# **Overreaction in Macroeconomic Expectations**

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#### Abstract

We examine the rationality of individual and consensus professional forecasts of macroeconomic and financial variables using the methodology of Coibion and Gorodnichenko (2015), which focuses on the predictability of forecast errors from earlier forecast revisions. We document two principal findings: at the individual level, forecasters typically over-react to information, while consensus forecasts exhibit under-reaction. To reconcile these findings, we combine the diagnostic expectations model of belief formation from Bordalo, Gennaioli, and Shleifer (2018) with Woodford's (2003) noisy information model of belief aggregation. The model accounts for the findings, but also yields a number of new implications related to the forward looking nature of diagnostic expectations, which we also test and confirm. Finally, we compare our model to mechanical extrapolation, rational inattention, and natural expectations.

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### **I. Introduction**

Since the advent of the Rational Expectations Hypothesis, the dominant approach in economics is to assume that market participants form their beliefs about the future, and make decisions, on the basis of statistically optimal forecasts. Recent research challenges this approach. Empirically, a growing body of work tests the Rational Expectations Hypothesis using survey data on the anticipations of households and professional forecasters. The evidence uniformly points to systematic departures from statistical optimality, which take the form of predictable forecast errors. Such departures have been documented, for example, in the context of forecasting inflation and other macro variables (Coibion and Gorodnichenko 2012, 2015, CG henceforth, Fuhrer 2017), the aggregate stock market (Bacchetta, Mertens, and Wincoop 2009, Amromin and Sharpe 2014, Greenwood and Shleifer 2014, Adam, Marcet, and Buetel 2017), the cross section of stock returns (e.g., La Porta 1996, Bordalo, Gennaioli, La Porta and Shleifer 2018, and corporate earnings (DeBondt and Thaler 1990, Ben-David et al. 2013, Gennaioli, Ma, and Shleifer 2015, Bouchaud, Kruger, Landier, and Thesmar 2017). Departures from optimal forecasts also obtain in controlled experiments (e.g., Hommes et al. 2004, Beshears et al. 2013, Frydman and Nave 2017, Landier, Ma, and Thesmar 2017).

On the theoretical side, various relaxations of the Rational Expectations Hypothesis have been proposed to account for the data. In macroeconomics, the main approach builds on rational inattention and information rigidities (Sims 2003, Woodford 2003, Carroll 2003, Mankiw and Reis 2005, Gabaix 2014). This view maintains the rationality of individual inferences, but relaxes the assumption of common information or full information processing. This is often justified by arguing that acquiring, absorbing, and processing information entails sizable material and cognitive costs. To economize on these costs, agents optimally revise their expectations only sporadically, or on the basis of selected news. As a consequence, expectations (and decisions) under-react to news relative to the world of unlimited information capacity. In an important empirical test of these theories, CG (2015) study predictability of errors in consensus macroeconomic forecasts of inflation and other variables, and find evidence consistent with under-reaction.

In finance, in contrast, although there is some evidence of momentum and under-reaction (Cutler, Poterba, and Summers 1990, Jegadeesh and Titman 1993), the dominant puzzle is over-reaction to news. This puzzle has been motivated by the evidence that stock prices move too much relative to the movements in fundamentals both in the aggregate (Shiller 1981) and in the cross section (De Bondt and Thaler 1985). The leading psychological mechanism for understanding over-reaction is Kahneman and Tversky's (1972) finding that, in reacting to news, people tend to overweight "representative" events (Barberis, Shleifer and Vishny 1998, Gennaioli and Shleifer 2010). For instance, exceptional past performance of a firm may cause overweighting of the probability that this firm is "the next google" because googles are representative of the group of well performing firms, even though they are rare in absolute terms. This approach is not inconsistent with limited information processing, but stresses that people infer too much from the information they attend to, however limited. Thus, beliefs and decisions move too much with news (Augenblick and Rabin 2017, Augenblick and Lazarus 2017). BGLS (2017) look at the cross section of stock returns and at analyst expectations about earnings growth and find support for over-reaction driven by representativeness.

This state of research motivates two questions. First, which departure from rational expectations is predominant, under- or over-reaction to news? At the least, can we identify circumstances in which either of them is more likely to prevail? Second, which mechanisms create these departures? Put differently, can one account for the main features in the data using a parsimonious model capturing precise cognitive mechanisms for under- and over-reaction?

This paper addresses these questions by studying the predictions of professional forecasters about 16 macroeconomic variables, which include but are not limited to those considered by CG (2015). We use both the Survey of Professional Forecasters (SPF) and the Blue Chip Survey, which gives us 20 expectations time series in total. These include forecasts of real economic activity, consumption, investment, unemployment, housing starts, and government expenditures, as well as multiple interest rate variables. We examine both consensus and individual level forecasts. SPF data are publicly available; Blue Chip data were purchased.

Section 3 addresses the first question above, namely what are the patterns of over- and underreaction across different series. We follow CG's methodology of measuring a forecaster's news by his forecast revision, and of using this forecast revision to predict the forecast error, computed as the difference between the realization and the corresponding forecast. In this setting, under-reaction to news implies a positive correlation between forecast errors and forecast revisions, while over-reaction to news implies the opposite. Unlike CG, we examine not only consensus forecasts, defined as the average forecast across all analysts, but individual ones. We then explore the consequences of aggregating forecasts, which turns out to be crucial for understanding their properties.

For the case of consensus forecasts, our analysis confirms the CG findings of under-reaction: the average forecast revision positively predicts the average future forecast errors for most series. At the individual level, however, the opposite pattern emerges: for most series, the forecast revision of the average forecaster negatively predicts the same forecaster's future error. In stark contrast with the consensus results, at the level of the individual forecaster over-reaction is the norm, under-reaction the exception.

In Section 4 we propose a model that reconciles these seemingly contradictory findings from the viewpoint of leading theories of under- and over-reaction to news. In our setup, agents must predict the future value of a state that follows an AR(1) process. Each agent observes a different noisy signal of the current value of this state. To exploit such noisy information optimally, forecasters should use the Kalman filter. This setup captures Woodford's (2003) "Noisy Information Model", which describes CG's principal approach to rational inattention: noise stems from the cognitive costs of processing full information, but noisy signals are optimally evaluated using the Kalman filter. This setup can also capture a setting in which different forecasters, rather than being inattentive, simply observe different news (stemming for instance from their use of different models or different information sources, CG 2012).

To allow for over-reaction, we assume that – in processing the noisy signal – agents are swayed by representativeness. To formalize this heuristic we use the Gennaioli and Shleifer (2010) model, which was originally proposed to describe lab experiments on probabilistic judgments and later applied to social stereotypes (Bordalo, Coffman, Gennaioli, and Shleifer 2016), forecasts of credit spreads (BGS, 2018) and forecasts of firm performance (BGLS 2017). In this approach, the representativeness of a given future state is measured by the proportional increase in its probability in light of recent news. Agents exaggerate the probability of more representative states (states that have become relatively more likely) and underestimate the probability of others. Representativeness causes expectations to follow a modified Kalman filter that exaggerates the signal to noise ratio of news. As in earlier work, we call expectations distorted by representativeness "diagnostic."

In this model, under-reaction in the consensus can be reconciled with over-reaction at the individual level, *but only* when each forecaster over-reacts to the news he receives. When each forecaster over-reacts to his own information, the econometrician detects negative predictability of his forecast error at the individual level. At the consensus level, however, predictability may still be positive, provided the distortion caused by representativeness is not too strong. The reason is that, while over-reacting to his own signal, each individual forecaster does not react to the signals observed by the other forecasters. Because all signals are informative and on average correct about the state, the average forecast underreacts to the average information.

Our analysis therefore shows that judging whether individuals under- or over-react to information on the basis of consensus forecasts may be misleading. Even if all forecasters over-react, as under diagnostic expectations, looking at consensus forecasts may point to under-reaction simply because different analysts over-react in different directions to partial information. In Section 5 we assess whether the data are consistent with further distinctive predictions of diagnostic expectations. These predictions allow us to distinguish the model from the mechanical updating rule of adaptive expectations. They also allow us to better compare our model to Rational Inattention. The general logic of these tests relies on the "kernel of truth" property of diagnostic expectations, which holds that belief updating exaggerates true patterns in the data. This property yields testable predictions both across different series and in the time series of individual variables.

We present cross sectional tests in Section 5.1. We show first that, upon receiving news, individuals' forecast revisions are stronger for variables whose time series exhibit more persistence. This

is consistent with diagnostic expectations and with rational inattention, but not with adaptive expectations in which the updating rule is fixed. We then show that the individual-level CG coefficient of overreaction documented in Section 3 is closer to zero for series that are very persistent. This is in line with diagnostic expectations: as persistence increases, rational forecast revisions are more volatile (and in fact the signal to noise ratio increases) which reduces the scope for overreaction.

In Section 5.2 we develop a time-series test of the kernel of truth. We model individual series as AR(2) processes to account for long term reversals of actuals, consistent with the importance of hump shaped dynamics stressed by Fuster et al. (2010). We find that 12 out of 16 variables exhibit hump-shaped dynamics. We solve a diagnostic expectations model under AR(2) and show such dynamics have far-reaching implications for expectations under the kernel of truth property. In particular, they imply that: i) an upward forecast revision about the short term should predict excess pessimism about the long term, while ii) an upward forecast revision about the medium term should predict excess optimism about the long term. Put differently, diagnostic expectations exaggerate both short-term momentum and long-term reversals. We find that these predictions are borne out in the data. Besides strengthening the support for widespread over-reaction entailed by representativeness, these results also show the risks of using the CG method for AR(2) series. In fact, we show that overreaction to different time lags may contribute to finding apparent underreaction under an AR(1) specification. Taken together, the evidence is broadly consistent with the kernel of truth property of beliefs that is central to the diagnostic expectation mechanism.

The main contributions in this paper are to document empirically the prevalence of over-reaction to information in individual forecasts of macroeconomic variables, and to unify this finding with underreaction in the consensus using diagnostic expectations. There have been several other approaches to similar phenomena. One of them is fixed-rule extrapolation or adaptive expectations; and we show throughout that the diagnostic expectations model both has better psychological foundations and yields predictions more consistent with the data. Another approach is the model of Natural Expectations of Fuster et al. (2010). Diagnostic expectations yield some patterns that are similar to natural expectations, but also make distinctive predictions – such as over-reaction to long-term reversals – that more closely reflect the data. Finally, diagnostic expectations are related to the idea of over-confidence. In particular, they imply an exaggeration of the perceived signal to noise ratio, which is a conventional formalization of overconfidence. We focus on diagnostic expectations rather than overconfidence, because – as we show in other work – they help explain beliefs even in settings where overconfidence can be ruled out (such as in cases where information is common and public). We return to these alternatives throughout our analysis.

