Optimal Financing for R&D-Intensive Firms∗

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Abstract

We develop a theory of optimal financing of R&D-intensive firms that uses their unique features—large capital outlays, long gestation periods, and low probabilities of R&D success—to explain three prominent stylized facts about these firms: their relatively low use of debt, large cash balances, and underinvestment in R&D. This model relies on three key frictions: adverse selection, moral hazard from risk shifting, and costs from “two-audience” proprietary information disclosure. We establish the optimal pecking order of securities with direct market financing when information disclosure partially endogenizes the extent of adverse selection. Using the familiar debt tradeoff between tax benefits and the costs of risk shifting, we show that under plausible conditions, equity dominates debt, and firms raise enough financing to carry excess cash. However, market financing still leaves potentially valuable R&D investments unfunded. We then use a mechanism design approach to explore the potential of intermediated financing, with a binding precommitment by firm insiders to make costly ex post payouts. We show that a mechanism consisting of put options can be used in combination with equity to eliminate underinvestment in R&D and improve welfare relative to the direct market financing outcome. This optimal intermediary-assisted mechanism consists of bilateral “insurance” contracts, with investors offering firms insurance against R&D failure and firms offering investors insurance against very high R&D payoffs not being realized.

Keywords: R&D Investments; Healthcare Finance; Pharmaceutical Industry; Biotechnology Industry; Capital Structure; Information Disclosure; Debt Tax Shield; Mechanism Design

JEL Classification: D82, D83, G31, G32, G34, L65, O32

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1 Introduction

What is the optimal way for an R&D-intensive firm to finance itself? This question is especially urgent given the economic and social value created by R&D investment, and the evidence of a “funding gap” for innovation that creates underinvestment in R&D (see Hall and Lerner (2010)). Because this funding gap is only partly mitigated by venture capital, many potentially transformative innovations are not being realized or even pursued. Is there a market failure of existing financing mechanisms that systematically creates a “Valley of Death” for early stage R&D funding, and if so, how can the R&D financing mix address this failure? We address these issues theoretically in this paper.

Some suggested reasons for this funding gap include the following unique features of R&D-intensive firms:

1. R&D can be a very high investment cost for a project. For example, the development cost of a single new drug in the biopharmaceutical sector is estimated to be $2.6 billion (see DiMasi, Grabowski, and Hansen (2014)).

2. R&D investments often have long gestation periods, consisting of multiple phases of binary outcomes. Moreover, R&D investments involve a sequence of escalating resource commitments, requiring substantial specialized knowledge (see DiMasi et al. (1991) and Nanda and Kerr (2015)). In contrast, other industries, such as manufacturing, have a more continuous investment process.

\[\text{Brown, Fazzari, and Petersen (2009)}\] empirically document a significant link between financing supply and R&D. Lerner, Shane, and Tsai (2003) show that biotechnology firms are more likely to fund R&D through potentially inefficient alliances during periods of limited public market financing. Thakor et al. (2016) document that pharmaceutical and biotechnology companies have a significant exposure to the wellbeing of the economy. Kerr and Nanda (2015) provide a review of the literature related to financing and innovation. See also Fernandez, Stein, and Lo (2012) and Fagnan, Fernandez, Lo, and Stein (2013), who argue that R&D has become more difficult to finance through traditional methods, and thus that more innovative financing methods are needed to continue drug development in the future.

\[\text{DiMasi and Grabowski (2007)}\] estimated the average capitalized cost of a new drug to exceed $1 billion as of the mid-2000s, suggesting that this cost has been increasing over time. It is not uncommon for a pharmaceutical firm to invest fifty times as much in the R&D needed to develop a new drug as it does in the property, plant, and equipment to manufacture the drug.
3. R&D investments generally have low probabilities of success (see DiMasi et al. (1991, 2013)), but high payoffs conditional on success (e.g. Grabowski, Vernon, and DiMasi (2002), DiMasi, Grabowski, and Vernon (2004), and Nanda and Kerr (2015)).

4. Large R&D outlays rely on external financing to fund them. R&D-intensive firms are exposed by this last feature to many financing frictions, including adverse selection from uncertainty about the payoff potential of R&D, moral hazard from risk shifting, and costs from “two-audience” information disclosure signaling, because information disclosed to investors in order to obtain financing also becomes available to competitors, thereby diminishing the value of R&D (see Kamien and Schwartz (1978) and Bhattacharya and Ritter (1983)). These financing frictions have important implications for the capital structure choices of R&D-intensive firms.

The goal of this paper is threefold: to examine how these financing frictions theoretically interact with the unique features of R&D-intensive firms to influence their capital structure, how residual adverse selection problems may be left unresolved by standard debt and equity contracts used in the optimal capital structure, and how intermediary-assisted non-market solutions may be used to reduce the funding gap created by these unresolved adverse selection problems. We show that the optimal financing for R&D-intensive firms will involve a combination of market financing and a novel form of intermediary-assisted financing.

Our model has four key features. The first is taxes. R&D investments must be expensed, and these expenses are tax-deductible, as are payments to bondholders. Second, there is adverse selection related to the quality of the firm’s R&D, with the firm’s insiders knowing more than outside investors. Third, the firm can engage in unobservable risk shifting that can expropriate wealth from bondholders. Finally, adverse selection invites firms to disclose

\[ See \text{Lerner, Shane, and Tsai (2003), Brown, Fazzari, and Petersen (2009), and Acharya and Xu (2013) for empirical evidence of the reliance of these firms on the broader equity market. Also see Thakor et al. (2016) for empirical evidence of this for pharmaceutical and biotechnology companies.}

\[ For \text{example, see Jones (2007) for empirical evidence on the costs and benefits of information disclosure for R&D-intensive industries. In this paper, we focus on the costs of direct and verifiable disclosure. There may also be product market spillover costs associated with firms signaling to the financial market through, e.g., capital structure, as in Gertner, Gibbons, and Scharfstein (1988).} \]
information to investors in order to reduce the cost of external financing. However, this also reveals information to its competitors, reducing the value of the firm’s R&D.

There are a few noteworthy points about information disclosure in this setting. In many cases, a firm’s early stage R&D may not yield enough for a patent to be filed. As a result, disclosure may be damaging to a firm if it increases the odds of competitors preempts its R&D efforts. However, U.S. patent law allows some patents—such as those for drug compounds—to be filed relatively early on in the R&D process. By filing a patent, a firm both discloses information about its R&D and gains protection from product imitation.\(^5\) Given this protection, why should a firm fear additional information disclosure? There are at least two reasons. First, while patents can protect intellectual property, they do not guarantee market exclusivity.\(^6\) Second, even after filing a patent, there are some aspects of a firm’s R&D that the firm knows more about than its competitors, an informational advantage that disclosure can erode. For example, a biopharma firm may disclose information about a particular organic compound and the results of clinical trials through a patent filing, but the firm itself may still retain precise knowledge of the promise of the results, alternative applications of the drug, and other specifics about the commercial value of the R&D.

A firm makes the following decisions in our model: how much financing to raise at the outset, how much of the financing to raise from debt and how much from equity, and how much information to disclose at the outset. We show that the firm will raise all of the financing it is likely to need, both at present and in the future, right at the outset, investing some of it initially, and carrying the rest as cash. We also identify the conditions under which the pecking order of financing is first internal cash, then equity, followed by debt. As a result, all initial financing is raised through (outside) equity. Given the optimal capital

\(^5\)In addition, specifically for biopharma firms, the results of clinical trials are required to be reported to the FDA, and then publicly disclosed.

\(^6\)For example, in drug development, a firm can file for market exclusivity only after a drug has passed the final phase of approval with the FDA; until that point, it faces the risk of another firm getting to that phase in less time. Since the Hatch-Waxman Act of 1984, drug developers could skip the first few phases of clinical trials so long as some other firm has shown bioequivalence. This system was put into place in order to strike a balance between encouraging innovation (through market exclusivity) and allowing generic drugs to enter into the marketplace.
structure, we also solve endogenously for the amount of information disclosed by the firm.

The optimal capital structure results from the well-known tradeoff between the cost of risk shifting with debt and the value of the debt tax shield. However, even with this familiar tradeoff, we are able to show a reversal of the Myers and Majluf (1984) debt-equity pecking order for R&D-intensive firms. Three factors contribute to this reversal.\(^7\) First, R&D expenses are tax-deductible, and we show that this reduces the value of the debt tax shield. Second, engaging in risk shifting is considerably easier for firms with significant R&D than for other kinds of projects. It is also more difficult to detect, due to the technical nature of R&D and the relatively low probabilities of success of R&D projects. Third, debt optimally results in more information disclosure than equity, thereby resulting in higher proprietary information signaling costs. This means that debt financing of R&D-intensive firms has higher costs and smaller benefits than in other firms. We also show that, despite information disclosure, some asymmetric information remains unresolved, and this causes underinvestment in R&D.

An R&D-intensive firm raises more financing than it needs for immediate investment—and thus carries extra cash—because the more the firm knows relative to the market, the more its disclosure will reveal to its competitors. Thus, the losses related to information disclosure will be greater the more the firm knows. Since raising external financing conveys information, it is better for the firm to raise as much financing as it can at the outset, when its knowledge of what the R&D will produce is relatively low, rather than later, when it will know more. This justification for large cash holdings of R&D-intensive firms is distinct from either precautionary or tax-related motives for holding cash.\(^8\)

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\(^7\)This pecking order is based on the assumption that the firm has no assets other than the option to invest in R&D. As a result, the Myers and Majluf (1984) pecking order does not arise here in part because we have no assets in place in our model.

\(^8\)For example, Bolton, Chen, and Wang (2014) develop a model in which firms have a precautionary demand for liquidity, and thus build up cash reserves and hold low levels of debt in order to prevent liquidity from being drained for debt servicing. In contrast, we focus on the role of information disclosure costs in inducing firms to hold excess cash—thus, a firm in our setup will want to hold cash to avoid disclosure even if it has no need to protect against future bad states. Moreover, in our framework, firms also maintain low leverage due to the shortcomings of debt related to other frictions such as the tax expensing of R&D, information disclosure, and risk shifting.
Our model explains four important stylized facts about R&D-intensive firms. First, these firms use very little leverage in their capital structure (e.g. Himmelberg and Petersen (1994) and Thakor and Lo (2016)), and there is a negative correlation between leverage and R&D investments (e.g. Bradley, Jarrell, and Kim (1984)). Second, there appears to be underinvestment in R&D—the funding gap—even by firms that are publicly traded and have access to the capital market (see Hall and Lerner (2010)). Third, these firms tend to hold large cash balances (e.g. Begenau and Palazzo (2016) and Thakor and Lo (2016); also see Brown and Petersen (2011) and Bates, Kahle, and Stulz (2009) for evidence that greater R&D intensity leads to higher cash balances). Fourth, R&D-intensive firms rely on stock issues to finance R&D (e.g. Brown, Fazzari, and Petersen (2009)), and hence do not display the often-discussed aversion of other firms to equity issuance (e.g. Myers and Majluf (1984)).

Our result on capital structure differs from the standard theoretical argument that R&D-intensive firms avoid debt because knowledge assets have little collateral value (e.g. Hart and Moore (1994) and Rampini and Viswanathan (2010)). The importance of tangible assets for debt capacity is well documented empirically. However, it has also been documented that intangible assets also provide debt capacity. Lim, Macias, and Moeller (2014) find that both tangible and intangible assets are positively related to leverage, with intangible assets supporting half as much debt as tangible assets. Consistent with this fact, R&D-intensive firms are able to rely on their stock of knowledge patents as a source of collateral (see Mann (2014)). Moreover, Byoun, Moore, and Xu (2012) find that debt-free firms do have tangible assets to offer as collateral and have enough profitability to pay high dividends. All of these findings point to factors other than asset tangibility that may influence a firm’s debt decision.

The empirically documented “R&D funding gap” under market financing that arises in our analysis leads us directly to the next phase of our analysis. We explore whether it is possible to improve upon the traditional capital market funding of R&D-intensive firms by

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9He and Wintoki (2014) document that the sensitivity of cash holdings to R&D investments among R&D-intensive firms has increased dramatically in the last 30 years, and that increased competition seems to be an important driver of this, which is consistent with the evidence of Thakor and Lo (2016).
introducing an intermediary that is able to extract a binding precommitment from the firm’s insiders to make costly ex post payouts from their personal wealth endowment. We also design a mechanism to elicit truthful reports from firms about their private information on the expected cash flow enhancement from an additional R&D investment.\textsuperscript{10} This mechanism design uses a put option on the firm’s value that has an attached digital option such that over some range of firm values, the firm’s insiders are long the option and outside investors are short the option, whereas for all other firm values, insiders are short the option and outside investors are long. The basis for this mechanism design is as follows. Firm insiders are asked to report the likelihood of success of their additional R&D investment, and are also asked to provide “insurance” to investors against the possibility that the firm’s R&D fails to achieve relatively high cash flows, i.e., a put option. The amount of insurance that insiders must provide is larger if the firm reports a higher probability of success. The mechanism thus deters insiders from misrepresenting their R&D as having very probable high cash flows, while it (partially) protects investors against the firm’s failure to realize high R&D cash flows.

