The persons in the eligible-workers frame are disaggregated into those who report positive earnings (active) and those who do not (inactive). The frame is complete and covers the entire United States from 2004 forward.

[^9]:    ${ }^{21}$ App. A, sec. A2, provides a detailed analysis of the earnings coverage for each of our frames in comparison with US Bureau of Economic Analysis (BEA) NIPA annual wages and salary estimates.
    ${ }^{22}$ Bin 1 is reserved for eligible but inactive workers, who are not included in the summaries described in table 2.

[^10]:    ${ }^{23}$ Fig. B1 plots the same percentiles comparing the two worker frames for all available years, equivalent to the regime 4 cumulative distribution in fig. 2. That comparison indicates that the levels of all percentiles are greater in every year in the eligible-worker frame compared with the all-worker frame, but the trends are nearly identical. For both frames, there is no evidence of differences that are due to the dates in which states entered the frames except for the jump associated with the entry of California and New York in regime 2. Fig. B2 plots the ratio of the 90th percentile to the 10th percentile for each date regime using the all-workers frame. The figure confirms that there are some differences in the levels of these curves, but the trend analysis is largely unchanged. That the earnings distribution is unaffected by state entry is very strong evidence that the date of entry of a state into the LEHD infrastructure can be modeled as ignorably missing (Rubin 1987; Imbens and Rubin 2015).
    ${ }^{24}$ We also analyze how state entry into the LEHD data affects these measures of earnings inequality. Fig. B2 plots the $90 / 10$ ratio across date regimes. There are only minor differences across these regimes. Thus, the date of state entry does not affect the analysis of earnings inequality. Therefore, in the main discussion we present results from the overall distribution, where we include data from all available states in a given year.
    ${ }^{25}$ For a comparison of the levels of these ratios across the two frames, see figs. B5A, B5D, B6A, and B6D.

[^11]:    ${ }^{26}$ The statistics quoted in this paragraph are summarized in table B2, where they are also compared with ratios obtained when the all-workers frame is used. Removing the immigrant candidates from the frame materially alters the estimated trends in earnings inequality. While there is a similar decline in earnings inequality from 1995 to 2000 in both frames, after 2000 the trends in earnings inequality among eligible workers diverge from those observed among all workers. Table B2 shows that, on average, while the $99 / 1$ ratio was $15.4 \%$ higher after 2000 in the eligible-workers frame compared with only $5.0 \%$ higher in the all-workers frame, none of the other post-2000 inequality measures are rising in the all-workers frame.
    ${ }^{27}$ For example, decomposing the $90 / 10$ ratio in year $t$ (relative to 2000) around the median:

[^12]:    ${ }^{28}$ For a comparison of the levels of these ratios across the two frames, see fig. B5B, B5C, B5E, and B5F and fig. B6B, B6C, B6E, and B6F.
    ${ }^{29}$ These conclusions are materially different in the all-workers frame, which shows modest changes in inequality of roughly equal magnitudes at the top and bottom of the distribution. See fig. B4.

[^13]:    ${ }^{30}$ Because the ACS is a sample survey while the LEHD data are essentially the population over this period, we cannot distinguish between individuals found only in the LEHD data who should have linked to the ACS and those who were not sampled by the ACS. For this reason, we do not study the records of those in the LEHD-only group.
    ${ }^{31}$ Also compare fig. C1 with fig. B1.
    ${ }^{32}$ See also fig. C2.

[^14]:    ${ }^{33}$ These conclusions are not sensitive to using the eligible-workers frame. There are many more very low earnings records among the immigrant candidates, which would only exacerbate the differences below the median.
    ${ }^{34}$ See fig. C3A and C3C.
    ${ }^{35}$ See table C1.
    ${ }^{36}$ See table C2.
    ${ }^{37}$ See fig. C5 and the discussion in sec. C3 of app. C.
    ${ }^{38}$ See fig. D1.

[^15]:    ${ }^{39}$ See table D1.

[^16]:    ${ }^{40}$ See figs. D2-D5.
    ${ }^{41}$ The distribution of eligible workers across the four earnings/inactivity categories by year is shown in table E1. The table also shows the total earnings per year and the average earnings per year (total earnings/eligible workers with positive earnings). The last panel shows the cumulative change over the entire period for each of the three previous panels.

[^17]:    ${ }^{42}$ See table E1.
    ${ }^{43}$ When examining only the flows, we also implicitly assume average earnings are the same for each flow originating from the same bin. Although this assumption is false, it does not affect trends since average earnings for a given flow are typically stable over time. It does affect the scale or magnitude of each flow relative to those of other flows. Additional results and discussion for earnings changes, including the average earnings for each flow, are shown in app. E.

[^18]:    ${ }^{44}$ The disconnect is likely even greater than it may appear, especially for workers at the very top of the earnings distribution. Most of the workers moving from the bottom $20 \%$ to the top $20 \%$ and vice versa have earnings near the minimum value of the top earnings bin, suggesting that most of the transitions may be associated with small earnings changes than one might infer from the average earnings in each bin.
    ${ }^{45}$ Figs. E1-E3 repeat the analysis shown in figs. 10-12 using earnings changes instead of counts. The conclusions are essentially unchanged.