#### 2. The Data

#### Data on Forecasts

We collect forecast data from two sources: Survey of Professional Forecasters (SPF) and Blue Chip Financial Forecasts (Blue Chip).<sup>2</sup> SPF is a survey of professional forecasters currently run by the Federal Reserve Bank of Philadelphia. According to the enrollment form on Philadelphia Fed's website, "most of the survey's participants have formal and advanced training in economic theory and forecasting and use econometric models to generate their forecasts." Participation is also limited to "those who are currently generating forecasts for their employers or clients or those who have done so in the past." At a given point in time, around 40 forecasters contribute to the SPF anonymously. SPF is conducted on a quarterly basis, around the end of the second month in the quarter. It provides both consensus forecast data and forecaster-level data (identified by forecaster ID). Forecasters report forecasts for outcomes in the current and next four quarters, typically about the level of the variable in each quarter.

Blue Chip is a survey of panelists from around forty major financial institutions. The names of institutions and forecasters are disclosed. The survey is conducted around the beginning of each month. To match with the SPF timing most closely, we use Blue Chip forecasts from the end-of-quarter month survey (i.e. March, June, September, and December). Blue Chip has consensus forecasts available electronically, and we digitize individual-level forecasts from PDF publications. Panelists forecast outcomes in the current and next four to five quarters. For variables such as GDP, they report (annualized) quarterly growth rates. For variables such as interest rates, they report the quarterly average

<sup>&</sup>lt;sup>2</sup> Blue Chip provides two sets of forecast data: Blue Chip Economic Indicators (BCEI) and Blue Chip Financial Forecasts (BCFF). We do not use BCEI since historical forecaster-level data are only available for BCFF.

level. For both SPF and Blue Chip, the median (mean) duration of a panelist contributing forecasts is about 16 (23) quarters.

Given the timing of the SPF and Blue Chip forecasts we use, by the time the forecasts are made in quarter t (i.e. around the end of the second month in quarter t), forecasters know the actual values of variables with quarterly releases (e.g. GDP) up to quarter t - 1, and the actual values of variables with monthly releases (e.g. unemployment rate) up to the previous month.

Table 1 presents the list of variables we study, as well as the time range for which forecast data are available from SPF and/or Blue Chip. These variables cover both macroeconomic outcomes, such as GDP, price indices, consumption, investment, unemployment, government consumption, and financial variables, primarily yields on government bonds and corporate bonds. SPF covers most of the macro variables and selected interest rates (three month Treasuries, ten year Treasuries, and AAA corporate bonds). Blue Chip includes real GDP and a larger set of interest rates (Fed Funds, three month, five year, and ten year Treasuries, AAA as well as BAA corporate bonds). Relative to CG (2015), we add two SPF variables (nominal GDP and the 10Y Treasury rate) as well as the Blue Chip forecasts.<sup>3</sup>

#### Table 1. List of Variables

Variable	SPF	Blue Chip	Abbreviation
Nominal GDP	1968Q42014Q4	N/A	NGDP
Real GDP	1968Q42014Q4	1999Q12014Q4	RGDP
GDP Price Deflator	1968Q42014Q4	N/A	PGDP
Real Consumption	1981Q32014Q4	N/A	RCONSUM
Real Non-Residential Investment	1981Q32014Q4	N/A	RNRESIN
Real Residential Investment	1981Q32014Q4	N/A	RRESIN
Federal Government Consumption	1981Q32014Q4	N/A	RGF
State & Local Government Consumption	1981Q32014Q4	N/A	RGSL
Unemployment Rate	1968Q42014Q4	N/A	UNEMP
Housing Starts	1968Q42014Q4	N/A	HOUSING
Fed Funds Rate	N/A	1983Q12014Q4	FF
3M Treasury Rate	1981Q32014Q4	1983Q12014Q4	TB3M
5Y Treasury Rate	N/A	1988Q12014Q4	TN5Y
10Y Treasury Rate	1992Q12014Q4	1993Q12014Q4	TN10Y
AAA Bond Rate	1981Q32014Q4	1984Q12014Q4	AAA

This table lists our outcome variables, the forecast source, and the period for which forecasts are available.

<sup>&</sup>lt;sup>3</sup> Relative to CG, we do not use SPF forecasts on CPI inflation and industrial production index, as real time macro data are missing for these two variables for a period of time.

The main forecast horizon we analyze is annual. For variables like GDP and inflation, we look at the annual growth rate from quarter t - 1 to quarter t + 3. In SPF, the forecasts for these variables are in levels (e.g. level of GDP), so we transform them into implied growth rates (actual GDP of quarter t - 1is known at the time of the forecast, so this transformation complies with the forecasters' information sets). In Blue Chip, the forecasts for these variables are in the form of quarterly growth rates, so we add up forecasts for growth rates in quarters t to t + 3. For variables such as the unemployment rate and interest rates, we look at the level in quarter t + 3. Both SPF and Blue Chip have direct forecasts of the quarterly average level in quarter t + 3. Appendix C provides a description of variable construction.

N/A

Consensus forecasts are computed as means from individual-level forecasts available at a point in time. We calculate forecasts, forecast errors, and forecast revisions at the individual level, and then average them across forecasters to compute the consensus.<sup>4</sup>

#### Data on Actual Outcomes

The actual outcomes of macroeconomic variables are released quarterly but are often subsequently revised. To match as closely as possible the forecasters' information set, we focus on initial releases from Philadelphia Fed's Real-Time Data Set for Macroeconomists. For a given quarter, we proxy the forecasters' information set as the latest estimates available by the time of the forecast. Conversely, we measure the actual outcome that was forecasted using the initial release of the actuals in the corresponding time period. For example, for actual GDP growth from quarter t - 1 to quarter t + 3, we use the initial release of  $GDP_{t+3}$  (available in quarter t + 4) divided by the initial release of  $GDP_{t-1}$ (available in quarter t, prior to when the forecasts are made). For financial variables, the actual outcomes are available daily and are permanent (not revised). We use historical data from the Federal Reserve Bank of St. Louis.

<sup>&</sup>lt;sup>4</sup> There could be small differences in the set of forecasters who issue a forecast in quarter t, and the set of forecasters who revise their forecast at t (these forecasters need to be present at t - 1 as well). Thus, simple averages of forecasts and forecast revisions may cover different sets of individuals. This issue does not affect the results much. We can restrict our calculation to forecasters that have both forecasts and forecast revisions and results are the same.

Table 2 below presents the summary statistics of the variables, including the mean and standard deviation for the actuals being forecasted, as well as the consensus forecasts, forecast errors, and forecast revisions at a horizon of quarter t+3. The table also shows statistics for the quarterly share of forecasters with no meaningful revisions,<sup>5</sup> and the quarterly share of forecasters with positive revisions.

#### **Table 2. Summary Statistics**

Summary statistics of main variables; means and standard deviations are presented. All values are in percentages. Panel A shows the statistics of actuals, consensus forecasts, consensus errors and consensus revisions. Actuals are realized outcomes corresponding to the forecasts, and errors are actuals minus forecasts. Revisions are forecasts of the outcome made in quarter t minus forecasts of the same outcome made in quarter t-1. Panel B shows additional individual level statistics. The forecast dispersion column shows the mean of quarterly standard deviations of individual level forecasts. The revision dispersion column shows the mean of quarterly standard deviations of individual level forecast revisions. Non-revisions are instances where forecasts are available in both quarter t-1 and the change in the value is less than 0.01. The non-revision and up-revision columns show the mean of quarterly non-revision shares and up-revision shares. The final column of Panel B shows the fraction of quarters where less than 80% of the forecasters revise in the same direction.

		Act	uals	Fore	casts	Err	ors	Revi	sions
Variable	Format	mean	sd	mean	sd	mean	sd	mean	sd
Nominal GDP (SPF)		6.19	2.90	6.43	2.30	-0.24	1.75	-0.14	0.71
Real GDP (SPF)	-	2.56	2.31	2.73	1.38	-0.17	1.74	-0.18	0.64
Real GDP (BC)	-	2.66	1.55	2.62	0.86	0.03	1.30	-0.12	0.48
GDP Price Index (SPF)	-	3.56	2.49	3.63	2.03	-0.07	1.14	0.02	0.48
Real Consumption (SPF)	Growth rate	2.85	1.46	2.53	0.76	0.32	1.15	-0.05	0.51
Real Non-Residential Investment (SPF)	from end of quarter <i>t</i> -1	4.90	7.35	4.41	3.68	0.49	5.86	-0.26	1.78
Real Residential Investment (SPF)	to end of $t \rightarrow 3$	2.77	11.68	2.67	6.19	0.11	8.71	-0.64	2.48
Real Federal Government Consumption (SPF)	- quarter t+3	1.36	4.59	1.34	2.61	0.02	3.22	0.13	1.24
Real State&Local Govt Consumption (SPF)	-	1.62	1.68	1.62	1.09	0.00	1.12	0.00	0.59
Housing Start (SPF)	-	1.67	22.16	4.75	15.33	-3.08	18.81	-2.41	5.97
Unemployment (SPF)		6.38	1.55	6.38	1.43	0.00	0.76	0.06	0.33
Fed Funds Rate (BC)	-	4.10	2.99	4.53	2.94	-0.42	1.04	-0.18	0.54
3M Treasury Rate (SPF)	Average	3.98	2.86	4.54	2.93	-0.56	1.15	-0.21	0.52
3M Treasury Rate (BC)	- level in quarter $t+3$	3.76	2.73	4.28	2.72	-0.52	1.02	-0.18	0.51
5Y Treasury Rate (BC)		4.45	2.24	4.86	2.05	-0.41	0.89	-0.15	0.45
10Y Treasury Rate (SPF)	_	4.49	1.56	4.99	1.40	-0.50	0.76	-0.12	0.37

#### Panel A. Consensus Statistics

<sup>&</sup>lt;sup>5</sup> We categorize a forecaster as making no revision if the forecaster provides non-missing forecasts in both quarters t-1 and t, and the forecasts change by less than 0.01. For variables in rates, the data is often rounded to the first decimal point, and this rounding may lead to a higher incidence of none-revision. For national accounts variables in SPF, which are provided in levels, we define no-revision as less than 0.01% change in the implied growth rate forecasts.