However, providing such insurance to investors is costly for the firm’s insiders. To offset this cost, the mechanism also includes a put option offered by the firm’s investors to the firm’s insiders, which insures the insiders against very low cash flows. Thus, through this mechanism, investors are provided a stronger assurance of a relatively high upside, while insiders are provided stronger protection against the downside.\textsuperscript{11} Potential underinvestment in R&D is thus discouraged both by insiders underinvesting due to a high possibility of failure, and by investors underinvesting due to a suspicion that the probability of high payoffs is too low (i.e., adverse selection). We view this arrangement as intermediated finance because the binding precommitment and coordination in the optimal mechanism may not be sustainable in a market setting.

\textsuperscript{10}The government or a third-party entity such as an exchange could play the role of this intermediary.

\textsuperscript{11}Although we do not have risk aversion in our model, this mechanism has an interesting interpretation in terms of encouraging risk-averse entrepreneurs to invest in R&D.
We argue that these options function as a form of bilateral insurance between investors and insiders, enabling them to protect each other against undesirable outcomes, thus allowing firms to make welfare-enhancing R&D investments. While some existing contracts suggest the idea of failure insurance for entrepreneurs, a novel normative aspect of our mechanism design is the put option sold by insiders to investors, as we discuss below. In terms of implementing our proposed mechanism, we relate these options to several recently proposed biopharma innovations such as FDA swaps and hedges (see Philipson (2015) and Jørring et. al. (2016)) and “phase 2 development insurance”. Our analysis reveals the potential benefits of coordinating mechanisms between firms and investors to induce precommitment in R&D financing.

While our analysis of capital structure focuses on R&D-intensive firms, it also has broader implications for financing decisions in other industries where the probability of success is low, but the payoff conditional on success is high, and projects involve considerable technical expertise. The film industry is one such example, and novel financing mechanisms have already emerged in that industry along the lines predicted by our model.

In Section 2 we review the related literature. We introduce our model in Section 3. Section 4 contains the analysis of direct market financing, as well as a discussion of extensions to this analysis. Section 5 contains the analysis of the mechanism design. We conclude in Section 6.

2 Related Literature

Our model is related to the vast theoretical literature on optimal capital structure. Starting with the seminal paper by Modigliani and Miller (1958) on the irrelevance of capital structure in a frictionless environment, subsequent papers have focused on the way various frictions push firms towards a certain optimal mix of debt and equity. Jensen and Meckling (1976), Miller (1977), Myers (1977), Leland and Pyle (1977), Myers and Majluf (1984), Zweibel
(1996), Fluck (1998), Bolton, Chen, and Wang (2014), and Abel (2014), among others, propose theories of optimal capital structure based on the role of frictions stemming from asymmetric information, agency problems, and tax distortions. For several more complete reviews, see Harris and Raviv (1991), Frank and Goyal (2005), and Myers (2001). In part, this literature has focused on the so-called pecking order of securities used to raise financing, with Myers and Majluf (1984) showing that equity is a last resort. More recent papers, like Fulghieri, Garcia, and Hackbarth (2015), have derived conditions under which this pecking order is reversed. While we also examine the optimal capital structure in the presence of asymmetric information and agency problems, we show how these frictions interact with the unique features of R&D-intensive firms to deliver different predictions about optimal capital structure, even within the well-known tradeoff between the risk shifting cost of debt and its tax benefit. Our analysis relative to this literature has two key distinguishing features, first, that the expensing of R&D reduces the tax shield attributable to debt, and second, that the costs of proprietary information disclosure contribute to the choice of R&D-intensive firms to carry large cash balances. In other words, risk shifting, the expensing of R&D for taxes, and proprietary disclosure costs can explain both the low levels of debt and the high levels of cash in R&D-intensive firms.

Our model is also related to the theoretical literature on incentives, decision-making, and contracts in R&D-intensive firms. For example, Aghion and Tirole (1994) use a contracting framework to examine the organization of R&D-intensive firms. While their focus is on the allocation of property rights and types of contracts that arise in such firms, however, our focus is on the optimal financing of R&D. Bhattacharya and Ritter (1983) point out the importance of disclosure with respect to R&D, while Bhattacharya and Chiesa (1995) examine the conditions under which R&D firms may choose bank funding over market debt to reduce disclosure costs. We incorporate information disclosure in our analysis, but we also examine

12 Other papers that have explored the optimal choice of security in a setting of pure adverse selection related to asymmetric information include Brennan and Kraus (1987), Noe (1988), and Nachman and Noe (1994).
the interaction between information disclosure and other frictions, and their effects on the funding decisions of R&D-intensive firms in the public debt and equity markets.\textsuperscript{13} Rather than focusing on the choice between market and intermediated debt, however, we examine how an intermediary, in conjunction with market financing, can reduce informational frictions, and hence increase R&D financing. Gertner, Gibbons, and Scharfstein (1988) develop a model in which the firm’s capital structure potentially signals proprietary R&D information to competitors in a firm’s product market. In contrast, in our analysis, capital structure does not play a signaling role, since it communicates no information beyond that contained in direct and verifiable disclosure.

In addition, we also examine how an intermediary-assisted mechanism may be used to improve the optimal investment in R&D. Our paper is thus related to Nanda and Rhodes-Kropf (forthcoming), who show that “financing risk”—a forecast of limited future funding—disproportionately affects innovative ventures with the greatest option values. They propose that highly innovative technologies may need “hot” financial markets to be adequately funded. We take an alternative theoretical approach to this R&D funding gap, and derive a mechanism that mitigates it.\textsuperscript{14} This connects our paper to the mechanism design literature (see Myerson (1979, 1982) and Baron and Myerson (1982) for important early contributions, and Tirole (2012) and Phillipon and Skreta (2012) for more recent contributions).

3 The Model

Consider an economy in which all agents are risk neutral and the riskless rate is zero. There are R&D-intensive firms, each of which has no assets in place or cash at the beginning, date.

\textsuperscript{13}Szydlowski (2016) examines, in a general setting, how a firm’s disclosure policy depends on its choice of financing. In our paper, a firm’s disclosure policy and choice of financing are also endogenously codetermined. However we focus specifically on R&D-intensive firms and how their unique characteristics interact with their disclosure and financing decisions to lead to an optimal mix of market and intermediary-assisted financing.

\textsuperscript{14}Another related paper is Myers and Read (2014), who examine financing policy in a setting with taxes for firms with significant real options. While the R&D projects of biopharma firms can be viewed as real options, we take a different theoretical approach in order to focus on frictions related to asymmetric information and moral hazard.
$t = 0$. The initial owners of the firm have some personal assets (not part of the firm) that are illiquid at $t = 0$ and will deliver a payoff of $\Lambda \in \mathbb{R}_+$ at $t = 3$ if held until $t = 3$. These assets, if liquidated at $t = 0$, can be used by the initial owners of the firm to self-finance the necessary investment in R&D that the firm needs to make at $t = 1$. However, because these personal assets are illiquid, they will fetch only $l\Lambda$ if liquidated at $t = 0$, where $l \in (0, 1)$. Thus, absent liquidation of these personal assets, all financing needed for R&D must be raised from external financiers. All securities are raised in a competitive capital market, so the expected return for all investors who provide financing to the firm is zero.

The firm needs $\omega R$ in capital at $t = 1$ to make the initial investment in R&D to develop a new idea, conduct clinical trials, etc., where $\omega \in (0, 1)$ and $R > 0$. If the clinical trials and other exploratory research financed by the initial investment $\omega R$ deliver good results, then the firm will make a bigger subsequent investment of $R$ in R&D at $t = 2$; otherwise it will cease further investment. The initial investment of $\omega R$ does not produce any cash flow. Its value lies solely in what it reveals about the payoff prospects of the bigger investment at $t = 2$. This setup mimics the staged R&D investment setup that is typical in R&D-intensive firms such as biopharma firms, which conduct multiple phases of drug development, each with escalating resource commitments. The corporate tax rate is $\tau \in (0, 1)$.

Let $q \in (0, 1)$ be the probability assessment at $t = 0$ that the initial R&D will yield good results ($G$) at $t = 2$ and $1 - q$ the probability that it will yield bad results ($B$) at $t = 2$. If the R&D yields good results, then investing $R$ at $t = 2$ will generate a probability $\delta \in (0, 1)$ of achieving a high cash flow distribution, i.e., the terminal (date $t = 3$) cash flow $x$ will have a cumulative distribution function $H$ with support $[x_L, x_H]$ and $x_L > R(1 + \omega)$. With good results there is a probability $1 - \delta$ of achieving a low cash flow $x$ that has a cumulative distribution function $L$ with support $[0, x_L]$. It is assumed that

$$\int_{x_L}^{x_H} x[1 - \tau] \, dH > R[1 + \omega],$$

(1)
and
\[ \int_0^{x_L} x[1 - \tau] \, dL + \Gamma_c = R[1 - \tau] + \omega R \tau, \]  
(2)

where
\[ \Gamma_c \equiv \tau \left\{ \int_0^{R[1 + \omega]} x \, dL + \int_{R[1 + \omega]}^{x_L} R[1 + \omega] \, dL \right\}, \]  
(3)

\( \varepsilon > 0 \) is an arbitrarily small positive scalar, and \( \Gamma_c \) is the tax shield associated with expensing R&D (the entire \( R[1 + \omega] \)) when the payoff distribution is \( L \). The idea is that, with a good result in the first stage, the lowest expected payoff equals the second-stage investment plus a small amount. If the R&D yields bad results (failure), then any investment at \( t = 2 \) leads to a zero cash flow almost surely at \( t = 3 \). The final commercial outcome of the R&D project conditional on success, therefore, may be either a “blockbuster” (with cash flows given by (1)) or a much smaller commercial success (given by (2)).\(^{15}\)

If, and only if, the firm invested \( \omega R \) at \( t = 1 \) will it have an opportunity to learn whether the outcome of the initial R&D is good or bad at \( t = 2 \). If it does not invest \( \omega R \) in the initial R&D, then it learns nothing at \( t = 2 \) almost surely. In other words, the initial investment in R&D is a necessary and sufficient condition for deciding at \( t = 2 \) whether it is worth proceeding further with the project.

Finally, if the firm invests \( R \) at \( t = 2 \), it also has the opportunity to invest an additional additional \( \Delta R > 0 \) at \( t = 2 \). If it does so, then there is a probability \( r \in [r_a, r_b] \) that the high cash flow distribution (given by (1)) can be enhanced from \( H \) to \( J \), where \( J \) is distributed over the support \([x_H, x_J]\). That is, if the firm invests an additional \( \Delta R \) in R&D at \( t = 2 \), then in the state in which the R&D yields good results and the firm has a high cash flow distribution (joint probability \( q \delta \)), there is a probability \( r \) that \( x \) will be distributed according to \( J \) and a probability \( 1 - r \) that it will be distributed according to \( H \), where \( J \) first-order-stochastically dominates \( H \). This R&D-enhancement can be interpreted as an alternate commercial application of the R&D project that can be revealed with additional

\(^{15}\)For the case of drug development in biopharma firms, this is consistent with the empirical evidence of Grabowski and Vernon (1990).
exploration. For example, a given medicinal compound that is targeted for a particular disease may also have wider (and potentially socially valuable) applications that were not initially considered at the start of the project, and these applications may be confirmed with additional exploration or expanded trials. If the firm has the cash to invest $R$ and $\triangle R$ in R&D but chooses not to do so, at $t = 2$, the cash will be kept idle until $t = 3$ if the firm is sound. If it is unsound, it will abscond with the cash.

In Figure 1, we graphically summarize the setup of staged R&D investment in the model.

### 3.1 The Firm’s Initial Investment Decision

At $t = 0$, the firm’s initial owners determine how much external financing to raise, the capital structure of the firm, and the firm’s decision of how much information, $\xi$, to disclose. The firm chooses between debt and equity for its capital structure at $t = 0$; both debt and equity investors’ claims are paid off at $t = 3$. At $t = 2$, after observing the outcome of the first-stage R&D, the firm may choose to raise additional external financing through debt and/or equity. The financing decisions are made by the firm’s owners, while all other decisions are made by a manager, who privately observes at $t = 1$ whether a worthwhile R&D project is available, and then privately observes whether the first-stage R&D produced a good or a bad outcome at $t = 2$. Thus, it is the manager who decides whether to invest $\omega R$ in the first-stage R&D at $t = 1$ and whether to invest $R$ in the second-stage R&D at $t = 2$ or keep the cash idle. We assume that the manager makes all decisions in the best interests of the initial owners.