[^19]:    ${ }^{46}$ This is a slight abuse of notation. Two billion person-firm-year observations were used in the estimation from 826 million jobs held by 201 million persons at 14.7 million firms. Unlike the standard AKM approach of using only the employer with the highest earnings per worker per year, we use all jobs. The $i, j, t$ subscripting is standing in for a more complicated notation to indicate multiple employers in a particular year. The model is fit to the 2004-13 period, where the eligible-worker frame is complete for the entire US labor market. See sec. E2 of app. E for further details.

[^20]:    ${ }^{47}$ We included all of the effects labeled "Actual labor force experience" in table E4 using the coefficients in table E7.

[^21]:    ${ }^{48}$ The nonfirm component here includes the constant, person effect $\theta_{i}$, index $\left(x_{i t} \beta\right)$, and $\varepsilon_{i j \text {. }}$. The estimated constant is equal to 6.01, and the average value of the person effect and residual across all observations in the estimation sample are both zero. The average experience component is 0.57 , the labor force attachment component is 2.24, and the aggregate labor market conditions component is -0.045 .

[^22]:    Note.-All statistics are calculated at the worker-year-job level with the value for each job weighted by ( $y_{i j t} / e_{i t}$ ) when forming the averages. $N=2,014,000,000$. A firm is defined by the state-level unemployment insurance account number, called an SEIN (state employer identification number) in Longitudinal Employer-Household Dynamics (LEHD) data. Firm age (measured in years) and firm size are based on the national firm definitions used in other LEHD data products, like the Quarterly Workforce Indicators. See Haltiwanger et al. 2012.

[^23]:    ${ }^{49}$ The estimated $\log$ AKM firm effects do not vary during the period; however, the dollar value of the firm effect depends on all employers during the year and actual earnings. Hence, these effects do change values even when workers do not change employers. Of course, the AKM firm effect changes when an individual changes employers as well.
    ${ }^{50}$ The earnings observation we used for classification are labeled "previous year" in the tables.

[^24]:    Note.-Estimates are based on the paired years from 2004-2005 to 2012-2013. The first year in the pair is the "previous year," and the second year in the pair is the "current year." Bins associated with the flows are as follows: $0=$ inflow/outflow from the eligible-workers frame; $1=$ inactive but eligible; $2=$ bottom of the overall-earnings distribution; $3=$ middle of the overall-earnings distribution; and $4=$ top of the over-all-earnings distribution. "Average Count" is the average number of persons in the row during the year labeled "previous year." "Percent" is the percent distribution of transitions for all persons who started the year in the same overall-earnings distribution bin. For "Previous Year Earnings" and "Current Year Earnings," "Total" is the average real earnings in 2000 dollars, "Firm" is the average real earnings associated with the firm component in our decomposition, and "Nonfirm" is the average real earnings associated with the nonfirm component in our decomposition.

[^25]:    ${ }^{52}$ See sec. E3 of app. E for an analysis of the changes in earnings inequality using only the firm-type and nonfirm-type distributions. Some anomalies appear in that analysis that do not appear when we use only the skill type to characterize worker differences.

[^26]:    Note.-The first column presents of the total number of earnings records excluded from the eligibleworkers frame each year. The remaining columns disaggregate this count by the different eligibility requirements the record failed to meet: (i) records that are only on the unemployment insurance ("Invalid SSN" [Social Security number]), (ii) records where the SSN is valid but the age of the worker is less than 5 years old ("Age < 5 "), (iii) records where the worker is between 5 and 13 years old (" $5 \leq$ Age $<13$ "), (iv) records where the worker is between 13 and 18 years old (" $13 \leq \mathrm{Age}<18$ "), (v) records where the worker is more than 70 years old ("Age > 70 "), (vi) records where the worker has more than 12 jobs a year ("No. Jobs > 12"), and (vii) records that fail to meet the other eligibility requirements ("Other"), such as the year being greater than or equal to the SSN year of issue and less than the year of death (when available). The frame is complete from 2004 forward.

[^27]:    ${ }^{53}$ See BLS (1997) for more information.
    ${ }^{54}$ The BLS QCEW estimates account for about $95 \%$ of the BEA wage and salary component of the NIPA tables. See http://www.bea.gov/faq/index.cfm?faq _id=104 for more information.

[^28]:    Nоте.-Each row in the table represents a specific combination of quarters worked and number of quarters in the longest job. A 5-quarter longest job is active in either the fourth quarter of the previous year or the first quarter of the subsequent year, while a 6-quarter longest job is active in both. The number of quarters in the longest job takes values from 1 to 6 . The counts are averages per year.

[^29]:    ${ }^{55}$ See Spletzer (2014) for a very similar comparison.

[^30]:    ${ }^{56}$ For similar comparisons of the 10th, 20th, 80th, and 90th percentiles, see fig. C4.

[^31]:    ${ }^{58}$ The estimated AKM firm effects do not vary during the period, but workers can and do change employers.
    ${ }^{59}$ The earnings observation we used for classification are labeled "previous year" in the tables.

[^32]:    ${ }^{60}$ Notice that the nonfirm component of earnings declines as we move up the firm-type distribution. Although it is unclear exactly which covariate is primarily responsible for this decline (fewer hours worked during the year perhaps), the impact of working at a higher-paying firm would be much greater if the nonfirm component of earnings were the same across firm types.