10Y Treasury Rate (BC)	4.42	1.56	4.86	1.38	-0.44	0.75	-0.13	0.39
AAA Corporate Bond Rate (SPF)	7.26	2.4	7.74	2.52	-0.47	0.85	-0.11	0.39
AAA Corporate Bond Rate (BC)	6.84	1.94	7.26	2.01	-0.42	0.7	-0.12	0.37
BAA Corporate Bond Rate (BC)	6.30	1.08	6.75	0.95	-0.45	0.68	-0.14	0.31

		Forecasts		Rev		
Variable	Format	Dispersion	Dispersion	non-rev share	up-rev share	Pr(<80% revise same direction)
Nominal GDP (SPF)	_	0.59	1.13	0.02	0.45	0.79
Real GDP (SPF)	_	0.63	0.94	0.02	0.43	0.74
Real GDP (BC)	_	0.17	0.40	0.05	0.43	0.66
GDP Price Index (SPF)	-	0.52	0.75	0.05	0.49	0.79
Real Consumption (SPF)		0.68	0.76	0.03	0.48	0.76
Real Non-Residential Investment (SPF)	Growth rate from end of quarter <i>t</i> -1 to end of	1.03	2.47	0.02	0.49	0.71
Real Residential Investment (SPF)	quarter t+3	2.09	4.24	0.03	0.45	0.83
Real Federal Government Consumption (SPF)		1.38	2.25	0.06	0.52	0.87
Real State&Local Govt Consumption (SPF)	_	1.45	1.28	0.10	0.48	0.93
Housing Start (SPF)		5.46	8.61	0.00	0.39	0.68
Unemployment (SPF)		0.13	0.30	0.18	0.42	0.77
Fed Funds Rate (BC)		0.33	0.48	0.22	0.30	0.68
3M Treasury Rate (SPF)		0.29	0.48	0.15	0.34	0.68
3M Treasury Rate (BC)		0.29	0.46	0.19	0.32	0.63
5Y Treasury Rate (BC)	Average level in	0.15	0.42	0.12	0.35	0.61
10Y Treasury Rate (SPF)	quarter t+3	0.09	0.38	0.10	0.35	0.65
10Y Treasury Rate (BC)		0.08	0.35	0.13	0.33	0.57
AAA Corporate Bond Rate (SPF)		0.25	0.51	0.09	0.38	0.73
AAA Corporate Bond Rate (BC)	_	0.22	0.47	0.12	0.34	0.71
BAA Corporate Bond Rate (BC)		0.12	0.41	0.13	0.32	0.81

Panel B. Additional Individual Level Statistics

Several patterns emerge from Table 2. First, the average forecast error is about zero. It does not appear that macro analysts have asymmetric loss functions that persistently bias their forecasts in a given direction. Second, for each variable, there is significant dispersion of forecasts and revisions at each point in time, as shown in Table 2 Panel B. Third, analysts frequently revise their forecasts, but they do so in different directions. For example, as shown by the final column of Panel B, it is uncommon to have quarters where more than 80% forecasters revise in the same direction. This suggests that the appropriate model is one in which different forecasters observe or attend to different news, either because they are exposed to different information or because they use different models, or both. Berger, Erhmann, and Fratzscher (2011) show, for example, that the geographical location of forecasters influences their ability

to predict monetary policy decisions. Different forecasters may have personal contacts with the industry, policymakers, etc., which offers one explanation for the disagreement we see in the data. In this sense, forecasting is in part psychological: it involves subjective weighting of model output with private signals.<sup>6</sup>

### 3. Over-reaction vs. Under-reaction: Basic Tests

Studies of the rational expectations hypothesis often test whether forecast errors can be predicted using information available at the time the forecast was made. Understanding whether departures from rational expectations are due to over- or under-reaction to information is more challenging, since the forecaster's full information set cannot be directly observed by the econometrician.

To confront this problem, CG (2015) measure the news observed by a forecaster by his forecast revision. Denote by  $x_{t+h|t}^{i}$  the *h*-periods ahead forecast made at time *t* by forecaster *i* about the value  $x_{t+h}$  of a certain variable. Denote by  $x_{t+h|t-1}^{i}$  his forecast in the previous period. The *h*-periods ahead forecast revision at *t* is given by  $FR_{t,h}^{i} = (x_{t+h|t}^{i} - x_{t+h|t-1}^{i})$ , or the one period change in the forecast about  $x_{t+h}$ . This revision captures the information that the forecaster has observed and used to update his forecast.

CG analyze consensus forecasts, defined as the average of individual forecasters' predictions  $x_{t+h|t} = \frac{1}{I} \sum_{i} x_{t+h|t}^{i}$ , where I > 1 is the number of forecasters. In this setting, the *h*-periods ahead "consensus information" or forecast revision is given by the change in the consensus forecast,  $FR_{t,h} = (x_{t+h|t} - x_{t+h|t-1})$ . The extent to which the consensus forecast under-reacts or over-reacts to information can then be assessed by estimating the regression:

$$x_{t+h} - x_{t+h|t} = \beta_0 + \beta_1 F R_{t,h} + \epsilon_{t,t+h}.$$
(1)

<sup>&</sup>lt;sup>6</sup> This is well illustrated by a quote from Cleveland Fed President Pianalto, as cited by Coibion and Gorodnichenko (2012): "To paraphrase one of my colleagues, we are looking at flawed data through the lens of imperfect models. To try to clarify my perspective on the economy, I also spend a lot of time talking with businesspeople."

Under the Rational Expectations Hypothesis, the forecast error should be unpredictable using any current information, including the forecast revision itself, so  $\beta_1 = 0$ . When instead forecasters underreact to information, we expect  $\beta_1 > 0$ . As shown by CG, this includes the case in which analysts, perhaps because they are inattentive, observe different noisy signals of  $x_{t+h}$  and update rationally based on those signals (see Section 4). At the same time,  $\beta_1 > 0$  is also consistent with non-rational forms of under-reaction, such as that arising under Adaptive Expectations. To see why  $\beta_1 > 0$  captures underreaction, suppose that positive information is received, leading to a positive forecast revision  $FR_{t,h} > 0$ . If the forecast under-reacts, the upward revision is insufficient, predicting a positive forecast errors are positively correlated with forecast revisions.

By the same logic, when forecasters over-react to information we should expect  $\beta_1 < 0$ . Indeed, over-reaction means that after positive information  $FR_{t,h} > 0$  forecasters are too optimistic, so the forecast error is negative  $\mathbb{E}_t(x_{t+h} - x_{t+h|t}) < 0$ . On the other hand, after negative information  $FR_{t,h} < 0$  they are too pessimistic, so the error is positive  $\mathbb{E}_t(x_{t+h} - x_{t+h|t}) > 0$ . That is, over-reaction implies that the forecast error should be negatively correlated with the forecast revision.

To test for Rational Inattention, CG's baseline estimate of Equation (1) uses *consensus* SPF forecasts for the GDP price deflator (PGDP\_SPF) at a horizon h = 3. This yields  $\beta_1 = 1.2$ , which is robust to a number of controls. They also run Equation (1) for 13 SPF variables by pooling forecast horizons from h = 0 to h = 3,<sup>7</sup> and find qualitatively similar results, with 8 out of 13 variables exhibiting significantly positive  $\beta_1$ 's, and the average coefficient being close to 0.7. The general message is that consensus forecasts of macroeconomic variables appear to display under-reaction.

We estimate Equation (1) for our 20 series for the same baseline horizon h = 3, using consensus forecasts. The results are reported in columns (1) through (3) of Table 3, and confirm the findings of CG. The estimated  $\beta_1$  is positive for 14 out of 20 series, statistically significant for 8 of them at the 5%

<sup>&</sup>lt;sup>7</sup> These results are presented in Figure 1 Panel B of CG.

confidence level, and for a further two series at the 10% level. Our point estimate for inflation forecasts is exactly in line with CG's. While results for the other SPF series are not directly comparable (since CG pool across forecast horizons), the estimates lie in a similar range. The one exception is RGF\_SPF (federal government spending) for which the estimated  $\beta_1$  is negative and significant at the 5% level. Results from the Blue Chip survey align well with SPF where they overlap, but do not exhibit significant consensus overreaction for the remaining (exclusively financial variables) series.

We stress that the various forecast series are not entirely independent. For instance, nominal and real GDP growth are naturally highly correlated; the different interest rate series are also closely connected. Nonetheless, the general message holds: for macro variables and short rates, under-reaction appears common in the consensus forecast regressions, while such patterns are largely absent in longterm rates.

As mentioned above, insufficient updating of consensus beliefs may be due to aggregation issues, rather than to under-reaction to information by individual forecasters. As we saw in Table 2, individual forecasters often revise in different directions, perhaps because they look at different pieces of data or use different forecasting models. In this case, even if individual forecasters over-react to their own information, such over-reaction may be attenuated by averaging individual revisions going in opposite directions.

#### **Table 3. Error-on-Revision Regression Results**

This table shows coefficients from the CG (error on revisions) regression (1). Coefficients are displayed for both consensus time-series regressions, and forecaster-level pooled panel regressions, together with standard errors and p-values. Standard errors are Newey-West for consensus time-series regressions, and clustered by both forecaster and time for individual level regressions.

	Consensus			Individual						
				No f	ïxed ef	fects	With fixed effects		fects	
	$\beta_1$	s.e.	<i>p</i> -val	$\beta_1^p$	s.e.	<i>p</i> -val	$\beta_1^p$	s.e.	<i>p</i> -val	
Variable	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	
Nominal GDP (SPF)	0.48	0.22	0.03	-0.26	0.07	0.00	-0.30	0.06	0.00	
Real GDP (SPF)	0.45	0.25	0.07	-0.23	0.08	0.00	-0.21	0.06	0.00	
Real GDP (BC)	0.59	0.34	0.09	0.12	0.19	0.26	-0.02	0.17	0.93	
GDP Price Index Inflation (SPF)	1.21	0.21	0.00	-0.07	0.10	0.46	-0.16	0.07	0.03	
Real Consumption (SPF)	0.18	0.22	0.41	-0.34	0.11	0.00	-0.39	0.10	0.00	
Real Non-Residential Investment (SPF)	0.93	0.38	0.02	0.01	0.13	0.93	-0.03	0.12	0.82	
Real Residential Investment (SPF)	1.26	0.38	0.00	-0.02	0.10	0.82	-0.12	0.08	0.14	

Real Federal Government Consumption (SPF)	-0.44	0.23	0.05	-0.62	0.07	0.00	-0.63	0.06	0.00
Real State&Local Govt Consumption (SPF)	-0.16	0.20	0.42	-0.71	0.14	0.00	-0.73	0.13	0.00
Housing Start (SPF)	0.82	0.21	0.00	0.33	0.11	0.00	0.26	0.11	0.02
Unemployment (SPF)	0.45	0.31	0.14	-0.25	0.09	0.01	-0.28	0.08	0.00
Fed Funds Rate (BC)	0.61	0.23	0.01	0.15	0.09	0.11	0.12	0.09	0.19
3M Treasury Rate (SPF)	0.71	0.26	0.01	0.24	0.09	0.01	0.19	0.09	0.04
3M Treasury Rate (BC)	0.67	0.25	0.01	0.20	0.09	0.02	0.16	0.08	0.06
5Y Treasury Rate (BC)	0.05	0.22	0.84	-0.12	0.10	0.23	-0.19	0.10	0.05
10Y Treasury Rate (SPF)	-0.01	0.28	0.97	-0.18	0.10	0.06	-0.23	0.09	0.01
10Y Treasury Rate (BC)	-0.06	0.25	0.81	-0.17	0.12	0.14	-0.25	0.11	0.02
AAA Corporate Bond Rate (SPF)	-0.01	0.24	0.97	-0.21	0.08	0.00	-0.26	0.07	0.00
AAA Corporate Bond Rate (BC)	0.21	0.21	0.31	-0.17	0.07	0.00	-0.22	0.06	0.00
BAA Corporate Bond Rate (BC)	-0.14	0.28	0.62	-0.28	0.10	0.00	-0.34	0.10	0.00

To assess whether individual forecasters over- or under-react to their own information, we continue to follow the CG methodology, but perform the analysis at the individual analyst level. Here  $FR_{t,h}^i = (x_{t+h|t}^i - x_{t+h|t-1}^i)$  is the analyst-level revision, and the *h*-periods ahead individual forecast error is  $x_{t+h} - x_{t+h|t}^i$ . For each variable, we then pool all analysts and estimate the regression:

$$x_{t+h} - x_{t+h|t}^{i} = \beta_0^p + \beta_1^p F R_{t,h}^{i} + \epsilon_{t,t+h}^{i}.$$
 (2)

Superscript *p* in the coefficients recognizes that these are estimated by pooling individual level data. The logic, however, does not change:  $\beta_1^p > 0$  indicates that the average analyst insufficiently adjusts his forecast on the basis of his own information, while  $\beta_1^p < 0$  indicates that the average analyst over-reacts.