This specification of decision control seems natural to us. The initial owners (insiders) make the important strategic decisions about capital raising, capital structure, and information disclosure. But the details of R&D are technical in nature and thus delegated to the manager who possesses the necessary expertise to evaluate whether the first-stage R&D was successful and whether more resources should be committed to the R&D. This is related
Figure 1: Summary of R&D Investment Timing (Absent Competitive Entry)
to an important assumption in our analysis: the R&D conducted by the firm relies on and generates highly specialized knowledge that the financiers may lack.

3.2 Informational Frictions

The model has three informational frictions: adverse selection, uncertainty about the upside of R&D, and risk-shifting.

**Adverse Selection:** At $t = 0$, there is a possibility that the firm is “sound”, in which case it has the opportunities described above, and there is also a possibility that it is “unsound”. An unsound firm has no idea worth investing in via R&D, so it will simply raise external financing at $t = 0$ and consume it. The common prior belief is that the probability that the firm is sound is $s \in (0, 1)$ and the probability that the firm is unsound is $1 - s$. The firm, its initial owners, and its manager know whether it is sound or unsound, but this is private information; investors cannot distinguish between sound and unsound firms.

**Upside Uncertainty:** The second informational friction is that, within the set of sound firms, there is unobservable heterogeneity with respect to $r$, the probability that the the high cash flow distribution in (1) can be enhanced from $H$ to $J$—each firm’s initial owners and manager know $r$, but others do not. It is common knowledge that $r$ is distributed in the cross-section of sound firms over $[r_a, r_b]$ according to the probability density function $z$ (with associated cumulative distribution function $Z$).

**“Buying Risk”: The Risk-shifting Opportunity:** After securities are issued, the manager (on behalf of the initial shareholders) can unobservably change the riskiness of the R&D payoff distributions at $t = 2$. We assume that the manager can increase the measure of the support of $L, H$, as well as $J$ by $2\nu$, where $\nu > 0$ is finite. That is, the manager can choose $\nu \in [0, \nu_m] \subset \mathbb{R}$ such that the lower end point of the support of the distribution decreases
by \( \nu \) and the upper end point increases by \( \nu \), with the following property being satisfied:

\[
\int_{-\nu}^{x_L+\nu} x \, dL - \int_{-\nu}^{x_L} x \, dL = \int_{x_L-\nu}^{x_H+\nu} x \, dH - \int_{x_L-\nu}^{x_H} x \, dH
\]

\[
= \int_{x_H-\nu}^{x_J+\nu} x \, dH - \int_{x_H}^{x_J} x \, dH
\]

\[
= 0 \tag{4}
\]

If the manager chooses to increase risk like this, he must do it for all three distributions.

However, to “buy” this additional risk, the manager must be willing to accept a pointwise reduction of \( m = \kappa \nu, \kappa \in (0, 1) \), in the realized value of the payoff under each of the three distributions, which yields a first-order-stochastic dominance shift of \( m \) to the left for each distribution. That is, for any chosen \( \nu \in [0, \nu_m] \subset \mathbb{R}_+ \), we have

\[
\int_0^{x_L} x \, dL - \int_{-\nu-m}^{x_L+\nu-m} x \, dL = \int_{x_L}^{x_H} x \, dH - \int_{x_L-\nu-m}^{x_H+\nu-m} x \, dH
\]

\[
= \int_{x_H}^{x_J} x \, dH - \int_{x_H-\nu-m}^{x_J+\nu-m} x \, dH
\]

\[
= m = \kappa \nu \tag{5}
\]

Given (4) and (5), it is clear that risk-shifting is inefficient—it leads to a lower total firm value. To capture the intuitive idea that higher cash flows permit more risk-shifting, we assume that \( \nu_m \) is a function of \( x_H \), with \( \partial \nu_m / \partial x_H > 0 \). In other words, when the upper endpoint of the high cash flow distribution is higher, it is easier for the firm to engage in (ex ante undetectable) risk shifting.

As the subsequent analysis will show, the manager has no incentive to engage in risk shifting when the firm has no leverage. However, with leverage, inefficient risk-shifting arises because the manager can increase the value of the initial owners’ equity by doing so. The risk shifting involves increasing the variance of R&D payoffs, which is a classical risk-shifting strategy. Such flexibility for the manager has been modeled in many contexts previously.
Jensen and Meckling (1976) introduced it in the context of capital structure, as we do here. Aumann and Perles (1965) discussed it in the context of the “variational problem” in which an agent who is rewared on the basis of the realization of a (non-negative) random variable can select any distribution for the random variable, subject only to a restriction that the mean of the random variable does not exceed an exogenous constant. Makarov and Plantin (2015) examine this in the context of risk shifting by agents who are willing to take large risks to maximize expected compensation.

We believe that such risk shifting is especially important in R&D-intensive firms because three features of R&D make it very difficult to detect and prevent it through monitoring and contracting. The first feature is that R&D has long gestation periods, so bondholders may be unable to observe in a timely manner signals that inform them that risk has been increased. The second feature is the technical nature of most R&D, and the fact that managers tend to have specialized expertise in the R&D which bondholders and other stakeholders do not. This may make it difficult for bondholders to ascertain the precise riskiness of the project even when signals are available, because these signals are hard to interpret, thus making it hard for bondholders to prevent managerial risk shifting. And the third feature is that R&D has a low success probability anyway, so a shift to riskier R&D with an even lower success probability may be hard to catch.

3.3 Taxes

Any investment in R&D must be expensed for tax purposes and thus provides a tax shield. Similarly, all debt repayments are treated as tax deductible.

3.4 The Effect of Information Disclosure

When the firm raises financing at \( t = 0 \), it can decide how much information it wishes to disclose. Let \( \xi \), chosen from a compact set \( [\xi_{\text{min}}, \xi_{\text{max}}] \), denote the extent of information disclosure. Information disclosure has two effects, one on the investors providing the financing,
and the other on the firm’s potential competitors who may decide to jump in and invest in
the same kind of R&D, thereby triggering an R&D “arms race” that will negatively impact
the firm’s cash flow distribution. That is, the firm faces a “two-audience” signaling problem
in its choice of disclosure.\textsuperscript{16}

Since the amount of information disclosure $\xi$ pertains to the quality/profitability of the
base R&D project, if it is available, it conveys no information about incremental value
enhancement due to investing the additional $\Delta R$. That is, $\xi$ conveys no information about
$r$. Let $\bar{r}$ be the expected value of $r$ to investors and other outsiders, i.e., $\bar{r} = \int_{r_a}^{r_b} rzdr$. This
is meant to capture the fact that while information disclosure may help to reduce some of
the asymmetric information pertaining R&D projects, there are some aspects of R&D that
the firm knows more about than the market, and its voluntary information disclosure is not
able to lessen this information asymmetry. The effects of the disclosure $\xi$ on the firm’s R&D
competitors and investors are described next.

For investors, the effect of disclosure $\xi$ is to create a noisy but informative signal $\phi$ of the
soundness of the firm which has the following probability distribution:

$$\Pr (\phi = \text{unsound} \mid \xi, \text{firm is unsound}) = p(\xi), \quad (6)$$

where $p' > 0$, $p'' < 0$, $\forall \xi \in [\xi_{\text{min}}, \xi_{\text{max}}]$, and the Inada-type condition $p'(\xi_{\text{max}}) = 0$ holds.
This means that the precision of the investors’ signal that the firm is sound is positively
related to the amount of information disclosed by the firm. It is assumed that:

$$\Pr (\phi = \text{sound} \mid \xi = \xi_{\text{min}}, \text{firm is sound}) = \Pr (\phi = \text{sound} \mid \xi = \xi_{\text{min}}, \text{firm is unsound})$$
$$= p(\xi_{\text{min}}) = \frac{1}{2}. \quad (7)$$

\textsuperscript{16}As discussed in the introduction, while a firm may have to publicly disclose some aspects of its R&D
through either patent filings, there will still be valuable private information about the future prospects
of the R&D that the firm does not disclose. This problem would be particularly acute for the biopharma
industry, as drug research is essentially winner-takes-all—the firm that successfully completes R&D and gets
their drug approved through the FDA gets a monopoly on the drug through “exclusivity” marketing rights
granted through the patent process, and can reap the very high cash flows that may come with such drugs.
Let $\hat{s}(\xi)$ be the posterior probability that investors have that the firm is sound, after it has disclosed $\xi$. Here, $\xi_{\text{min}}$ should be interpreted as the minimum level of information disclosure required by the securities regulator or stock exchange. This would involve the amount of funds to be raised, the number of shares to be issued, and other terms and conditions related to the capital raising. The specification above states that this minimum level is not sufficient to produce an informative signal.

Disclosure occurs whenever external financing is raised. The effect of disclosure on competitors is as follows. Imagine, for simplicity, that the firm has only one competitor who may come in. If the firm discloses information about its R&D when it raises financing at $t = 0$, this competitor can update its belief about the value of entering the race. We assume that the more the firm discloses, the higher the probability of competitive entry, and that this entry will drive down the prospects of the firm being able to profitably continue to develop its R&D in the second stage starting at $t = 2$. This is modeled by assuming that a higher $\xi$ leads to a higher probability of competitive entry, $\theta(\xi) \in [0, 1]$, with $\theta'(\xi) > 0$ and $\theta''(\xi) > 0$. In addition, $\theta(\xi_{\text{min}}) = 0$, $\theta(\xi_{\text{max}}) = \bar{\theta}$, and the Inada-type conditions hold: $\theta'(\xi_{\text{min}}) = \infty$ and $\theta'(\xi_{\text{max}}) = 0$. If there is no competitive entry due to information disclosure, the probability of a good first-stage R&D outcome for the firm is $q = \bar{q}$, and if there is competitive entry it is $q = q$, with $0 < q < \bar{q} < 1$. We will assume that $\bar{q} > 2q$.\(^{17}\)

### 3.5 The Firm’s Second-Stage Investment Decision

We will assume that it will be worthwhile for the firm to invest $R$ in further R&D at $t = 2$ only if its first-period R&D yielded good results ($G$). If it learns that the first-period R&D yielded bad results, then it has no incentive to invest $R$ in further R&D at $t = 2$ since the payoff from doing so is 0.

\(^{17}\)This is a minor technical condition used in the proof of Proposition 2, which ensures that competitive entry has a significant impact on the first-stage probability of success.
It is convenient to define the following:

\[ \mu_H \equiv \int_{x_L}^{x_H} x \, dH, \quad \mu_L \equiv \int_{0}^{x_L} x \, dL, \]  
(8)

and

\[ \bar{G} \equiv \delta \mu_H[1 - \tau] + [1 - \delta] \mu_L[1 - \tau], \]  
(9)

where \( \bar{G} \) is the after-tax expected value of the R&D in the good state (without competitive entry). Further,

\[ \Gamma_n \equiv \delta \tau R[1 + \omega] + [1 - \delta] \tau \left\{ \int_{R[1+\omega]}^{x_L} R[1+\omega] \, dL + \int_{0}^{R[1+\omega]} x \, dL \right\} \]  
(10)

is the expected value of the tax shield provided by the expensing of the R&D in the good state with no competitive entry.

We further make the following assumptions:

\[ q[\bar{G} + \Gamma_n] < R[1 - \tau] + \omega R\tau, \]  
(11)

\[ \omega R < q[\bar{G} + \Gamma_n - R[1 - \tau] - \omega R\tau]. \]  
(12)

Note that \( q[\bar{G} + \Gamma_n] \) is the expected value of investing \( R \) in the second stage. If \( R \) is kept idle, then the cash flow is \( R \) and \( \omega R \) can be treated as a tax-deductible R&D expense. Thus, the after-tax cash flow is the right-hand side of (12). Condition (11) says that absent the signal at \( t = 1 \) about the outcome of the first-stage R&D, the firm will choose not to invest \( R \) in the second stage, and condition (12) says that the expected value of the option to invest \( R \) in R&D in the second stage exceeds the investment \( \omega R \) in R&D in the first stage for any value of \( q \).
3.6 The Effect of Competitive Entry due to Information Disclosure in the Second-Stage

Competitive entry has two effects on the profitability of R&D. First, if a competitor enters at \( t = 0 \) and also invests \( \omega R \), then the first-stage R&D will yield a good outcome (success) with probability \( q \). Since competitive entry at \( t = 0 \) reduces the probability of R&D success to \( q \) for both firms, the two firms’ first-stage R&D outcomes are perfectly correlated. Second, if both firms are competing, then even conditional on a good first-period R&D outcome, the second-period R&D is less profitable. This is captured by assuming that the payoff distribution \( H \) vanishes and each firm’s cash flow is driven with probability 1 by the distribution \( L \), i.e., the \( \text{NPV} \) of the investment at \( t = 2 \) to the firm that invested \( \omega R \) at \( t = 1 \) becomes arbitrarily small (see (2))).