Columns (4) through (6) of Table 3 report the results of estimating Equation (2). Surprisingly, the picture is essentially reversed from the consensus analysis: at the individual level, the average analyst appears to over-react to information, as measured by a negative  $\beta_1^p$  coefficient. The estimated  $\beta_1^p$  is negative for 14 out of the 20 series, and significantly negative for 9 series at the 5% confidence level, and for one other series at the 10% level. Except for short rates (Fed Funds and 3-months T-bill rate), all financial variables display over-reaction, consistent with Shiller's evidence of excess volatility. But many macro variables also display over-reaction, including nominal GDP, real GDP (in SPF, not in Blue Chip), real consumption, real federal government expenditures, real state and local government expenditures. GDP price deflator inflation, real GDP in Blue Chip, and non-residential investment display neither over-

nor under-reaction ( $\beta_1^p$  is close to zero). Only the 3-months T-bill rate and unemployment rate display individual level under-reaction with positive and statistically significant  $\beta_1^p$ .

In columns (7) to (9), we also analyze regressions with forecaster-level dummies to account for possible time-invariant differences among analysts. For example, some analysts may be consistently overly-optimistic or overly-pessimistic, perhaps due to differences in their prior beliefs. These tendencies could contribute to positive correlations between forecast errors and revisions. Specifically, the overly optimistic analysts systematically receive bad news, leading to negative revisions and negative forecast errors. Similarly, the overly pessimistic analysts systematically receive good news, leading to positive revisions and positive forecast errors. In the data, the results with and without forecaster fixed effects are similar. With forecaster fixed effects, the estimated  $\beta_1^p$  is negative for 17 series, and significantly negative for 13 series at the 5% confidence level. Overall, the broad message from Table 3 is clear: at the level of the individual forecaster, over-reaction is the norm.

A seemingly contradictory picture emerges from these CG tests. At the consensus level, expectations typically under-react to information. At the individual level, in contrast, they typically overreact. In the next section, we present a model capable of reconciling these patterns.

#### 4. Diagnostic Expectations

At each time t, forecasters try to forecast a certain variable  $x_{t+h}$ , whose current value  $x_t$  is not directly observed. What is observed instead is a noisy signal  $s_t^i$ :

$$s_t^i = x_t + \epsilon_t^i,\tag{3}$$

where  $\epsilon_t^i$  is analyst specific noise, which is i.i.d. normally distributed across forecasters and over time, with mean zero and variance  $\sigma_{\epsilon}^2$ . The hidden state  $x_t$  evolves according to an AR(1) process with persistence  $\rho$ :

$$x_t = \rho x_{t-1} + u_t, \tag{4}$$

where  $u_t$  is a normal shock with mean zero and variance  $\sigma_u^2$ . We consider the case in which fundamentals follow an AR(1) process (here and in Section 5) for two reasons. First, AR(1) is a benchmark that was also considered by CG (2015), so it allows us to compare our model to theirs. Second, AR(1) yields a closed form characterization of the model's predictions. In particular, it allows us to study how expectations depend on the persistence parameter  $\rho$ . In Section 6 we allow series to follow an AR(2) process and show that this has additional implications for our analysis.

This setup accommodates several interpretations. In CG (2015), the fact that  $x_t$  is unobservable stems from rational inattention (Sims 2003, Woodford 2003). Forecasters could in principle perfectly observe the true current value of  $x_t$ , say GDP, but doing so is too costly. As a consequence, they observe a noisy proxy for it. This version of rational inattention is called "Noisy Rational Expectations", to reflect the fact that individuals rationally update on the basis of noisy signals. It is a different formulation of rational inattention than, for example, sticky information models (Mankiw and Reis 2002), in which all forecasters observe the same information but only sporadically revise their predictions. As shown by CG, these two versions of rational inattention have similar predictions on the relationship between consensus forecast errors and consensus forecast revisions. For this reason, our model only considers Noisy Rational Expectations. When we discuss predictions, however, we refer more broadly to Rational Inattention.

Another interpretation of Equations (3) and (4) is that the current realization of a variable, say GDP, is influenced by a persistent component  $x_t$  and a transitory component. In predicting the future, forecasters must estimate the persistent component on the basis of the noisy signal  $s_t^i$ . In this interpretation, the forecaster specific shock  $\epsilon_t^i$  captures the fact that different forecasters extract information using different models or pieces of evidence, and the variance  $\sigma_e^2$  of this shock captures the difficulty of the information extraction problem (which is shaped by the availability of reliable models and/or evidence). For professional forecasters, the latter interpretation is perhaps more compelling, since their job is to look at, and predict, the variables in question, so they are very attentive to these variables. The problem they face, though, when looking at, say, GDP statistics, is to assess whether shocks are transitory or persistent. Under both interpretations, the predictions of the model depart from full

information rational expectations because forecasters form their revisions through rational updating on the basis of noisy signals. In this sense, it is not misleading to place both interpretations under the rubric of Noisy Rational Expectations.

A Bayesian, or rational, forecaster enters period t carrying from the previous period beliefs about the current persistent state  $x_t$  summarized by a probability density  $f(x_t|S_{t-1}^i)$ , where  $S_{t-1}^i$  denotes the full history of signals observed by this forecaster. In period t, the forecaster observes a new signal  $s_t^i$ . In light of this evidence, he updates his estimate of the current state using Bayes' rule:

$$f(x_t|S_t^i) = \frac{f(s_t^i|x_t)f(x_t|S_{t-1}^i)}{\int f(s_t^i|x)f(x|S_{t-1}^i)dx}.$$
(5)

Equation (5) iteratively defines the forecaster's beliefs. In the current setting with normal shocks, the distribution  $f(x_t|S_t^i)$  is described by the Kalman filter. A rational forecaster should then estimate the current state to be  $x_{t|t}^i = \int x f(x|S_t^i) dx$  and should forecast the economic series of interest by using the AR(1) structure of the state  $x_t$ , namely  $x_{t+h|t}^i = \rho^h x_{t|t}^i$ .

We allow beliefs to be distorted by Kahneman and Tverky's representativeness heuristic, as in our model of Diagnostic Expectations. In line with BGLS (2017), which applied Diagnostic Expectations to a (diagnostic) Kalman Filter, we define the representativeness of a state  $x_t$  at time t as the likelihood ratio:

$$R_t(x_t) = \frac{f(x_t|S_t^i)}{f(x_t|S_{t-1}^i \cup \{x_t^i|_{t-1}\})}.$$
(6)

State  $x_t$  is more representative at t if the signal  $s_t^i$  received in this period increases the probability of that state, relative to not receiving any news. Receiving no news means observing a signal equal to the exante forecast,  $s_t^i = x_{t|t-1}^i$ , as described in the denominator of equation (6).

Intuitively, the most representative states are those whose likelihood has increased the most in light of recent data. The forecaster then overweighs representative states by using the distorted posterior:

$$f^{\theta}\left(x_{t}|S_{t}^{i}\right) = f\left(x_{t}|S_{t}^{i}\right)R_{t}\left(x_{t}\right)^{\theta}\frac{1}{Z_{t}},\tag{7}$$

where  $Z_t$  is a normalization factor ensuring that  $f^{\theta}(x_t|S_t^i)$  integrates to one. Parameter  $\theta \ge 0$  denotes the extent to which beliefs are distorted by representativeness. For  $\theta = 0$  beliefs are rational, described by the Bayesian conditional distribution  $f(x_t|S_t^i)$ . For  $\theta > 0$  the diagnostic density  $f^{\theta}(x_t|S_t^i)$  inflates the probability of highly representative states and deflates the probability of unrepresentative states. Mistakes occur because states that have become relatively more likely may still be unlikely in absolute terms.

This formalization of representativeness as relative likelihood, and its distortive effect on probability assessments, has been shown to unify well-known biases in probability assessments such as base rate neglect, the conjunction fallacy, and the disjunction fallacy (Gennaioli and Shleifer 2010). It has also been used to explain phenomena such as stereotyping (BCGS 2016), self-confidence (BCGS 2017), and expectation formation in financial markets (BGS 2018, BGLS 2017).

Equation (7) yields a very intuitive formalization of beliefs.

**Proposition 1** The distorted density  $f^{\theta}(x_t|S_t^i)$  is normal. In the steady state it is characterized by a constant variance  $\Sigma$  and by a time varying mean  $x_{t|t}^{i,\theta}$  which are given by:

$$x_{t|t}^{i,\theta} = x_{t|t-1}^{i} + (1+\theta) \frac{\Sigma}{\Sigma + \sigma_{\epsilon}^{2}} (s_{t}^{i} - x_{t|t-1}^{i}),$$
(8)

$$\Sigma = \frac{-(1-\rho^2)\sigma_{\epsilon}^2 + \sigma_u^2 + \sqrt{[(1-\rho^2)\sigma_{\epsilon}^2 - \sigma_u^2]^2 + 4\sigma_{\epsilon}^2\sigma_u^2}}{2}.$$
(9)

In equations (8) and (9),  $x_{t|t-1}^i$  refers to the rational forecast of the hidden state implied by the Kalman Filter. Diagnostic beliefs resemble rational beliefs in several respects. They have the same variance  $\Sigma$ , and their mean  $x_{t|t}^{i,\theta}$  updates past rational beliefs  $x_{t|t-1}^i$  with "rational news"  $s_t^i - x_{t|t-1}^i$ , to an extent that increases in the signal to noise ratio  $\Sigma/\sigma_{\epsilon}^2$ .

The difference between diagnostic and rational expectations is that the former overweigh the impact of news by the multiplicative factor  $\theta$  in Equation (8). That is, representativeness induces forecasters to behave as if news is more informative than it actually is, exaggerating updating. As a consequence, the Diagnostic Kalman Filter generates over-reaction to information. This stands in contrast to models of information rigidity or inattention, which generate under-reaction to information.<sup>8</sup> Equation (8) highlights another important feature of diagnostic expectations: they display excess volatility. In particular, the discrepancy between rational and diagnostic expectations arises only in the presence of rational news, namely when  $(s_t^i - x_{t|t-1}^i)$  is non-zero. Since rational news are zero on average, diagnostic expectations over-react on impact but then systematically revert to rationality, creating excess volatility.

In contrast to traditional departures from rationality such as adaptive expectations, diagnostic expectations are forward-looking, in that they depend on parameters of the true data generating process. They are characterized by the "kernel of truth" property: they exaggerate true patterns in the data. Positive news are objectively associated with improvement, but representativeness causes excess focus on the right tail, generating excessive optimism. Likewise, expectation revisions should exaggerate the true properties of the underlying data generating process. If fundamentals are more persistent, kernel of truth implies that expectations should react more strongly to news. Furthermore, as we show in Section 5.2, the kernel of truth implies that expectations exaggerate autocorrelation features of time series, so that the impact of longer lags may be overstated. In sum, the kernel of truth yields distinctive predictions that can be used to test them against conventional mechanical models of extrapolation such as adaptive expectations. We revisit such cross sectional and time-series implications in Sections 5 and 6.

<sup>&</sup>lt;sup>8</sup> Equation (8) is reminiscent of overconfidence, which is in fact often modeled as inflating the signal to noise ratio of private information. In our current setup, where  $s_t^i$  is private to each forecaster, the Diagnostic Kalman Filter is equivalent to this formulation of overconfidence. In other settings it is possible to distinguish these mechanisms, which are psychologically very different. First, over-confidence refers only to private information, while representativeness causes over-reaction to all information, including the public one, as shown in BGLS (2017). Second, depending on the data generating process, representativeness and diagnostic expectations can cause distortions also in the variance and other moments. Finally, representativeness unifies distortions in expectations with a variety of errors in probabilistic judgments, including conjunction and disjunction fallacies, and also social stereotypes, which overconfidence cannot account for.

Consider the implications of Diagnostic Expectations for forecasts and forecast errors. Section 3 presented two seemingly contradictory findings: predominance of under-reaction in consensus forecasts, and of over-reaction in individual forecasts. Define the consensus diagnostic forecast of  $x_{t+h}$  at time t as

$$x_{t+h|t}^{\theta} = \int x_{t+h|t}^{i,\theta} di = \rho^h \int x_{t|t}^{i,\theta} di,$$

so that the Diagnostic forecast error and revision are respectively given by  $x_{t+h} - x_{t+h|t}^{\theta}$  and  $x_{t+h|t}^{\theta} - x_{t+h|t-1}^{\theta}$ . In the appendix, we prove the following result.

**Proposition 2** Under the Diagnostic Kalman Filter, the estimated coefficients of regression (2) at the consensus and individual level,  $\beta_1$  and  $\beta_1^p$ , are given by:

$$\frac{cov(x_{t+h} - x_{t+h|t}^{\theta}, x_{t+h|t}^{\theta} - x_{t+h|t-1}^{\theta})}{var(x_{t+h|t}^{\theta} - x_{t+h|t-1}^{\theta})} = (\sigma_{\epsilon}^{2} - \theta\Sigma)g(\sigma_{\epsilon}^{2}, \Sigma, \rho, \theta)$$
(10)

$$\frac{cov(x_{t+h} - x_{t+h|t}^{i,\theta}, x_{t+h|t}^{i,\theta} - x_{t+h|t-1}^{i,\theta})}{var(x_{t+h|t}^{i,\theta} - x_{t+h|t-1}^{i,\theta})} = -\frac{\theta(1+\theta)}{(1+\theta)^2 + \theta^2 \rho^2}$$
(11)

where  $g(\sigma_{\epsilon}^2, \Sigma, \rho, \theta) > 0$  is a function of parameters. As a result, for  $\theta \in (0, \sigma_{\epsilon}^2/\Sigma)$  the Diagnostic Kalman Filter entails a positive consensus coefficient  $\beta_1 > 0$ , and a negative individual coefficient  $\beta_1^p < 0$ .

When representative types are not too overweighed,  $\theta < \sigma_{\epsilon}^2 / \Sigma$ , the Diagnostic Kalman Filter can reconcile positive consensus coefficients with negative individual level coefficients, consistent with the broad patterns of Section 3. Intuitively, when individual analysts over-react to their own information, a positive forecast revision by a given analyst is associated with excess optimism, while a negative revision is associated with his excess pessimism, which both imply  $\beta_1^p < 0$ . At the consensus level, however, matters are different. Individual analysts over-react to their own information but they don't react at all to the information received by the other analysts (which they do not observe). This is a force toward underreaction to average information, which is particularly strong if individual analysts receive very noisy information. In fact, when  $\sigma_{\epsilon}^2 / \Sigma$  is high, a forecaster's neglect of the signals observed by the other forecasters entails a large loss of information. As a result, when noise is large enough, each analyst severely under-reacts to the information held by all other forecasters, so the average analyst consequently under-reacts to the average analyst information, even if each analyst over reacts to his own news.

The condition on  $\theta$  that reconciles individual level overreaction and aggregate under-reaction has an intuitive interpretation. In fact,  $\theta < \sigma_{\epsilon}^2 / \Sigma$  is equivalent to the diagnostic Kalman gain  $(1 + \theta) \frac{\Sigma}{\Sigma + \sigma_{\epsilon}^2}$ being smaller than 1. This means that, as long as individual forecasters filter news to some extent, consensus forecasts exhibit underreaction, even if they discount information too little.

Compare Diagnostic Expectations with Noisy Rational Expectations ( $\theta = 0$ ). The latter approach can generate under-reaction of consensus forecasts,  $\beta_1 > 0$ , but it cannot generate over-reaction of individual analysts,  $\beta_1^p < 0$ . The reason is that in this model forecasters use the limited information at their disposal in an optimal, rational, way. As a result, their forecast error is uncorrelated with their own forecast revision. As evident from Equations (9) and (10), when  $\theta = 0$  there is under-reaction at the consensus level but no individual-level predictability. This stands in stark contrast to the evidence of Section 3.

Finally, Proposition 2 also illustrates the cross-sectional implications of the kernel of truth mentioned above: the predictability of forecast errors depends on the true features of the data generating process in the sense that the coefficients estimated at the pooled and individual analyst levels depend on the parameters characterizing the data generating process ( $\sigma_{\epsilon}^2, \Sigma, \rho, \theta$ ). In particular, higher noise to signal ratio  $\sigma_{\epsilon}^2/\Sigma$  implies stronger consensus under-reaction (i.e. larger  $\beta_1$ ).

We now summarize how different departures from rational expectations account for the findings of Section 3. These are: Rational Inattention (which shares the broad predictions of the Noisy Rational Expectations model above), Diagnostic Expectations, and Mechanical Extrapolation (i.e., adaptive expectations). We evaluate these models according to three predictions: 1) consensus level predictability, 2) individual level predictability, and 3) dependence of forecast revisions on the true features of the data generating process. Table 4 below presents the predictions of the different models:

#### Table 4.

Model	Consensus	Individual	Updating
Noisy Dational un	underreaction	no prodictability	depends on
Noisy Kational	underreaction	no predictability	fundamentals
<b>Diagnostia</b> consistent with		overmeention	depends on
Diagnostic	underreaction	overreaction	fundamentals
Mechanical /		underreaction for	does not depend
Adaptive	undetermined	persistent series	on fundamentals

Let us compare Rational Inattention to Diagnostic Expectations. The broad pattern of Section 3 – the positive predictability of consensus forecast errors and the negative predictability of individual forecast errors – indicates that 9 or 10 out of 20 series are consistent with diagnostic expectations but not rational inattention. Four series out of 20 – the GDP price deflator, the investment variables, and the Federal Funds rate – are consistent with rational inattention, featuring  $\beta_1 > 0$  and  $\beta_1^p$  statistically indistinguishable from zero. Finally, the 3-month T-bill rate (in SPF and Blue Chip), and the unemployment rate are consistent with neither Rational Inattention nor Diagnostic Expectations because they feature under-reaction at both the consensus and individual level,  $\beta_1$ ,  $\beta_1^p > 0$ . Perhaps the behavior of these latter series, as well as of other series, may be accounted for by individual under-reaction due to mechanical adaptive expectations.

Overall, most of the evidence is consistent with Diagnostic Expectations, but Rational Inattention or Adaptive Expectations may play a role for some series. We further assess these models next.

#### 5. Kernel of Truth

We run two sets of tests. The first is cross sectional, based on the persistence of the different series. By looking at how forecasts depend on persistence, we can distinguish whether they are backward looking (as in Adaptive Expectations) or forward looking (as in Rational Inattention or Diagnostic Expectations) and, if the latter, which model best accounts for the evidence. The second test is a time series test, assessing whether expectations display over-reaction to longer lags of the series in question.

#### **5.1 Persistence Tests**

Under both Noisy Rational Expectations and Diagnostic Expectations, the forecast revision made at t about  $x_{t+h}$  is given by:

$$x_{t+h|t}^{i} - x_{t+h|t-1}^{i} = \rho \big( x_{t+h-1|t}^{i} - x_{t+h-1|t-1}^{i} \big).$$

The revision *h* periods ahead reflects the forecast revision about the same variable h - 1 periods ahead, adjusted by the persistence  $\rho$  of the series. The idea is simple: when forecasts are forward looking, more persistent series should feature stronger news-based updating.

Under adaptive expectations, in contrast, updating is mechanical and should not depend on the true persistence of the forecasted process. Formally, in this case we should have that:

$$x_{t+h|t}^{i} - x_{t+h|t-1}^{i} = \mu (x_{t+h-1|t}^{i} - x_{t+h-1|t-1}^{i}),$$

where  $\mu$  is a positive constant independent of  $\rho$  (we formally show this in the Appendix).

To assess this prediction, we fit an AR(1) for the actuals of each series and estimate  $\rho$ . The actuals have the same format as the forecast variables,<sup>9</sup> and we use the exact time period for which the forecasts are available.<sup>10</sup> We estimate the following individual level regression:

$$x_{t+3|t}^{i} - x_{t+3|t-1}^{i} = \gamma_{o}^{p} + \gamma_{1}^{p} \left( x_{t+2|t}^{i} - x_{t+2|t-1}^{i} \right) + \epsilon_{t+3}^{i}$$

We estimate the same regression at the consensus level, which yields coefficients estimates  $\gamma_0$  and  $\gamma_1$ . We then regress the slope coefficients  $\gamma_1^p$  and  $\gamma_1$  on the estimated persistence  $\hat{\rho}$  of each series. By integrating this equation, it is easy to see that consensus forecasts should satisfy the same condition.

The results of the exercise are reported in Figure 1 Panel A. The evidence shows, both at the individual and at the consensus level, that the more persistent series display larger forecast revisions. While we only have 20 series, the correlation is statistically different from zero with a p-value less than

<sup>&</sup>lt;sup>9</sup> Here we follow CG and estimate persistence directly using autoregressions. Some of the series (e.g. interest rates) have time trends and are not stationary; in these cases we estimate persistence by fitting an ARIMA(1,1,0) process. <sup>10</sup> Thus the properties of the actuals can be slightly different for the same variable from SPF and BlueChip (e.g. real GDP growth in SPF and Blue Chip), as these two datasets generally span different time periods.