Note that even if the competitor who enters at \( t = 0 \) does not make the investment \( R \) at \( t = 2 \), if it becomes publicly known that the firm achieved good results on its first-stage R&D, then any new competitor can come in at \( t = 2 \) and invest \( R \) in second-stage R&D.\(^{18}\) To ensure that a competitor will indeed wish to do this, we assume:

\[
\mu_L [1 - \tau] + \int_0^R x \tau dL + \int_R^{2L} R \tau dL \geq R. \quad (13)
\]

The left-hand side of (13) is the after-tax cash flow to a new entrant (who did not invest \( \omega R \) at \( t = 1 \)) from investing \( R \) at \( t = 2 \), and the right-hand side is the investment \( R \).

The assumption that higher competition has such a two-fold effect on R&D is a reasonable approximation of reality. On the one hand, competition creates an initial arms race between competing firms, which means that both are competing for and dividing up the available pool of human talent for the R&D and also suppliers who may come up with innovations

\(^{18}\)For example, the successful completion of research on the human genome project in the 1990s and 2000s—the results of which were publicly released—allowed a proliferation of biotech companies in the marketplace (see Thakor et al. (2016)). As another example, after the Hatch-Waxman bill of 1984 was passed for the biopharma industry, it became easier for generics to enter the marketplace by skipping initial trials if someone had previously proven efficacy (e.g. Grabowski (2007) and Thakor and Lo (2016)).
in inputs. Hence, \( q \) becomes lower. On the other hand, even if there is first-period R&D success, competition also has an adverse effect on second-period profits.

### 3.7 Discussion of the Setup of the Model

*Figure 2* summarizes the timeline of events. Note that formally this is a game in which the informed firm moves first with its financing and information disclosure decisions, and the uninformed investors move next. As *Figure 2* indicates, this model is rich, with many elements. We briefly summarize here the role these elements play in the model and how they correspond to biopharma firms in practice.

The first set of elements has to do with the sequential staged nature of R&D and escalating resource commitments over time. In our model, as in practice, there is an initial exploratory investment in R&D, followed by a subsequent (larger) investment if the initial R&D yields promising results. This is captured by an investment of \( \omega R \) at \( t = 1 \) and then a possible additional investment of \( R \) at \( t = 2 \), that is conditional on good (\( G \)) first-stage R&D results.

The second set of elements has to do with the pros and cons of information disclosure about the R&D. In practice, as in our model, the benefit of information disclosure is a reduction in the adverse-selection of external financing, which is captured by introducing a non-zero probability (\( 1 - s \)) of investors encountering an unsound firm. The cost is that the more information the firm discloses, the higher is the probability \( \theta \) that a competitor will enter and reduce the expected value of R&D to the firm. However, information disclosure pertains to only one aspect of R&D, leaving one informational asymmetry entirely unresolved.

The third set of elements has to do with informational frictions. The probability \( s \) of a firm being sound is introduced to capture adverse selection in external financing, which is a well-known friction. The ability to undertake a value-enhancing R&D investment \( \Delta R \) provides the opportunity for the firm to widen the commercial applicability of the project, while the probability \( r \) of finding a worthwhile R&D-enhancing project is introduced to capture
<table>
<thead>
<tr>
<th>$t = 0$</th>
<th>$t = 1$</th>
<th>$t = 2$</th>
<th>$t = 3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>• Sound firm needs $\omega R$ for initial R&amp;D investment and $R$ for later investment.</td>
<td>• Manager decides whether to invest $\omega R$ in an R&amp;D project (if there is a worthwhile one).</td>
<td>• If the firm invested at $t = 1$, then with probability $q$ the investment yields $G$ (good results), and with probability $1 - q$ that it yields $B$ (bad results).</td>
<td>• Final R&amp;D payoff $x$ is observed.</td>
</tr>
<tr>
<td>• Firm raises financing from debt, equity, or a mix</td>
<td></td>
<td>• $q = \bar{q}$ with no competitive entry, and $q = q &lt; \bar{q}$ with competitive entry.</td>
<td>• If firm invested $R$ at $t = 2$, then $x \sim H$ with probability $\delta$ and $x \sim L$ with probability $1 - \delta$.</td>
</tr>
<tr>
<td>• The firm’s initial owners (insiders) could also liquidate personal assets $\Lambda$ at a cost as an alternative to capital market financing.</td>
<td>• The firm may raise additional financing from debt, equity, or a mix. If the firm raises more capital at this stage, the firm discloses additional information.</td>
<td>• With $G$, firm invests $R$ at $t = 1$. May also invest additional $\Delta R$.</td>
<td>• If firm also invested additional $\Delta R$ at $t = 2$, then high cash-flow realization (which happens with probability $\delta$) becomes $x \sim J$ with probability $r$, or remains $x \sim H$ with probability $1 - r$.</td>
</tr>
<tr>
<td>• Probability is $s \in (0, 1)$ that the firm is sound and $1 - s$ that it is unsound.</td>
<td>• With $G$, firm invests $R$ at $t = 1$. May also invest additional $\Delta R$.</td>
<td>• With $B$, firm ceases further investment.</td>
<td>• Investors are paid off.</td>
</tr>
<tr>
<td>• The firm chooses how much information $\xi$ to disclose. This affects investors’ posterior beliefs that firm is sound as well as probability $\theta$ of competitive entry.</td>
<td>• The manager has the option to add risk to the R&amp;D payoff distributions.</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Figure 2: Time-line of Events and Decisions**
the idea that market financing may be incapable of resolving all informational problems. This leaves some room for mechanism design to play an incremental role, something we explore later in the paper. As discussed earlier, the manager’s ability to engage in risk shifting is particularly relevant in the context of R&D-intensive firms. The nature of R&D can be altered in subtle—and undetectable—ways ex post without changing the basic purpose of the R&D or violating any bond covenants.

The final feature worth discussing is taxes. Having taxes creates a debt tax shield and provides perhaps the most familiar reason for using debt. But the fact that R&D can be immediately expensed means that R&D-intensive firms also have large non-debt tax shields, an issue that affects the capital structure decision (e.g. DeAngelo and Masulis (1980)).

We assume throughout that the deadweight cost of liquidating personal assets makes it prohibitively expensive for insiders to raise all of the financing through personal-asset liquidation.

4 Analysis

We now analyze the model. The initial owners of the firm decide at $t = 0$: (1) how much financing to raise; (2) whether to raise financing with a mix of debt and equity, just debt, or just equity; and (3) how much information to disclose. For now, we will ignore the self-financing option for the initial owners, and verify later that there are conditions under which self-financing is not optimal.

The manager runs the R&D project. At $t = 1$, the manager will decide whether to invest $\omega R$ in initial R&D. At $t = 2$, he will have to determine whether to invest $R$ for further R&D, and also whether to undetectably engage in risk-shifting. The manager makes these decisions to maximize the wealth of the firm’s initial owners.
4.1 Definition of Equilibrium

We now define the equilibrium concept we use. This is a game in which the informed manager moves first by disclosing information and raising capital, and the uninformed investors respond by pricing the securities used to raise the financing.

**Equilibrium:** The competitive sequential equilibrium is one in which the informed manager makes decisions to maximize the expected wealth of the firm’s initial owners. The equilibrium is: (i) a triplet of strategies \( \{I, C, \xi\} \) chosen by the manager at \( t = 1 \), where \( I \) is the total financing raised for R&D, \( C \) is the capital structure (mix of debt and outside equity in the financing), and \( \xi \) is the information disclosed; (ii) investors’ best response in terms of the pricing of the firm’s securities at \( t = 1 \), conditional on their priors about whether the firm is sound, the information disclosed, and the probability \( \beta \) they attach to the manager engaging in risk-shifting at \( t = 2 \); (iii) the manager’s strategy at \( t = 2 \) about whether to raise additional financing, how much additional investment to make in R&D, and whether to engage in risk shifting, after observing whether competitive entry has occurred, with the manager’s actual probability of risk shifting being \( \beta \), the probability in the investors’ belief at \( t = 0 \); and (iv) a belief revision process for investors whereby all beliefs are revised according to Bayes Rule when the manager plays his equilibrium strategies, and an out-of-equilibrium belief that the firm is unsound if the manager plays some other strategy.

4.2 Analysis of Amount of Financing Raised

Our first result is about how much financing the firm will raise at \( t = 0 \).

**Proposition 1:** The firm will raise all of the financing it needs, \([1 + \omega] R\), at \( t = 0 \). It will invest \( \omega R \) in its first-stage R&D at \( t = 1 \) and carry a cash stockpile of \( R \) to date \( t = 2 \).

The intuition behind this result is that the firm will not want to raise additional capital

---

19All proofs are in the Appendix.
at $t = 2$ because doing so would signal project success not only to the market, but also to its competitors. Were there no information disclosure required, the firm could raise the needed financing “quietly”, without any revelation that financing was being raised. However, we know that at $t = 2$, if additional financing is raised, the information disclosure will be $\xi \geq \xi_{\text{min}}$. This will be enough to alert the firm’s competitors that financing is being raised, implying that the first-stage R&D (for a sound firm) was successful. Competitive entry at that point in time would reduce the margins of the project—something the firm would like to avoid. Thus, the firm will optimally want to raise all of its necessary capital earlier, when it knows less about the potential success of the R&D project, and its capital raising is consequently less informative.

Disclosure at $t = 0$ is “partial” and only increases the probability of competitive entry, $\theta$, thereby reducing the probability of a good R&D outcome at $t = 1$. But raising capital at $t = 2$ is tantamount to “full” disclosure about the value of the R&D (since it unambiguously reveals first-period R&D success), so it induces competitive entry with certainty, driving down profits. Thus, it is rational for the firm to disclose information at $t = 0$, before it knows how the first-period R&D will fare. In other words, it makes sense to raise considerable external financing when the firm knows less and then use it as an internal capital market to fund additional R&D when it knows more.\textsuperscript{20}

4.3 The Debt-Equity Choice and How Much Information to Disclose

Next we consider whether the firm will use debt or equity or some mix of the two to raise financing at $t = 0$.

\textsuperscript{20}The full revelation through capital raising at $t = 2$ is an assumption that could be weakened (some incremental information is revealed at $t = 2$) without changing the results. In this case, Proposition 1 would still hold, since the firm would want to raise all of its financing at $t = 0$ in order to avoid the incremental information disclosure that comes with capital raising at $t = 2$. 

25
4.3.1 Equity Financing

Consider first equity. It is clear that no risk-shifting will occur at $t = 2$ if the firm is all-equity-financed, so we can set $\beta = 0$ for this analysis. The firm now has to choose how much information to disclose. Let $f$ be the fraction of ownership that the initial owners sell to investors of the sound firm in order to raise $[1 + \omega] R$. That is, assume initially that $\Delta R$ is not raised. The initial owners of the sound firm solve the following maximization problem:

$$
\max_{\xi \in [0, \xi_{\text{max}}]} [1 - f] \Omega (\xi), \quad (14)
$$

subject to:

$$
\hat{s} (\xi) f [\Omega (\xi)] = [1 + \omega] R, \quad (15)
$$

$$
\Omega (\xi) \equiv \bar{q} [1 - \theta (\xi)] [\bar{G} + \Gamma_n] + [1 - \bar{q}] [1 - \theta (\xi)] [R[1 - \tau] + \omega R\tau],
$$

$$
+ \bar{q} \theta (\xi) [\mu_L[1 - \tau] + \Gamma_c] + [1 - \bar{q}] \theta (\xi) [R[1 - \tau] + \omega R\tau] \quad (16)
$$

and

$$
f \in [0, 1], \quad (17)
$$

where $\Gamma_c$ is defined in (3).