0.001.<sup>11</sup> In line with forward-looking models, analysts take persistence into account when forming their forecasts. This evidence is inconsistent with adaptive expectations, where forecasters update mechanically, without taking into account the true properties of the data generating process, including persistence. This result is also robust to a series having richer dynamics, as it depends only on the first autocorrelation lag. The pattern is similar for consensus forecasts, as shown in Figure 1 Panel B.

#### Figure 1. Properties of Forecast Revisions and Actuals

In Panel A, the y-axis is the regression coefficient  $\gamma_1^p$  from regression  $x_{t+3|t}^i - x_{t+3|t-1}^i = \gamma_o^p + \gamma_1^p (x_{t+2|t}^i - x_{t+2|t-1}^i) + \epsilon_{t+3}^i$ . The x-axis is the persistence measured from an AR(1) regression of the actuals corresponding to the forecasts. For each variable, the AR(1) regression uses the same time period as when the forecast data is available. In Panel B, the y-axis is the regression coefficient from the parallel specification using consensus forecasts.



Panel A. Individual Level Coefficients

Panel B. Consensus Coefficients

<sup>&</sup>lt;sup>11</sup> The results in Figure 1 and 2 obtain also if we exclude the Blue Chip series that are also available in SPF (e.g. real GDP, 3-month Treasuries, 10-year Treasuries, AAA corporate bond rate).



Another possibility is to assess the correlation between the persistence of a series and the CG coefficient of reaction to news. With respect to this test, Diagnostic Expectations do not have clear predictions at the consensus level. Indeed, the coefficient  $(\sigma_{\epsilon}^2 - \theta \Sigma)g(\sigma_{\epsilon}^2, \Sigma, \rho, \theta)$  in Equation (10) can be either decreasing or increasing in persistence  $\rho$ , depending on parameter values. A more direct test is to check the correlation between the CG coefficient estimated at the individual level and the persistence of the series in question. In fact, Equation (11) predicts that the coefficient should increase, i.e. get closer to zero, as persistence  $\rho$  increases. The intuition is that when the series is more persistent, forecast revisions become more volatile, even if due to noise, which reduces their correlation with forecast errors. Under Noisy Rational Expectations, on the other hand, individual coefficients should be zero, so they should be uncorrelated with the persistence of the series that forecasters are trying to predict.

Figure 2 shows the correlation for the CG coefficient estimated from individual-level regressions. We find that the CG coefficient rises with persistence, which lends additional support for Diagnostic Expectations. The correlation is statistically different from zero with a *p*-value of 0.035.

#### Figure 2. CG Regression Coefficients and Persistence of Actual

Plots of individual level CG regression (forecast error on forecast revision) coefficients against the persistence of the actual variable (x-axis).



#### 5.2. Kernel of Truth in the Time Series

We now analyze the possibility that some of the forecasted series may be influenced by longer lags, and in particular that may be better described by an AR(2) process. As discussed by Fuster, Laibson and Mendel (2010), several macroeconomic variables follow hump-shaped dynamics with short-term momentum and longer-term reversals. Considering this possibility is relevant for two reasons.

First, under the kernel of truth, forecasters should exaggerate true features of the data generating process, including the presence of long-term reversals. Checking whether longer lags are exaggerated in expectations thus allows us to further distinguish Diagnostic Expectations from Rational Inattention. This also allows us to compare these approaches to Natural Expectations, a model proposed by Fuster, Laibson and Mendel (2010) in which agents forecast and AR(2) process "as if" it was AR(1) in changes. In a stationary setting, this means that agents exaggerate the short run persistence of the process while dampening long-run reversals. Second, long-term reversals may help us to better understand our basic results in Section 3. In particular, AR(2) dynamics may contaminate the evidence of over and underreaction to news documented in Section 3. We clarify this point later.

### 5.2.1 Diagnostic Expectations with AR(2) Processes

Suppose that the state which agents seek to forecast follows an AR(2) process:

$$x_{t+3} = \rho_2 x_{t+2} + \rho_1 x_{t+1} + u_t.$$
(12)

If  $\rho_2 > 0$  and  $\rho_1 < 0$ , the variable displays short-term momentum and long-term reversal. Each agent now observes two signals, one about the current state  $s_t^i = x_t + \epsilon_t^i$  and another about the past state  $s_{t-1}^i = x_{t-1} + \epsilon_{t-1}^i$ . The optimal solution to this inference problem is again provided by the Kalman filter.

Consider diagnostic expectations. Denote by  $x_{t+s|t}^{i,\theta}$  the diagnostic expectation held by forecaster *i* about  $x_{t+s}$  at time *t*. Then, the diagnostic expectation of  $x_{t+3}$  is a linear combination of the diagnostic forecasts of  $x_{t+2}$  and  $x_{t+1}$  according to the autoregressive parameters  $\rho_1$  and  $\rho_2$ :

$$x_{t+3|t}^{i,\theta} = \rho_2 x_{t+2|t}^{i,\theta} + \rho_1 x_{t+1|t}^{i,\theta}.$$

In the appendix we show that the diagnostic forecasts about these intermediate outcomes take the form of a distorted Kalman filter in which the signal to noise ratio of each signal is exaggerated. The Diagnostic forecast revision for t + 3 at time t is a linear combination of the current Diagnostic Forecast revisions about the intermediate states:

$$x_{t+3|t}^{i,\theta} - x_{t+3|t-1}^{i,\theta} = \rho_2 \left( x_{t+2|t}^{i,\theta} - x_{t+2|t-1}^{i,\theta} \right) + \rho_1 \left( x_{t+1|t}^{i,\theta} - x_{t+1|t-1}^{i,\theta} \right).$$
(13)

This decomposition suggests a way to assess forecasters' reaction to information in an AR(2) setting, generalizing Equation (2). Denote by  $FR_{t,t+1}^{i}$  the forecast revision at t about next period t + 1. Likewise, denote by  $FR_{t,t+2}^{i}$  the forecast revision at t about t + 2. These forecast revisions are not indexed by  $\theta$  because they represent data, not predictions of a diagnostic model. The forecasters' reaction to information can then be assessed by running the regression:

$$x_{t+3} - x_{t+3|t}^{i} = \delta_0^p + \delta_2^p F R_{t,t+2}^i + \delta_1^p F R_{t,t+1}^i + \epsilon_{t,t+h}.$$
(13)

In other words by predicting the forecast error at t + 3 on the basis of current forecast revisions about the short and medium term. The Diagnostic Expectations model has the following implication.

**Proposition 3.** Under the Diagnostic Kalman filter, the estimated coefficients  $\hat{\delta}_1^p$  and  $\hat{\delta}_2^p$  in Equation (13) are proportional to the negative of the AR(2) coefficients:

$$\hat{\delta}_1^p \propto -\rho_1 \theta, \tag{14}$$

$$\hat{\delta}_2^p \propto -\rho_2 \theta. \tag{15}$$

As in the case of AR(1), rational expectations ( $\theta = 0$ ) imply that individual forecast errors cannot be predicted by any forecast revisions, including those on the right hand side of (13). In contrast, diagnostic expectations imply that the coefficients should be non-zero, with flipped signs relative to the data generating process. In line with kernel of truth, this predictability reflects over-reaction to the effect of lags in the true process. Suppose for instance that the process has short-term momentum, namely  $\rho_2 >$ 0. Then, over-reaction means that upward forecast revisions about  $x_{t+2}$  lead to exaggerated optimism about  $x_{t+3}$  and thus negative forecast errors. This yields  $\delta_2^p < 0$  in Equation (15), reproducing the basic insight of Equation (2). Suppose instead that the process has long-term reversal, namely  $\rho_1 < 0$ . Then, over-reaction to long-term reversal means that upward forecast revisions about  $x_{t+1}$  lead to exaggerated pessimism about  $x_{t+3}$  and thus positive forecast errors. This yields in  $\delta_1^p > 0$  in Equation (14).

Proposition 3 shows why assessing the AR(2) structure of our series is important to test the model. First, kernel of truth makes precise predictions for how forecast revisions should predict forecast errors on the basis of the data generating process. Diagnostic Expectations imply that forecast revisions about short and medium term conditions should predict forecast errors with a sign opposite to their true effects on  $x_{t+3}$ .

Second, Proposition 3 implies that the tests of Section 3 may not reliably distinguish over- or under- reaction when lags have different signs. Indeed, suppose that the AR(2) process features short term momentum,  $\rho_2 > 0$ , and long term reversals,  $\rho_1 < 0$ . Positive news at t may then trigger an upward revision of both the forecast about the short-term  $x_{t+1}$  and of that about the medium-term  $x_{t+2}$ . The former creates excess pessimism, the latter excess optimism. If the first effect is strong, it can reduce excess optimism after good news, making it harder to detect over-reaction using the specification of Section 3. We can compare Diagnostic to Natural Expectations in this setting of the AR(2) process in Equation (12), which features short term momentum and long term reversal. Under natural expectations, agents form their forecasts by fitting an AR(1) process in changes  $(x_{t+1} - x_t) = \varphi(x_t - x_{t-1}) + v_{t+1}$ . The resulting estimate for the autoregressive term is  $\varphi = (\rho_1 - \rho_2 - 1)/2$ . In the case of a stationary process, this implies that natural expectations exaggerate the short run persistence of the series while dampening long-term reversals.<sup>12</sup> Overall, then, the comparison with Diagnostic Expectation goes as follows.

Table 5.									
Model Individual $\hat{\delta}_2^p$		Individual $\hat{\delta}^p_1$							
Noisy Rational	Zero	Zero							
Diagnostia	Negative, due to overreaction to	Positive, due to over-reaction to							
Diagnostic	short term momentum	long term reversal							
Natural	Negative, due to overreaction to	Negative, due to under-reaction to							
Expectations	short term momentum	long term reversal							

Diagnostic and Natural Expectations share the same prediction concerning the coefficient on forecast revision at t + 2. In both models forecasters exaggerate short run persistence, predicting a negative  $\delta_2^p$ . On the other hand, Diagnostic and Natural Expectations make opposite predictions about the coefficient on forecast revision at t + 1. Diagnostic expectations over-react to long term reversals, predicting  $\delta_1^p > 0$ , while Natural expectations under-react to long term reversals thereby predicting  $\delta_1^p < 0$ .

In the remainder of the section, we test the predictions of Proposition 3 about the term structure of expectations. Section 5.2.2 performs some tests to assess which of the 16 variables we consider can be more accurately described by an AR(2) rather than an AR(1). We do not aim to find the unconstrained optimal ARMA(k, q) specification, which is a notoriously difficult task. We only wish to capture the simplest longer lags and see whether expectations react to them as predicted by the model. Section 5.2.3 then estimates Equation (13) for the variables that are found to be better approximated by an AR(2) process.

<sup>&</sup>lt;sup>12</sup> Indeed, the "intuitive" process under this model is  $x_{t+1} = (1 + \varphi)x_t - \varphi x_{t-1} + v_{t+1}$ . The original AR(2) process is stationary if  $\rho_1 - \rho_2 < 1$ ,  $\rho_1 + \rho_2 < 1$  and  $|\rho_2| < 1$ . This implies that  $1 + \varphi > \rho_1$  and that  $0 < \varphi < |\rho_2|$ .