This maximization can be understood as follows. (14) is given by the initial owners maximizing their share of the total firm value $\Omega (\xi)$, when their post-financing ownership share is reduced to $[1 - f]$. Equation (15) is the outside investors’ equilibrium pricing constraint, where $\hat{s} (\xi)$ is the investors’ posterior belief that the firm is sound after the disclosure $\xi$ has occurred. Finally, (16) is the total firm value. If no competitive entry occurs (probability $1 - \theta (\xi)$), then the probability of success of the first-stage R&D is $\bar{q}$. Then, conditional on first-stage success, the second-stage R&D generates a firm value of $\bar{G} + \Gamma_n$, where $\Gamma_n$ is the value of the R&D tax shield in this state. If the first-stage R&D does not succeed
(probability $1 - \overline{q}$), cash $R$ sits idle. We assume it will be treated as income and taxed, but the $\omega R$ investment made earlier will be treated as an expense that generates a tax shield of $\tau \omega R$. This explains the first two terms in the braces in (16). For the third term, if competitive entry occurs (probability $\theta(\xi)$), then the first-stage R&D success probability drops to $q$, and the firm’s value is $\mu_L[1 - \tau]$ plus the tax shield $\Gamma_c$ associated with a payoff distribution of $L$ (which occurs with competitive entry). Finally, in this case with competitive entry (probability $\theta(\xi)$), if the first-stage R&D does not succeed (probability $1 - q$), cash $R$ sits idle, so the value is $R[1 - \tau] + \omega R\tau$, as explained earlier. This explains the fourth term in the braces in (16).

The next result connects the amount of information disclosure firms choose to the equity financing that they are able to secure:

**Lemma 1:** Conditional on the firm being sound, a higher $\xi$ leads to a higher posterior probability, $\hat{s}(\xi)$, that the firm is sound.

The intuition is that a higher amount of disclosure $\xi$ leads to a higher precision of the signal investors receive about the firm’s type, so the posterior belief that a firm is sound is higher for a sound firm when $\xi$ is higher. Holding fixed the value of the firm, this means that a greater amount of disclosure leads equity investors to demand a lower fraction of ownership $f$ in exchange for the funding that they provide (see (15)). As firm value declines as $\xi$ increases (due to the damaging effects of competitive entry), this creates a tradeoff that enables us to establish an optimal level of information disclosure with all-equity financing:

**Proposition 2:** Assuming only equity financing and that no firm wants to invest $\Delta R$, there exists a unique interior optimal level of disclosure $\xi^*$ that solves the problem in (14)–(17).

This proposition states that firms will choose a level of $\xi$ that trades off the costs and benefits of disclosure. On the one hand, greater disclosure leads to a higher posterior belief among investors that the firm is sound as $\partial \hat{s}/\partial \xi > 0$ (see Lemma 1). On the other hand, a higher $\xi$ also increases the probability of competitive entry, $\theta$, which reduces the value
of R&D to the firm. An interior optimum is achieved that balances the benefit of a lower
cost of financing against the cost due to a higher probability of competitive entry. This
interior optimum also implies that firms have no incentive to disclose information beyond $\xi^*$
for signaling purposes.

Let us now consider the firm’s incentive to raise the financing $\Delta R$. We assume that,
evaluated at $\bar{r}$, the prior belief about $r$, the payoff-enhancement R&D investment has negative
NPV, i.e.,

$$\bar{q} \delta [\bar{r} (\mu_J - \mu_H)] < \Delta R,$$

(18)

where

$$\mu_J = \int_{x_H}^{x_J} x dJ,$$

(19)

The next result establishes a pooling sequential equilibrium with respect to the R&D-
enhancing investment, $\Delta R$.

**Proposition 3:** There exists a sequential equilibrium where all firms avoid raising financing
$\Delta R$ for R&D payoff enhancement. If a firm chooses to raise this financing, investors believe
it is unsound with probability 1.

The intuition is that raising financing for a project that on average is negative NPV is most
attractive for the unsound firms. The market understands this and as a result will identify
a firm as unsound if it tries to raise financing for the R&D enhancement. In equilibrium, no
firm will therefore choose to undertake the R&D enhancement using market financing.\textsuperscript{21}

\textsuperscript{21}With reasonable additional parametric restrictions, we could establish that this equilibrium survives
refinements of sequential equilibrium. For example, suppose investors assume that firms with $r > \hat{r}$ will
invest in the payoff enhancement if financing were raised, and the rest will keep the cash idle. Then a
condition such as $[1 - \kappa] \left\{ \int_{\hat{r}}^{r} \bar{b} \bar{q} \delta [\mu_J - \mu_H] \, dr + \int_{r}^{\hat{r}} \Delta R \, dr \right\} < \Delta R$ will ensure that no financing will ever be
provided and the sequential equilibrium is unique.
4.3.2 Debt Financing

Now consider debt financing. Let $F$ be the face value of debt that must be repaid at $t = 3$. Before we get to the question of how much debt the firm will use, we prove some preliminary results.

**Lemma 2:** For any $F > 0$, the manager will engage in the maximum risk shifting at $t = 2$, choosing $\nu = \nu_{\text{max}}$.

The intuition is that, given the R&D payoff distribution, debt is risky in this model for any $F > 0$. With risky debt, the value of the call option represented by equity increases monotonically with risk.\(^{22}\) Our next result is about the impact of R&D expensing on the debt tax shield.

**Lemma 3:** The tax shield benefit of debt is smaller when R&D is treated as a tax-deductible expense than when it is not, and, holding $F$ fixed, the tax shield benefit of debt is smaller when the tax-deductible R&D expense is higher.

The reason for this in our model is that there is a set of states (with positive probability measure) in which the R&D payoff is smaller than the investment, i.e., R&D is risky. In these states, the debt tax shield has no value because no taxable income is left after R&D is expensed. Absent this expensing of R&D for tax purposes, the measure of the set of states in which debt provides a tax shield is larger.\(^\text{23}\)

It is convenient to now define some terms:

$$A_1 \equiv \int_{x_N - [1 - \kappa] \nu_m}^{x_H + [1 - \kappa] \nu_m} \left\{ (x - F) [1 - \tau] + [1 + \omega] R \tau \right\} dH, \quad (20)$$

\(^{22}\)We believe that the assumption the even debt financing in relatively small amounts will be risky in R&D-intensive firms is realistic. The unique features of R&D-intensive firms that we discussed earlier imply that issuing riskless debt is likely to be infeasible for these firms.

\(^{23}\)DeAngelo and Masulis (1980) were the first to note that non-debt tax shields can reduce the value of debt tax shields. The empirical evidence on this is mixed; see Eckbo (2011).
\[ A_2 \equiv \int_{F}^{F+[1+\omega]R} [x - F] \, dL + \int_{F+[1+\omega]R}^{xL+[1-\kappa]\nu_m} \left\{ [x - F - [1 + \omega]R] [1 - \tau] + [1 + \omega]R \right\} \, dL, \quad (21) \]

\[ A_3 \equiv \int_{-\kappa\nu_m}^{F} x \, dL + \int_{F}^{xL+[1-\kappa]\nu_m} F \, dL. \quad (22) \]

We can now turn to how much information will be optimally disclosed by the firm when there is debt. The maximization program of the initial owners of the firm can be written as:

\[ \max_{\xi \in [0, \xi_{\text{max}}]} \Omega_D(\xi) \quad (23) \]

\[ \Omega_D(\xi) \equiv [1 - \theta(\xi)] q \left\{ \delta A_1 + [1 - \delta] \left\{ \int_{-\kappa\nu_m}^{F} [0] \, dL + A_2 \right\} \right\} \\
\quad + [1 - \theta(\xi)] [1 - q] [0] + [1 - q] \theta(\xi)[0] \\
\quad + q \theta(\xi) \left\{ A_2 + \int_{-\kappa\nu_m}^{F} [0] \, dL \right\} \quad (24) \]

\[ \hat{s}(\xi) \left\{ [1 - \theta(\xi)] q [\delta F + [1 - \delta] [F[1 - L(F)] + A_3] + [1 - q] [1 - \theta(\xi)] R \right\} \\
\quad + \hat{s}(\xi) \left\{ q \theta(\xi) [F[1 - L(F)] + A_3] + [1 - q] \theta(\xi) R \right\} \\
\quad = [1 + \omega]R \quad (25) \]

This maximization program can be understood as follows. The wealth of the sound firm’s initial shareholders, \( \Omega_D(\xi) \), is the total value of the firm minus what the firm owes to the bondholders—this is given by (24), and maximizing it is the objective function in (23). What the firm owes to the bondholders is determined by the competitive equilibrium pricing constraint (25), and it includes the posterior belief \( \hat{s}(\xi) \) that the firm is sound. Now, \( \Omega_D(\xi) \) in (24) is the sum of two parts. The first part pertains to the value if there is no competitive entry, and the probability of success in this case is \( q \). The probability of no competitive entry is \( 1 - \theta(\xi) \). The second part pertains to the value if there is competitive entry, and
the probability of success in this case is $q$. The probability of competitive entry is $\theta (\xi)$. In writing expressions for $A_1$ and $A_2$ that are included in (24), it is recognized that the firm will engage in risk shifting. Moreover, R&D is treated as a tax-deductible expense before interest expense is deducted. Consider $A_1$ in (20). Over the entire support of $H$, $x > F$, so the firm’s initial owners are able to get the entire tax shield associated with expensing R&D, $[1 + \omega] R \tau$. Now consider $A_2$ in (21). The support of $L$ is such that debt is riskless only over a subset of that support. For $x \in [F, F + (1 + \omega) R]$, the firm pays no taxes due to the shield provided by the expensing of the R&D. For $x \in [F + [1 + \omega] R, x_L + [1 - \kappa] \nu_m]$, the firm’s initial owners are able to capture fully the tax shield associated with R&D expensing. In (22), $A_3$ represents the expected payoff to the bondholders when the R&D payoff distribution is $L$.\textsuperscript{24}

The next result states that, with debt financing in addition to equity financing, there is also a unique level of disclosure chosen by the firm:

**Proposition 4:** There exists a unique interior optimal level of disclosure $\xi^o \in [0, \xi_{\text{max}}]$ chosen by the firm’s initial owners. For $\mu_H$ large enough, $\xi^o > \xi^*$.\textsuperscript{25}

This proposition says that the firm discloses less information with equity than with debt. The reason is that, for a given increase in information disclosure, equity provides a larger “bang for the buck” than debt in terms of affecting the amount of capital that investors are willing to provide. This intuition is also consistent with papers that have argued that debt is less informationally sensitive than equity (e.g. Townsend (1979), Dang, Gorton, Holmstrom (2012), and Holmstrom (2015)). This allows the firm to optimally disclose less information with equity, and hence less firm value is lost due to information disclosure with equity than with debt.\textsuperscript{25}

\textsuperscript{24}The support of $L$ (with risk shifting) in $A_3$ includes negative values of $x$. The idea is that for $x < F$, the firm is bankrupt and belongs to the bondholders. Therefore, the bondholders must absorb the cost of liquidating the firm. The value from selling whatever the firm has is exceeded by the liquidation cost. This is an assumption of mathematical convenience.

\textsuperscript{25}This can be seen by considering equity to be a long call option on the value of assets of the firm, while debt is a combination of a short put option and a riskfree bond. The strike price in both cases is the
4.4 Analysis of Optimal Capital Structure

We now examine the firm’s choice of debt versus equity at \( t = 0 \). To do this, we need some preliminary notation.

First, let us write down the expected tax shield created by R&D expensing when the firm uses debt financing:

\[
\Gamma_R = [1 - \theta]q \Gamma_n + [1 - \theta] [1 - \theta'] \omega R \tau + [1 - q] \theta \omega R \tau + q \theta \Gamma_c. \tag{26}
\]

Similarly, let us write down the expected tax shield created by debt:

\[
\Gamma_F = \tau \left\{ [1 - \theta]q [\delta F + [1 - \delta] \varphi(F, [1 + \omega] R)] + q \theta \varphi(F, [1 + \omega] R) \right\}, \tag{27}
\]

where

\[
\varphi(F, [1 + \omega] R) \equiv \int_{[1+\omega]R}^{F} x \, dL + F[1 - L(F)]. \tag{28}
\]

In writing (28), we note that (24) implies that \( F > [\hat{s}(\xi)]^{-1} [1 + \omega] R \), so given the expensing of R&D, there is no debt tax shield until \( x > [1 + \omega] R \). We can now state our main result in this section:

**Proposition 5:** There exists \( \tau \) small enough and \( \kappa \nu_m \) large enough such that the competitive sequential equilibrium is one in which: (i) the firm raises \( R[1 + \omega] \) at \( t = 1 \) entirely from (outside) equity; (ii) the firm chooses a level of information disclosure of \( \xi^* \) (Proposition 2); (iii) investors price the equity using Bayes Rule to revise their prior beliefs that the firm is sound after observing \( \xi^* \) and the equity issue, and also assume that the probability of risk-shifting by the firm is zero; and (iv) the manager does not engage in risk shifting. No outstanding face value of debt. Note that changes in information disclosure will change the value of the firm. Since the gamma of a long call option is positive, the delta of the call (which can be interpreted as the sensitivity of the option with respect to information disclosure) will increase as firm value increases. Since the gamma of a short put option is negative, the delta of the short put will decrease as firm value increases. Thus, for sufficiently large firm values, the delta of the short put option will be less than the delta of the long call option. The disclosure conditions in Section 3.4, combined with a high upside value of R&D, ensure this.
capital is raised at \( t = 2 \). Any firm that raises capital different from \( R[1 + \omega] \) at \( t = 1 \), raises capital at \( t = 2 \), or chooses a different capital structure is viewed as unsound with probability one by investors.