### 5.2.2 AR(1) vs AR(2) Dynamics

To assess whether some series are better described by an AR(2) model, we first fit a quarterly AR(2) process to our 20 series.<sup>13</sup> Figure 4 below plots the estimates for the autocorrelation parameters  $\rho_1$  and  $\rho_2$  estimated for the relevant series. As before, the actuals have the same format as the forecast variables, and for each series the regression covers the time period when the forecast data is available.

For all series, the sign of coefficients is indicative of positive momentum at short horizons ( $\rho_2 > 0$ ) and long-run reversals ( $\rho_1 < 0$ ).<sup>14</sup> To assess which dynamics better describe the series, we compare the AR(2) estimates to the AR(1) estimates from Section 5.1. Table 5 below shows the Bayesian Information Criterion (BIC) score associated with each fit.

For a majority of series, AR(2) dynamics are favored over AR(1). The tests favor AR(1) dynamics only for real consumption (SPF) and the BAA bond rate (BC), while for the 10-year Treasury rate series the tests are inconclusive.<sup>15</sup> Indeed, the estimates for the long-run reversals are weakest for these series. Taken together, Table 5 and Figure 4 indicate that hump shaped dynamics are a key feature of several series, which should shape expectations under the hypothesis of kernel of truth.

#### Figure 4. AR(2) Coefficients of Actuals

For each variable, the AR(2) regression uses the same time period as when the forecast data is available. The blue circles show the first lag and the red diamonds show the second lag. Standard errors are Newey-West, and the vertical bars show the 95% confidence intervals.

<sup>&</sup>lt;sup>13</sup> Just like for the case of AR(1), for growth variables we run quarterly AR(2) regressions of growth from t - 1 to t + 3. For variables in levels, we run quarterly regressions in levels. We run separate regressions for the variables that occur both in SPF and BC, because they cover slightly different time periods.

<sup>&</sup>lt;sup>14</sup> We check whether multicollinearity may affect our results in this Section, given that forecasts revisions at different horizons are often highly correlated. The standard issue with multicollinearity is the coefficients are imprecisely estimated, which we do not find to be the case. We also perform simulations to verify that the correlation among the right hand side variables by itself does not mechanically lead to the patterns we observe.

<sup>&</sup>lt;sup>15</sup> The Akaike Information Criterion (AIC) yields similar results, except that it positively identifies the TN10Y series as AR(2). To interpret the IC scores, recall that lower scores represent a better fit. The likelihood ratio  $\frac{\Pr(AR2)}{\Pr(AR1)}$  is estimated as  $exp\left[-\frac{BIC_{AR2}-BIC_{AR1}}{2}\right]$ , so that  $\Delta BIC_{2-1} = -2$  means the AR(2) model is 2.7 times more likely than the AR(1) model. We follow the standard usage of considering scores below -2 as evidence for AR(2) over AR(1).



Table 5. BIC of AR(1) and AR(2) Regressions of Actuals

This table shows the BIC statistic corresponding to the AR(1) and AR(2) regressions of the actuals. The final column shows the specification that has a lower BIC (preferred).

Variable	BIC <sub>AR1</sub>	BIC <sub>AR2</sub>	$\Delta BIC_{2-1}$	model
Nominal GDP (SPF)	-1133.74	-1149.13	-15.39	AR(2)
Real GDP (SPF)	-1120.33	-1164.52	-44.19	AR(2)
Real GDP (BC)	-618.50	-626.83	-8.33	AR(2)
GDP Price Index Inflation (SPF)	-1423.70	-1456.90	-33.20	AR(2)
Real Consumption (SPF)	-924.47	-911.66	12.82	AR(1)
Real Non-Residential Investment (SPF)	-509.72	-524.37	-14.65	AR(2)
Real Residential Investment (SPF)	-375.81	-401.05	-25.25	AR(2)
Real Federal Government Consumption (SPF)	-560.97	-553.12	7.85	AR(1)
Real State&Local Govt Consumption (SPF)	-905.91	-896.23	9.68	AR(1)
Housing Start (SPF)	168.69	111.57	-57.12	AR(2)
Unemployment (SPF)	-250.88	-265.89	-15.01	AR(2)
Fed Funds Rate (BC)	191.89	149.87	-42.02	AR(2)
3M Treasury Rate (SPF)	240.87	232.25	-8.62	AR(2)
3M Treasury Rate (BC)	163.27	118.76	-44.51	AR(2)
5Y Treasury Rate (BC)	126.30	123.51	-2.79	AR(2)
10Y Treasury Rate (SPF)	89.66	89.91	0.25	AR(1)
10Y Treasury Rate (BC)	86.54	84.80	-1.74	AR(2)
AAA Corporate Bond Rate (SPF)	129.84	118.64	-11.20	AR(2)
AAA Corporate Bond Rate (BC)	86.05	84.72	-1.32	AR(2)
BAA Corporate Bond Rate (BC)	58.33	61.79	3.46	AR(1)

### 5.2.3 Empirical Tests of Over-Reaction with AR(2) dynamics

We now restrict the analysis to the series for which AR(2) is favored, and test the prediction of Proposition 3 by estimating Equation (13). Given that all AR(2) series we consider exhibit short term momentum  $\rho_2 > 0$  and long-term reversals  $\rho_1 < 0$ , under Diagnostic Expectations the estimated coefficient on medium term forecast revision should be negative,  $\delta_2^p < 0$ , while the estimated coefficient on short term forecast revision should be positive,  $\delta_1^p > 0$ . To test this prediction, we run regressions on the pooled individual level data, as in Section 3.

Figure 5 shows, for each relevant series, the forecast error regression coefficients  $\hat{\delta}_2^p$  and  $\hat{\delta}_1^p$  estimated from Equation (13). Table 6 also displays these two coefficients, together with their corresponding standard errors and *p*-values. In line with the predictions of the model, the signs of the coefficients indicate that the short-term revision positively predicts forecast errors ( $\hat{\delta}_1^p > 0$  for all 15 series, 10 of which are statistically significant at the 5% level) while the medium-term revision negatively predicts them ( $\hat{\delta}_2^p < 0$  for 12 out of 15 series, 8 of which are statistically significant at the 5% level). To further assess the results, we perform a test of joint significance for  $\hat{\delta}_2^p < 0$ ,  $\hat{\delta}_1^p > 0$  holds, as shown in the last column of Table 6. The probability is greater than 95% for 8 out of the 15 series.

Figure 5. Coefficients in CG Regression AR(2) Version

This plot shows the coefficients  $\delta_2^p$  (blue circles) and  $\delta_1^p$  (red diamonds) from the regression in Equation (13). Standard errors are clustered by both forecaster and time, and the vertical bars shown the 95% confidence intervals.



Coefficients  $\delta_2^p$  and  $\delta_1^p$  from the regression in Equation (13), together with the corresponding standard errors and *p*-values. The final column resamples the data using block bootstrap and shows the probability of  $\delta_2^p < 0$  and  $\delta_1^p > 0$ .

Variable	$\delta^p_2$	s.e.	<i>p</i> -val	$\delta_1^p$	s.e.	<i>p</i> -val	Prob $\delta_2^p < 0$ & $\delta_1^p > 0$
Nominal GDP (SPF)	-0.37	0.12	0.00	0.33	0.15	0.03	0.99
Real GDP (SPF)	-0.21	0.16	0.19	0.23	0.18	0.22	0.86
Real GDP (BC)	-0.14	0.40	0.72	0.24	0.33	0.48	0.78
GDP Price Index Inflation (SPF)	-0.36	0.11	0.00	0.59	0.18	0.00	0.99
Real Non-Residential Investment (SPF)	-0.48	0.26	0.03	0.88	0.31	0.00	1.00
Real Residential Investment (SPF)	0.05	0.16	0.77	-0.19	0.20	0.34	0.12
Housing Start (SPF)	-0.31	0.16	0.01	0.85	0.20	0.00	1.00
Unemployment (SPF)	0.09	0.12	0.15	0.31	0.13	0.11	0.40
Fed Funds Rate (BC)	-0.17	0.18	0.43	0.55	0.20	0.03	0.85
3M Treasury Rate (SPF)	-0.17	0.11	0.20	0.62	0.14	0.00	0.92
3M Treasury Rate (BC)	-0.40	0.06	0.00	0.46	0.19	0.00	1.00
5Y Treasury Rate (BC)	-1.08	0.11	0.00	1.03	0.16	0.00	1.00
10Y Treasury Rate (BC)	-0.60	0.13	0.00	0.51	0.16	0.01	1.00
AAA Corporate Bond Rate (SPF)	-0.43	0.11	0.00	0.49	0.14	0.00	1.00
AAA Corporate Bond Rate (BC)	-0.61	0.12	0.00	0.45	0.17	0.01	1.00

The fact that short-term revisions negatively predict forecast errors conditional on longer-term revisions, and that they do so in different directions, is consistent with the idea that forecasters exaggerate true patterns in the data, including for longer-term dynamics. In contrast, this finding is harder to reconcile with Natural Expectations, where forecasters neglect longer lags (in the current setting, this means fitting an AR(1) model even for AR(2) series).

Overall, the AR(2) analysis confirms and in fact strengthens the evidence for the prevalence of over-reaction in the data. Indeed, four of the seven series (PGDP\_SPF, RRESINV\_SPF, TN5Y\_BC and TN10Y\_BC) for which individual level forecast errors seemed unpredictable (Table 3), and thus consistent with Noisy Rational Expectations, show evidence of over-reaction in the AR(2) setting. In addition, the two series that seemed to display under-reaction at the individual level, unemployment and the 3-months T Bill rate, now show evidence of over-reaction to long-term reversals ( $\delta_1^p > 0$ ), albeit not significantly. In all these cases, it is possible that over-reaction to long term reversals moved the individual level coefficient in Table 4 close to zero or above, giving the false impression of rationality or

under-reaction. Only for the variable RGDP\_SPF, which displayed significant over-reaction under the AR(1) specification loses its significance at conventional level under the more appropriate AR(2) case. Overall, then, the AR(2) specification strengthens the case for over-reaction.

#### 6. Conclusion

Using data from both the Blue Chip Survey and the Survey of Professional Forecasters, we have investigated how professional forecasters react to information using the methodology of Coibion and Gorodnichenko (2015). We have found that for individual forecasters, over-reaction to information is the norm, whereas for the consensus forecast the norm is under-reaction. We then applied a psychologically founded model of belief formation, diagnostic expectations, to these data. Diagnostic expectations generate over-reaction in individual data, but also yields many additional predictions, and showed that this model is consistent with individual forecast data for many series. We further showed that because different forecasters see different information and use different models, the consensus forecast may theoretically exhibit under-reaction, as previously shown by Coibion-Gorodnichenko and confirmed in our data.

The ubiquity of over-reaction in individual macroeconomic forecasts helps reconcile distinctive evidence in finance and macroeconomics. Financial economics has put together a lot of evidence of over-reaction in individual markets, such as housing, credit, and equities. It would be puzzling if macroeconomic forecasts were completely the opposite, but as we show this may be largely a consequence of aggregation.

We also find that individual forecasts are better described by diagnostic expectations than by mechanical models of extrapolation. Adaptive expectations have been criticized by Lucas and others for assuming that people are entirely backward looking. Because with diagnostic expectations, forecasters are forward looking but their judgment is distorted by representativeness, this model is not vulnerable to the Lucas critique. Of course, diagnostic expectations can serve as a micro-foundation of adaptive expectations and extrapolation at a crude level. At the same time, the kernel of truth property of

diagnostic expectations produces exact predictions on when we can see overreaction in forecasts, which becomes extremely important in some contexts, such as credit cycles (Bordalo, Gennaioli, and Shleifer 2018).

A final benefit of our approach is that it enables to reconcile diverse evidence that identified distinctive features of expectations. At the most basic level, we sought to reconcile the evidence on individual and consensus forecasts. Perhaps more subtly, diagnostic expectations when extended to the AR(2) context enable us to model expectations for hump shaped series. In this setting, diagnostic expectations capture some features of Natural Expectations (Fuster et al. 2010), namely exaggeration of short term persistence, but they also yield over-reaction to long term reversal, which seems to be an important feature of the data.

Our paper leaves at least two important problems to future work. We have stressed over-reaction in individual time series, which seems to be the norm in our data, but other studies have also found some rigidity in expectations even in individual data. For example, in their experimental study, Landier, Ma, and Thesmar (2017) find that beliefs of experimental subjects are best characterized by a mixture of anchoring to old forecasts and over-reaction to news. In this paper we have combined over-reaction with rigidity by incorporating representativeness in a noisy information setting. The reconciliation of anchoring with over-reaction to information based on psychological foundations remains an open problem.

We have not addressed the basic theoretical question: do individual or consensus beliefs matter for macroeconomic outcomes? For aggregate outcomes, what may matter is consensus expectations, so all one needs to know is that consensus expectations under-react. There are two problems in this view. First, over-reaction by individual forecasters can influence aggregate outcomes through dispersion in beliefs. Certain firms or sectors will over-invest, others will under-invest, creating aggregate misallocations. Second, in some circumstances news may be correlated across different agents, for instance when major innovations are introduced, or when repeated news in the same direction are highly informative of persistent changes. In these cases, individual over-reaction will entail aggregate overreaction. There is of course evidence of aggregate over-reaction in the stock market going back to Shiller,

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and in credit markets as well (Greenwood and Hanson 2013, Lopez-Salido et al. 2017). Whether overreaction can account for macroeconomic phenomena such as investment booms or business cycles is a key question in this research project.

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### Appendix

### A. Variable Definitions

### 1. NGDP\_SPF

- Variable: Nominal GDP. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of nominal GDP in the current quarter and the next 4 quarters.
- Forecast variable: Nominal GDP growth from end of quarter t-1 to end of quarter t+3 $\frac{F_t x_{t+3}}{r} - 1$ , where t is the quarter of forecast and x is the level of GDP in a given quarter;  $x_{t-1}$  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$ . published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 2. RGDP SPF

- Variable: Real GDP. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of real GDP in the current quarter and the next 4 quarters.
- Forecast variable: Real GDP growth from end of quarter t-1 to end of quarter t+3 $\frac{F_t x_{t+3}}{x} - 1$ , where t is the quarter of forecast and x is the level of GDP in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in • quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 3. RGDP\_BC

- Variable: Real GDP. Source: Blue Chip.
- Survey time: End of the middle month in the quarter/beginning of the last month in the • quarter.
- Survey question: Real GDP growth (annualized rate) in the current quarter and the next 4 • to 5 quarters.
- Forecast variable: Real GDP growth from end of quarter t-1 to end of quarter t+3 $F_t(z_t + z_{t+1} + z_{t+2} + z_{t+3})/4$ , where t is the quarter of forecast and  $z_t$  is the annualized quarterly GDP growth in quarter t.
- •
- Revision variable:  $\frac{F_t(z_t+z_{t+1}+z_{t+2}+z_{t+3})}{4} \frac{F_{t-1}(z_t+z_{t+1}+z_{t+2}+z_{t+3})}{4}$ Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 4. PGDP\_SPF

- Variable: GDP price deflator. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of GDP price deflator in the current quarter and the next 4 quarters.
- Forecast variable: GDP price deflator inflation from end of quarter t-1 to end of quarter  $t+3\frac{F_t x_{t+3}}{x_{t-1}} - 1$ , where t is the quarter of forecast and x is the level of GDP price deflator in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in • quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 5. RCONSUM SPF

- Variable: Real consumption. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of real consumption in the current quarter and the next 4 quarters.
- Forecast variable: Growth of real consumption from end of quarter t-1 to end of quarter •  $t+3\frac{F_t x_{t+3}}{x_{t-1}}-1$ , where t is the quarter of forecast and x is the level of real consumption in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 6. RNRESIN\_SPF

- Variable: Real non-residential investment. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of real non-residential investment in the current quarter and the next 4 quarters.
- Forecast variable: Growth of real non-residential investment from end of quarter t-1 to • end of quarter  $t+3\frac{F_t x_{t+3}}{x_{t-1}} - 1$ , where t is the quarter of forecast and x is the level of real non-residential investment in a given quarter;  $x_{t-1}$  uses the initial release of actual value
- in quarter *t*-1, which is available by the time of the forecast in quarter *t*. Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

# 7. RRESIN\_SPF

- Variable: Real residential investment. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter. •

- Survey question: The level of real residential investment in the current quarter and the next 4 quarters.
- Forecast variable: Growth of real residential investment from end of quarter t-1 to end of quarter  $t+3 \frac{F_t x_{t+3}}{x_{t-1}} - 1$ , where t is the quarter of forecast and x is the level of real residential investment in a given quarter;  $x_{t-1}$  uses the initial release of actual value in
- quarter *t*-1, which is available by the time of the forecast in quarter *t*. Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 8. RGF\_SPF

- Variable: Real federal government consumption. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of real federal government consumption in the current quarter • and the next 4 quarters.
- Forecast variable: Growth of real federal government consumption from end of quarter t-• 1 to end of quarter  $t+3\frac{F_t x_{t+3}}{x_{t-1}} - 1$ , where t is the quarter of forecast and x is the level of real federal government consumption in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_{t}x_{t+3}}{x_{t-1}} \frac{F_{t-1}x_{t+3}}{F_{t-1}x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.
- 9. RGSL\_SPF
  - Variable: Real state and local government consumption. Source: SPF. •
  - Survey time: Around the 3rd week of the middle month in the quarter. •
  - Survey question: The level of real state and local government consumption in the current quarter and the next 4 quarters.
  - Forecast variable: Growth of real state and local government consumption from end of • quarter t-1 to end of quarter t+3  $\frac{F_t x_{t+3}}{x_{t-1}} - 1$ , where t is the quarter of forecast and x is the level of real state and local government consumption in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.

  - Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 10. UNEMP SPF

- Variable: Unemployment rate. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average unemployment rate in the current quarter and the next 4 quarters.

- Forecast variable: Average quarterly unemployment rate in quarter  $t+3 F_t x_{t+3}$ , where t is • the quarter of forecast and x is the level of unemployment rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter *t*+4.

### 11. HOUSING SPF

- Variable: Housing starts. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter. •
- Survey question: The level of housing starts in the current quarter and the next 4 quarters.
- Forecast variable: Growth of housing starts from quarter t-1 to quarter t+3  $\frac{F_t x_{t+3}}{x_{t-1}} 1$ , where t is the quarter of forecast and x is the level of housing starts in a given quarter;  $x_{t-1}$  uses the initial release of actual value in quarter t-1, which is available by the time of the forecast in quarter t.
- Revision variable:  $\frac{F_t x_{t+3}}{x_{t-1}} \frac{F_{t-1} x_{t+3}}{F_{t-1} x_{t-1}}$ . Actual variable:  $\frac{x_{t+3}}{x_{t-1}} 1$ , using real time macro data: initial realease of  $x_{t+3}$  published in quarter t+4 and initial release of  $x_{t-1}$  published in quarter t.

## 12. FF\_BC

- Variable: Federal funds rate. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average federal funds rate in the current quarter and the • next 4 quarters.
- Forecast variable: Average quarterly 3-month federal funds rate in quarter  $t+3 F_t x_{t+3}$ , • where t is the quarter of forecast and x is the level of federal funds rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

### 13. TB3M\_SPF

- Variable: 3-month Treasury rate. Source: SPF. •
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average 3-month Treasury rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly 3-month Treasury rate in quarter  $t+3 F_t x_{t+3}$ , where • t is the quarter of forecast and x is the level of 3-month Treasury rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

## 14. TB3M BC

- Variable: 3-month Treasury rate. Source: Blue Chip.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average 3-month Treasury rate in the current quarter and the next 4 quarters.

- Forecast variable: Average quarterly 3-month Treasury rate in quarter  $t+3 F_t x_{t+3}$ , where *t* is the quarter of forecast and x is the level of 3-month Treasury rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

### 15. TN5Y\_BC

- Variable: 5-year Treasury rate. Source: Blue Chip.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average 5-year Treasury rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly 5-year Treasury rate in quarter  $t+3 F_t x_{t+3}$ , where t is the quarter of forecast and x is the level of 5-year Treasury rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

## 16. TN10Y\_SPF

- Variable: 10-year Treasury rate. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average 10-year Treasury rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly 10-year Treasury rate in quarter  $t+3 F_t x_{t+3}$ , where t is the quarter of forecast and x is the level of 10-year Treasury rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

## 17. TN10Y\_BC

- Variable: 10-year Treasury rate. Source: Blue Chip.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average 10-year Treasury rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly 10-year Treasury rate in quarter  $t+3 F_t x_{t+3}$ , where t is the quarter of forecast and x is the level of 10-year Treasury rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

## 18. AAA\_SPF

- Variable: AAA corporate bond rate. Source: SPF.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average AAA corporate bond rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly AAA corporate bond rate in quarter  $t+3 F_t x_{t+3}$ , where *t* is the quarter of forecast and x is the level of AAA corporate bond rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .

• Actual variable:  $x_{t+3}$ .

# 19. AAA\_BC

- Variable: AAA corporate bond rate. Source: Blue Chip.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average AAA corporate bond rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly AAA corporate bond rate in quarter  $t+3 F_t x_{t+3}$ , where *t* is the quarter of forecast and x is the level of AAA corporate bond rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .

## 20. BAA\_BC

- Variable: BAA corporate bond rate. Source: Blue Chip.
- Survey time: Around the 3rd week of the middle month in the quarter.
- Survey question: The level of average BAA corporate bond rate in the current quarter and the next 4 quarters.
- Forecast variable: Average quarterly BAA corporate bond rate in quarter  $t+3 F_t x_{t+3}$ , where *t* is the quarter of forecast and x is the level of BAA corporate bond rate in a given quarter.
- Revision variable:  $F_t x_{t+3} F_{t-1} x_{t+3}$ .
- Actual variable:  $x_{t+3}$ .