This proposition describes a pooling sequential equilibrium. The unsound firm always mimics the capital structure of the sound firm because choosing any other capital structure would reveal its type almost surely. Consequently, a separating signaling equilibrium is precluded and investors price firms expecting sound and unsound firms to pool together.\(^{26}\)

The combination of a tax rate \( \tau \) low enough and a reduction in mean cash flow (with maximum risk shifting) \( \kappa \nu_m \) high enough represents a sufficiency condition for equity to dominate debt. When \( \kappa \nu_m \) is high, the expected loss in firm value due to risk shifting is also high. When \( \tau \) is low, so is the debt tax shield. The reduction in firm value due to risk shifting only occurs when the firm invests \( R \) in R&D at \( t = 2 \), i.e., when the outcome of the first-stage R&D is good; otherwise \( R \) sits idly by on the firm’s balance sheet. The probability of the firm investing \( R \) in R&D at \( t = 2 \) is \([1 - \theta]\bar{q} + \frac{q\theta}{2}\). Thus, the expected reduction in firm value due to risk shifting is \([1 - \tau]\{[1 - \theta]\bar{q} + \frac{q\theta}{2}\} \kappa \nu_m\), which is decreasing in \( \tau \) and increasing in \( \kappa \nu_m \). The debt tax shield \((\Gamma_F)\) is decreasing in \( \tau \). Hence, with a low \( \tau \) and high \( \kappa \nu_m \), the expected loss in firm value due to risk shifting exceeds \( \Gamma_F \). That is,

\[
[1 - \tau]\{[1 - \theta]\bar{q} + \frac{q\theta}{2}\} \kappa \nu_m > \Gamma_F. \tag{29}
\]

The inequality in (29) is more likely to be satisfied for R&D-intensive firms than for other firms. First, as mentioned earlier, risk shifting is much easier to do but more difficult to detect in R&D—researchers can always reorient the R&D towards riskier bets with higher payoffs conditional on success without making the research seem visibly different, due to their

\(^{26}\)For separation to occur, as in Ross (1977) for example, there should be a firm-type-dependent tradeoff between the benefit of choosing a given strategy (market value impact) and the future cost. The unsound firm’s valuation benefit from choosing the sound firm’s capital structure is the same as that for the sound firm, but it bears no future cost; there is a disclosure cost, but it is not type-dependent. Hence, it always pays for the unsound firm to “hide in the crowd”. 

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technical expertise which outsiders lack. Thus, \( \kappa \nu_m \), which is larger when there is more risk shifting, will be bigger in R&D-intensive firms. Note that the high upside of R&D also plays a role here—since \( \nu_m \) is increasing in \( x_H \), the high upside of R&D also contributes to the ease of risk shifting and the optimality of equity. Second, by Lemma 3, \( \Gamma_F \) is smaller in R&D-intensive firms due to the tax-deductibility of R&D expenses.

The reason why a low \( \tau \) and high \( \kappa \nu_m \) is only a sufficiency condition is that it ignores another advantage of equity over debt—it is that equity optimally requires less information disclosure (see Proposition 4).

4.5 Model Discussion and Extensions

In this section, we discuss a number of possible extensions of the model related to how R&D-intensive firms operate, and how these may affect our conclusions.

4.5.1 Tangible Assets-in-place or Cash Reserves

In our analysis, we assume that the firm has no significant assets in place at the beginning \( t = 0 \). If the firm has tangible assets in place at \( t = 0 \) that can be used as collateral, then debt may show up in the optimal capital structure for two reasons.

First, collateral attenuates moral hazard.\(^{27}\) It is easy to verify in our model that if the firm could post sufficient collateral, risk-shifting could be eliminated, as long as the amount of debt did not exceed the collateral posted. The amount of debt used in this case would be increasing in the collateral available.

Second, as long as collateral can be protected from risk shifting, it can be a direct source of repayment for debt.

This extension in the analysis may provide a differentiation between R&D-intensive firms, for example between pharmaceutical ("pharma") and biotechnology ("biotech") firms, in terms of their capital structures. Pharma firms tend to have greater amounts of assets.

\(^{27}\)See, for example, Boot, Thakor and Udell (1991).
in place than biotech firms, as a result of existing product lines and drug manufacturing operations. The theory therefore predicts that pharma firms will optimally tend to have more debt in their capital structure than biotech firms, a fact that holds empirically (see Thakor et al. (2016)).

4.5.2 Portfolio of Projects

In our model, the R&D project is a single project. In practice, firms may have portfolios of projects. A portfolio of projects may provide a number of benefits. One benefit is risk diversification for the firm—this has also been emphasized in the context of a drug “mega-fund” by Fagnan et al. (2013) and Fernandez et al. (2012). A second benefit may be a lower per-project cost of disclosing proprietary information to product-market competitors. This is because, since the idiosyncratic nature of each project is diversified away through the portfolio, the technical aspects of each individual R&D project are also obscured to competitors, thus revealing less information about any one project.

4.5.3 Debt Signaling

The results in the previous sections establish a financing pecking order, but there is also a pooling equilibrium where all firms do not invest in the (socially) valuable R&D-enhancement, \( \Delta R \). A natural question that arises is whether it is possible to avoid this pooling outcome through signaling via debt as in Ross (1977)?

In our model, however, debt signaling does not work to eliminate the pooling with respect to the R&D-enhancing investment. For debt to be a signal as in Ross (1977), the single-crossing property must be satisfied and the marginal cost of signaling should be lower for the firms with higher values of \( r \). However, the marginal cost of using debt in our model to separate sound firms with different values of \( r \) is the same for all values of \( r \) since it stems from risk-shifting.\(^{28}\) Thus, the single-crossing property does not hold. In the subsequent

\(^{28}\)Note that if debt signaling were feasible, the unsound firm would always wish to mimic the sound firm with the highest \( r \) in order to raise the maximum financing at \( t = 0 \).
analysis, we explore a possible resolution to the pooling outcome of the R&D-enhancement.

4.5.4 Convertible Bonds

In the previous analysis, we have just considered straight equity and debt as choices of securities that the firm may issue. However, in practice, R&D-intensive firms like biopharma firms also use convertible debt. It is therefore interesting to consider whether convertible debt is an optimal method of funding when compared to straight debt or equity within the context of our model.

Green (1984) showed that appropriately-designed convertible debt can mitigate risk-shifting moral hazard, emphasizing that this will only happen if the option to convert their debt to equity is exercised by the convertible holders only in a subset of the “upper-tail” cash flow states. In our model, these conditions are satisfied. In our model, these conditions are satisfied. Convertible holders will convert only when $x > F$. The set of states represented by $x \leq F$ can be divided into two subsets: $S_1 \equiv \{x \mid x \leq [1 + \omega]R\}$ and $S_2 \equiv \{x \mid x \in ([1 + \omega]R, F]\}$. In $S_1$, convertible holders will not convert, but debt provides no tax shield benefit; all of the tax benefit comes from R&D expensing. In $S_2$, there is a tax benefit of debt, but its expected value is $\tau \{[1 - \theta]q[1 - \delta] + q\theta\} \int_{[1 + \omega]R}^{F} x dL$ (see (26)-(28)). The reason is that in states in which the firm does not invest in second-stage R&D, its payoff is only $R$, so all of the tax benefit comes from R&D expensing, and none from debt. So while convertible debt may eliminate risk shifting, its tax shield advantage will be small if the R&D financing need is large (so that $x_L - [1 + \omega]R$ is small) and $\delta$ is relatively high.

Convertible debt will, however, have a disadvantage. Given that the optimal level of information disclosure $\xi$ is lower for equity than for debt, the conversion feature of convertible debt also implies that the optimal level of information disclosure for convertible debt will be between that of debt and equity. Since overall firm value is decreasing in the amount of information disclosure, this in turn implies that, when the incremental debt tax shield is small (under the conditions identified above), convertible debt will be preferrable to straight
debt, but less attractive than equity.

It should also be noted that convertible debt, like debt and equity, will not solve the problem of non-investment in the R&D-enhancement \( \Delta R \). Indeed, to the extent that it is not possible to contract on (or reveal) the probability of success \( r \) of the R&D-enhancement, then any other alternative security will also not be able to solve this underinvestment problem. We address this in Section 5.

5 An Exploration of a New Intermediary-Assisted Financing Mechanism Design

The previous analysis assumed that firms would rely on standard debt and equity contracts to finance R&D, and proceeded to derive a pecking order in which, under some conditions, equity ends up at the top. However, there is still a friction that is not resolved by market financing—no firm will choose to invest \( \Delta R \) to enhance the R&D payoff distribution from \( H \) to \( J \), even though such an investment would be valuable for some firms.\(^{29}\) This raises the question of whether there is a mechanism beyond straight market financing that may improve outcomes, and allow this R&D enhancement to be undertaken.

To explore this, we introduce an intermediary that can, unlike the pure market financing case, make binding precommitments, get firms to do the same, and is not constrained to debt and equity. We thus view this mechanism as an intermediary-assisted approach that is used in conjunction with equity financing raised from the market.

5.1 Mechanism Design Framework

We approach this in a standard mechanism-design framework (e.g. see Myerson (1979)). The intermediary acts as an arbitrator that asks each firm to directly and truthfully report

\(^{29}\)One could also interpret this enhancement as something that has a positive social externality that is not internalized in the NPV calculation for the firms. For example, this could be some sort of drug that may have wider applications given further testing.
The left figure depicts the payoffs to the insider, while the right figure depicts the payoffs to investors. In the region where $x < x_L$, insiders are long in the put and investors are short in the put. In the region where $x \in [x_L, \zeta(r)]$, the insiders are short in the put and the investors are long in the put. In the region where $x > \zeta(r)$, the put is out of the money and the payoff is zero.

Note that when investors exercise their put option, the firm does not generate sufficient...
cash flow to satisfy their claim. Thus, the insiders of the firm must liquidate their personal assets \( A \) at a cost. This requires a precommitment to the intermediary’s scheme, something that is not available with market financing. Absent such precommitment, the firm’s insiders would simply invoke the firm’s limited liability and not sell personal assets at a cost to settle any payment on the put option. The scheme would then unravel.

Since the firm’s report \( r \) is made at \( t = 0 \) (and we assume it becomes common knowledge right away), and it is always truthful in equilibrium in an incentive compatible mechanism, the firm can choose its disclosure after having reported its \( r \). In other words, the firm can choose \( \xi \) as if there was perfect (symmetric) information about \( r \).

Let \( \pi(r) \) be the probability that the intermediary will allow the firm to participate in the scheme. If the firm is not allowed to participate, it must seek market financing, as in the previous section. Let \( \alpha(r) \) be the social value the arbitrator attaches to the expected payoff due to the incremental investment \( \Delta R \). Thus, the intermediary’s mechanism \( \Psi \) can be described as:

\[
\Psi : [r_a, r_b] \rightarrow \mathbb{R}_+ \times [0, 1].
\]

That is, the firm reports \( r \in [r_a, r_b] \) to the intermediary, it is asked to create a put option with a strike price of \( \zeta(r) \in \mathbb{R}_+ \) (the positive real line), and is allowed to participate in the scheme with a probability of \( \pi(r) \in [0, 1] \). Let \( P_0(\tilde{r} | r) \) be the value of the put option when the firm reports \( \tilde{r} \) and its true parameter value is \( r \), with \( P_0(\tilde{r} | r) \equiv P_0(r) \). The firm then chooses its disclosure \( \xi \) and investors then determine the fractional ownership \( f \) that the firm must sell in order to raise \( [1 + \omega + \Delta]R \) at \( t = 0 \). We rely on the result of the previous section that equity dominates debt in the external financing pecking order, i.e., (29) is assumed to hold. In what follows, we set the tax rate \( \tau = 0 \) to reduce notational clutter, since it plays no further role in the analysis.

Let \( U(\tilde{r} | r) \) be the expected utility or net payoff of a firm whose true parameter is \( r \) but which reports \( \tilde{r} \). Before stating the intermediary’s problem, we describe the first-best solution when each firm’s \( r \) is common knowledge. Because of the deadweight loss associated
with insiders liquidating their own assets to cover the cost of the put option, in the first-best
case no firm writes a put option. Each firm’s insiders maximize:

\[ [1 - f] \Omega (r, \xi) , \]  

subject to\(^{30}\)

\[ \Omega (r, \xi) = B_1(\xi) \left[ G + \delta r \left[ \mu_J - \mu_H \right] + B_2 \mu_L + B_3 R \right] , \]  

\[ \hat{s}(\xi)f\Omega (r, \xi) = [1 + \omega + \triangle] R. \]  

In the above, note that

\[ B_1 \equiv \bar{q} [1 - \theta] , \]  

\[ B_2 \equiv \bar{q} \theta , \]  

\[ B_3 \equiv [1 - \theta] [1 - \bar{q}] + \theta [1 - \bar{q}] . \]  

5.2 Analysis of the Mechanism

We start by characterizing the first-best level of information disclosure, \( \xi \).

**Lemma 4:** There is a unique optimal level of disclosure in the first-best case that is strictly
decreasing in \( r \).

Our next result shows that the intermediary cannot implement the first-best solution
when there is asymmetric information about \( r \).

**Lemma 5:** The first-best solution is not incentive compatible.

\(^{30}\)To obtain (32) below, note that

\[ \Omega(r, \xi) = B_1 \left[ \delta \left\{ r \int_{x_H}^{x_J} x dJ + [1 - r] \int_{x_L}^{x_H} x dH \right\} + [1 - \delta] \int_{0}^{x_L} x dL \right] + B_2 \int_{0}^{x_L} x dL + B_3 R \]

and substitute \( \mu_J = \int_{x_H}^{x_J} x dJ, \mu_H = \int_{x_L}^{x_H} x dH, \mu_L = \int_{0}^{x_L} x dL, \) and \( \bar{G} \equiv \delta \mu_H + [1 - \delta] \mu_L. \)
The reason why the first-best solution is not incentive compatible is that a firm with a higher $r$ is more valuable holding fixed its disclosure level $\xi$, and moreover, it also discloses less in the first best, further enhancing its value. Thus, there is a “double advantage” for the firm to masquerade as a firm with a higher $r$—it can “get away” with disclosing less and raising the needed financing by giving up a lower ownership share.

Under asymmetric information, the intermediary’s problem can be expressed as that of designing functions $\pi \in [0, 1]$ and $\zeta$ to solve:

$$\max \int_{r_a}^{r_b} \pi(r) \left\{ \Omega(\xi, r) + \alpha(r) - P_0(r)l^{-1} - \Omega(\xi^*) \right\} z(r) \, dr,$$

subject to

$$\Omega(\tilde{\xi}, \tilde{\tau} \mid r) = B_1(\tilde{\xi}) \left[ \tilde{G} + \delta r [\mu_J - \mu_H] + B_2(\tilde{\xi}) \mu_L + B_3(\tilde{\xi}) R \right],$$

$$U(\tilde{\tau} \mid r) = \pi(\tilde{\tau}) \left\{ [1 - \tilde{f}] \Omega(\tilde{\xi}, \tilde{\tau} \mid r) - P_0(\tilde{\tau} \mid r) l^{-1} \right\},$$

$$U(r) \geq U(\tilde{\tau} \mid r) \ \forall r, \tilde{\tau} \in [r_a, r_b],$$

where $P_0$ is the value of the put option at $t = 0$, and with $\tilde{f}$ being determined by:

$$\tilde{s}(\tilde{\xi}) \left[ \tilde{f} \Omega(\tilde{\xi}, r) + P_0(\tilde{\tau} \mid r) \right] = [1 + \omega + \triangle] R,$$

and $\Omega(\xi, r \mid r) \equiv \Omega(\xi, r), U(r \mid r) \equiv U(r)$. Note that $\Omega(\xi^*)$ is the total value of each firm that raises market financing using optimal disclosure $\xi^*$. That is, the intermediary maximizes the incremental surplus from mechanism design relative to the market-financing outcome.

To understand the intermediary’s mechanism design problem, note that in (37) the intermediary maximizes the expectation (taken with respect to $r$ that the intermediary does not know) of the total value of the firm $\Omega$, plus its social value $\alpha$, minus the deadweight cost of the put option $P_0 l^{-1}$, minus the value $\Omega(\xi^*)$ attainable with market financing. (38)
is simply the firm value when the firm’s true parameter is \( r \) and it reports \( \tilde{r} \) (which then implies a disclosure level of \( \tilde{\xi} \) associated with that \( \tilde{r} \)). In (39) we have the expected utility of the firm’s insiders. (40) is the global incentive compatibility (IC) constraint, and (41) is the competitive capital market pricing constraint.

Henceforth, for simplicity, we shall assume that \( L, H, \) and \( J \) are all uniform. Let us now write down the value of the put option (assuming that \( \zeta(r) > x_L \), something we will verify later as being associated with the optimal solution):

\[
P_0 = \left\{ B_1 \left[ \delta [1 - r] \int_{x_L}^{\zeta} [\zeta - x] dH - [1 - \delta] \int_{x_0}^{x_L} [\zeta - x] dL \right] \right\}
- \left\{ B_2 \int_0^{x_L} [\zeta - x] dL + B_3 [\zeta - R] \right\}.
\] (42)

Now,

\[
\int_{x_L}^{\zeta} [\zeta - x] dH = \int_{x_L}^{\zeta} \frac{\zeta - x}{x_H - x_L} dx = \frac{(\zeta - x_L)^2}{2 [x_H - x_L]}.
\] (43)

\[
\int_0^{x_L} [\zeta - x] dL = \int_0^{x_L} \frac{\zeta - x}{x_L} dx = \zeta - \mu_L.
\] (44)

Substituting (43) and (44) in (42) gives:

\[
P_0 = \frac{B_1 \delta [1 - r] [\zeta - x_L]^2}{2 [x_H - x_L]} - B_1 [1 - \delta] [\zeta - \mu_L] - B_2 [\zeta - \mu_L] - B_3 [\zeta - R]
\] (45)

We shall assume henceforth that the function \( \phi(r) \equiv \frac{1 - Z(r)}{z(r)} \) satisfies:

\[
\inf_r \left\{ \frac{1 - r}{\phi(\xi)} \right\} > \frac{1 - l}{l}
\] (46)
and

$$-\frac{\partial \phi(r)}{\partial r} < \frac{l}{1-l}. \quad (47)$$

These conditions simply assume that $l$ is large enough (the personal asset liquidation cost is not too high) and will be satisfied for many distributions (e.g. it holds for $l \in (0.5, 1)$ if $z$ is uniform).

We now present a result that allows us to express the global IC constraint (40) as a local constraint.

Lemma 6: The global IC constraint (40) is equivalent to:

1. $U'(r) = \pi(r) \left[ B_1 \delta [\mu_J - \mu_H] + \frac{[l^{-1} - 1] \delta B_1 [\zeta - \bar{x}]^2}{2(x_H - x_L)} \right]$ for almost every $r \in [r_a, r_b]$ and $U'(r) > 0$ wherever it exists.

2. $U'' \geq 0$ for almost every $r \in [r_a, r_b]$

3. (40) holds where $U'$ does not exist.

The main contribution of this lemma is that it allows us to replace the infinite number of constraints embedded in the global IC constraint (40) with conditions involving the first and second derivatives of $U$. This facilitates the subsequent analysis.

Lemma 7: The regulator’s mechanism design problem in (37)–(41) is equivalent to designing the functions $\pi$ and $\zeta$ to maximize:

\[
\int_{r_a}^{r_b} \pi(r) \left\{ \phi(r) \left[ C_1 C_2 + C_1 \left[ l^{-1} - 1 \right] \left\{ \frac{[\zeta - \bar{x}_L]^2}{2(x_H - x_L)} \right\} \right] \right\} z(r) \, dr \\
+ \int_{r_a}^{r_b} \pi(r) \left\{ \frac{[1 + \omega + \Delta] R}{s} + \alpha(r) - \Omega (\xi^*) - P_0(r) \right\} z(r) \, dr \quad (48)
\]

where $C_1 \equiv B_1 \delta$ and $C_2 \equiv \mu_J - \mu_H$. 

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Given the allocation \(\{\pi(r), \zeta(r)\}\) in response to its reported \(r\), the firm chooses its disclosure \(\xi\) to maximize \(U(r)\), conditional on being allowed to participate, i.e. it solves

\[
\max_{\xi} \left[ 1 - \tilde{f} \right] \Omega(\xi | r) - P_0(r)l^{-1},
\]

(49)

which upon substituting from (41) becomes:

\[
\max_{\xi} \left\{ \Omega(\xi | r) - \frac{[1 + \omega + \triangle]}{\hat{s}} R - P_0(r) \left[ l^{-1} - 1 \right] \right\}.
\]

(50)

The intermediary will take each firm’s (anticipated) post-reporting \(\xi^*(r)\) and solve for the \textit{ex ante} optimal mechanism accordingly. The following result characterizes the optimal mechanism.

**Proposition 6:** The optimal mechanism involves:

1. A put option strike price of

\[
\zeta(r) = x_L + \frac{[x_H - x_L] \left\{ [B_1 \left[ 1 - \delta \right] + B_2 + B_3] \right\}}{B_1 \delta \left\{ [1 - r] - \phi(r) \left[l^{-1} - 1\right] \right\}},
\]

(51)

which is greater than \(x_L\) and increasing in \(r\), and a digital option that makes investors long in the put and insiders short in the put when \(x \in [x_L, x_H]\), and investors short in the put and insiders long in the put when \(x < x_L\).

2.

\[
\pi(r) = \begin{cases} 
1 & \text{if } r \geq r^* \in [r_a, r_b] \\
0 & \text{otherwise}
\end{cases}
\]

(52)

The intuition for this mechanism is as follows. Firms with lower values of \(r\) want to masquerade themselves as firms with higher values of \(r\). The optimal mechanism copes with this by making the put option strike price an increasing function of \(r\). That is, for
$x \in [x_L, x_H]$, the firm’s insiders (who are short in the put) have a higher liability under the put option they have sold to investors if they report a higher $r$. This mechanism is incentive compatible because it is less costly for the insiders of a firm with a higher true $r$ to be short in such an option.

In addition to this, the digital option makes insiders long in the put and investors short in the put when $x < x_L$. Because the probability of $x < x_L$ does not depend on $r$, the probability of this digital option being turned on is the same for all firms regardless of $r$. So it reduces the probability of personal asset liquidation equally for all insiders. However, since the option strike price is higher for firms that report higher values of $r$, the reduction in the expected cost of personal asset liquidation is greater for the firms with higher values of $r$, a benefit to these firms that offsets their higher liability under the put option that is turned on when $x \in [x_L, x_H]$. The reduction in the expected cost of personal asset liquidation increases the expected utility of insiders. The probability of being allowed to participate in this mechanism is 1 as long as the mechanism enables the intermediary to achieve a higher value of the objective function than with direct market financing. Otherwise, the firm is asked to go for the direct market financing option.\(^\text{31}\)

This mechanism helps to overcome two major impediments to financing risky R&D—convincing investors that there is enough upside in the success of the R&D to make it attractive for them to invest, and convincing the entrepreneur (e.g. the manager of a biotech firm) that there is sufficient downside protection against the failure of the R&D that it is worthwhile.

\(^{31}\)In this analysis we have taken the reservation utilities of the firms for participating in the mechanism as exogenous. This is in contrast to the Phillipon and Skreta (2012) and Tirole (2012) models in which reservation utilities are endogenous in the sense that they depend on the mechanism itself. In these models, the mechanism is meant to deal with the market freeze caused by the lowest quality firms, and in Tirole (2012), for example, the government buys up the weakest assets. While we also allow the market to be open and hence market financing is an alternative to the mechanism for each firm, in our model the mechanism is designed in such a way that it is optimally preferred to market financing by the highest quality firms, and it is only the firms at the lowest end of the quality spectrum (with respect to the R&D payoff enhancement) that go to the market because the mechanism cannot do incrementally better than market financing for these firms. Moreover, the mechanism ensures that any firm that uses the mechanism gets an expected utility that is higher than that with market financing. So, no matter what the design of the mechanism, the firms that are not part of it cannot raise market financing for the R&D project enhancement, and thus reservation utilities for participating in the mechanism are unaffected by the market option.
to undertake it.

5.3 Interpretation and Intuition

The core intuition behind why this mechanism works can be thought of as follows. Roughly speaking, there are three ranges of R&D cash flows in the model: very low, intermediate, and very high. The probability of achieving the very high cash flows is private information for the firm’s insiders, and varies in the cross-section of firms. Firms with low probabilities have an obvious incentive to misrepresent themselves as having high probabilities. By asking firms that report higher probabilities of achieving very high cash flows to provide investors greater insurance against intermediate cash flows, the optimal mechanism design deters such misrepresentation. Of course, since R&D outcomes are uncertain, providing such insurance is costly for the firm’s insiders. To offset this cost, investors in turn insure the firm’s insiders against very low cash flows. Thus, potential underinvestment in R&D is discouraged from both the standpoint of insiders underinvesting due to a high possibility of failure, and investors underinvesting due to suspicion of too low a probability of very high payoffs.

More formally, our mechanism can functionally be interpreted as an exchange of put options (insurance contracts) between investors and insiders. One contract is offered by insiders to investors, and insures investors against the possibility that the firm misrepresents its chances of the R&D-enhancement succeeding. Since the strike price is increasing in $r$, this cost makes it progressively more onerous for a firm to misrepresent itself as a high-$r$ firm, thus inducing it to truthfully report its value of $r$. Put another way, the payoff range of this insurance contract only occurs when $x$ achieves a high cash flow distribution (with cdf $H$). Firms with a high likelihood of R&D-enhancement success will not expect to fall into this region (since they will have cash flow $x$ distributed according to cdf $J$). However, firms with a low likelihood of R&D-enhancement success have a high chance of falling into this region. Of these firms, the ones that truthfully report their (low) value of $r$ will not be invited
to participate in the mechanism.\textsuperscript{32} The ones that choose to participate by misrepresenting their value of \( r \) as being higher will be required to provide an insurance contract to investors. This insurance contract therefore helps to incentivize investors to provide financing for the R&D-enhancing investment, by protecting them against the risk of financing unsound firms as well as sound firms with a relatively low likelihood of achieving very high payoffs.

The other contract is offered by investors to insiders, and insures insiders against a poor cash-flow outcome in the final stage of R&D. For insiders, this contract offers a more flat net payoff that offsets disappointing (commercialized) R&D results in the final stage. Investors are willing to provide this “downside” insurance in order to induce insiders to undertake the R&D-enhancement, which makes their initial investment pay off even more. Investors’ willingness to provide this insurance therefore also increases in the probability \( r \) because this makes the upside more likely, and thus investors are willing to pay more to enable it.

The interpretation of our mechanism in terms of insurance contracts and guarantees corresponds in part to the recent use of similar financial contracts in the biopharma sector, but also offers insights into how these contracts could be augmented. For example, a financing innovation for investors is called an “FDA swap”, which provides firms insurance against the failure of a drug to get FDA approval (see Philipson (2015) for details).\textsuperscript{33} Another innovation is “Phase 2 development insurance”, which is offered to small biotech firms in exchange for an equity stake in the firm, and pays out in the event that a drug candidate fails Phase 2 R&D trials. These contracts resemble the put sold by investors to insiders. Our mechanism shows the value of such contracts, but also indicates that an appropriate exchange of insurance contracts between firms and investors can potentially overcome impediments to financing related to adverse selection, and lead to an improvement in R&D outcomes.

Overall, our mechanism highlights the value of credible precommitment to a coordinating

\textsuperscript{32}It should be noted that the design of the mechanism does not change the behavior of the firms that do not participate in the mechanism and only go to the market to raise financing. In other words, for the firms not investing in the R&D payoff enhancement (and thus not participating in the mechanism), the investment and capital structure analysis of Section 4 of the paper still holds.

\textsuperscript{33}A similar proposed innovation is “FDA hedges”, which involves binary options struck on FDA drugs in development. See Jørring et. al. (2016).
mechanism between firm insiders and investors, which can increase R&D investments. As mentioned earlier, the intermediary in our mechanism could be any entity which plays an intermediation role, bringing firms and investors together, eliciting information about the true prospects of some R&D investments in a way that the market cannot, and enforcing the ex ante commitments made to the mechanism. This role could practically be played, for example, by the government, or a third-party entity like an exchange or consortium of firms.\footnote{For example, financial exchanges such as the Chicago Mercantile Exchange, which serve as an intermediary to bring two counterparties together in a financial transaction, can be seen as playing a similar role.}

To the extent that existing contracts do not reflect the kind of bilateral exchange of insurance that our analysis says is optimal, the implication is that the empirically-documented underinvestment in R&D (e.g. Brown and Lerner (2010)) may be attenuated by augmenting the contract space with intermediary assistance along the lines indicated here.

6 Conclusion

In this paper, we develop a model of optimal investment and capital structure for R&D-intensive firms. We examine a setting with adverse selection, information disclosure, and moral hazard in which firms need to raise large amounts of capital to invest in an R&D project with long-term staged investments and low probabilities of success—features that typify many R&D-intensive firms. Adverse selection in this setting is partially endogenized, as firms can reduce it by disclosing information about their projects; however, this also generates a cost to firms, as valuable proprietary information is revealed to competitors.

We use this model to explain various stylized facts about firms in this environment. First, these firms have lower leverage ratios than other firms, and they rely more on internal funds and equity. Second, they have large amounts of cash. Third, there is a “funding gap” or underinvestment in R&D. In explaining these stylized facts, we establish the optimal pecking order of securities with market financing: equity dominates debt under some conditions, and firms also seek to hold excess cash for future investments rather than tap the external finance
market. However, there are still socially valuable project enhancements that firms do not undertake in equilibrium with market financing.

We then ask whether there is a non-market solution to the underinvestment problem. For this analysis, we take a mechanism design approach, and show that an intermediary may design a mechanism that resolves this friction and induces firms to undertake the additional investment in R&D. Specifically, a mechanism consisting of insiders buying and selling put options, in combination with equity, allows the firm to commit to making the socially beneficial R&D enhancement. The introduction of this mechanism improves welfare relative to market financing because it eliminates underinvestment. The analysis also more generally highlights the potential benefit of an intermediation-assisted coordinating mechanism between investors and firms, which can induce a precommitment in R&D financing.

The mechanism developed in this paper provides a broader theoretical foundation for combining market financing and intermediation-assisted financing, as in the recently proposed alternative methods of financing biomedical innovation via “megafunds” (Fernandez, Stein, and Lo, 2012; Fagnan et al., 2013) which uses private-sector means to facilitate socially valuable R&D.
Appendix

Proof of Proposition 1: Suppose this were not true. Then suppose the firm receives the signal at \( t = 2 \) that its first-stage R&D produced good results. If it now raises the investment \( R \) that it needs by accessing external financing, in doing so, it will choose some level of information disclosure \( \xi \geq \xi_{\text{min}} \). Assuming that the firm is sound, this will make it publicly known that the first-stage R&D was successful. Of course, the probability that the firm is unsound is non-zero, but given our earlier specification of competitive entry, the disclosure that the first-stage R&D was successful will lead to competitive entry with probability one. Competitive entry at \( t = 2 \) means that the firm’s expected project value will drop to

\[
\int_{0}^{x_L} x \, dL - \int_{R}^{x_L} (x - R) \tau \, dL = R + \varepsilon, \quad (A.1)
\]

and thus the NPV of the investment to an entrant is \( \varepsilon \). Since \( \varepsilon \) is arbitrarily small, we have that \( \varepsilon < \omega R \), so the firm will not make the initial investment at \( t = 0 \) in the first place. This means that if the firm does invest in R&D at all, it will raise the entire financing needed for the two stages, \( [1 + \omega] R \), at \( t = 0 \), so as to avoid revealing the outcome of the first-stage R&D publicly at \( t = 2 \).

Proof of Lemma 1: Let us now solve for \( \hat{s}(\xi) \). Note that:

\[
\hat{s}(\xi) = \Pr(\text{firm sound} \mid \phi = \text{sound})
= \frac{\Pr(\phi = \text{sound} \mid \text{firm sound}) \Pr(\text{firm sound})}{\Pr(\phi = \text{sound})}
= \frac{p(\xi) s}{p(\xi) s + [1 - p(\xi)][1 - s]}, \quad (A.2)
\]

\[
\frac{\partial \hat{s}}{\partial \xi} = \frac{p'(\xi) s [1 - s]}{[p(\xi) s + [1 - p(\xi)][1 - s]]^2} > 0. \quad (A.3)
\]

Note further that:

\[
\frac{\partial^2 \hat{s}}{\partial \xi^2} = \frac{D \{p'' s [1 - s] - 2p' s [1 - s] [p' s - p'[1 - s]]\}}{D^2}, \quad (A.4)
\]

50
where
\[ D \equiv [p(\xi) s + [1 - p(\xi)] [1 - s]]^2. \] (A.5)

Note that \( \partial^2 \hat{s}/\partial \xi^2 < 0 \) since \( p'' < 0, p' > 0, \) and \( s > 0.5. \)

**Proof of Proposition 2:** Combining (14) and (15), we can write the objective function as:
\[ \Omega (\xi) - [1 + \omega] R [\hat{s}(\xi)]^{-1}. \] (A.6)

The first-order condition is:
\[ \left[ \frac{\partial \Omega}{\partial \xi} \right] + [1 + \omega] R [\hat{s}(\xi)]^{-2} \left[ \frac{\partial \hat{s}}{\partial \xi} \right] = 0. \] (A.7)

The second-order condition is:
\[ \left[ \frac{\partial^2 \Omega}{\partial \xi^2} \right] - 2 [1 + \omega] R [\hat{s}(\xi)]^{-3} \left[ \frac{\partial \hat{s}}{\partial \xi} \right]^2 + [1 + \omega] R [\hat{s}(\xi)]^{-2} \left[ \frac{\partial^2 \hat{s}}{\partial \xi^2} \right] < 0. \] (A.8)

Now,
\[
\frac{\partial \Omega}{\partial \xi} = -\theta' (\xi) \left\{ \bar{q} \left[ G + \Gamma_n \right] + [1 - \bar{q}] \left[ R[1 - \tau] + \omega R \tau \right] \right\} \\
+ \theta' (\xi) \left\{ \bar{q} \left[ \mu_L [1 - \tau] + \Gamma_c \right] + [1 - \bar{q}] \left[ R[1 - \tau] + \omega R \tau \right] \right\} \\
= -\theta' (\xi) \left\{ \bar{q} \left[ G + \Gamma_n \right] + [1 - \bar{q}] \left[ R[1 - \tau] + \omega R \tau \right] \right\} \\
+ \theta' (\xi) \left\{ R[1 - \tau] + \omega R \tau \right\} \quad \text{(by (2))} \\
< 0 \quad \text{since} \quad G + \Gamma_n > R[1 - \tau] + \omega R \tau, \] (A.9)

since \( \theta' > 0, \) and the quantity inside the braces is positive. Moreover, defining \( A_4 \equiv \bar{q} \left[ G + \Gamma_n \right] + [1 - \bar{q}] \left[ R[1 - \tau] + \omega R \tau \right] - \bar{q} \left[ \mu_L [1 - \tau] + \Gamma_c \right] - [1 - \bar{q}] \left[ R[1 - \tau] + \omega R \tau \right] > 0, \) we have:
\[ \frac{\partial^2 \Omega}{\partial \xi^2} = \theta'' (\xi) A_4 < 0, \] (A.10)
since \( \theta'' > 0 \). Since \( \partial^2 s/\partial \xi^2 < 0 \), it is clear now that (A.8) holds. The fact that \( \xi^* \) is in the interior follows from the Inada-type conditions. ■

**Proof of Proposition 3:** First, it is straightforward to see this is a Nash equilibrium—holding fixed the strategy of investors to price the firm that raised financing as if it is unsound, it is an optimal strategy for each sound firm to not raise financing. In equilibrium, then, non firm raises financing. Given this strategy, the optimal strategy for investors is to price the firm as if it is unsound. Given the out-of-equilibrium belief stipulated in the proposition, it is clear that the pooling Nash equilibrium is sequential, since each firm’s equilibrium expected utility is higher than if it deviates from the equilibrium strategy. ■

**Proof of Lemma 2:** Using (20) and replacing \( \nu_m \) by \( \nu \), we see that

\[
\frac{\partial A_1}{\partial \nu} = \{[x_H + (1 - \kappa)\nu - F][1 - \tau] + [1 + \omega]R\tau\}[1 - \kappa] \\
+ \{[x_L - (1 - \kappa)\nu - F][1 - \tau] + [1 + \omega]R\tau\}[1 - \kappa] \\
> 0.
\]

(A.11)

Similarly, using (21) and replacing \( \nu_m \) by \( \nu \), we see that

\[
\frac{\partial A_2}{\partial \nu} = \{[x_L + (1 - \kappa)\nu - F - [1 + \omega]R][1 - \tau] + [1 + \omega]R\}[1 - \kappa] \\
> 0.
\]

(A.12)

From (24), we see that \( \partial \Omega_D(\xi) \) is strictly increasing in \( A_1 \) and \( A_2 \) \( \forall F \). Thus, \( \Omega_D(\xi) \) is strictly increasing in \( \nu \) for any \( F \). ■

**Proof of Lemma 3:** From (28) we see that, holding \( F \) fixed,

\[
\frac{\partial \varphi(F, [1 + \omega]R)}{\partial R} < 0,
\]

(A.13)
which means that $\partial \Gamma_F / \partial R < 0$. Moreover, if R&D were not tax-deductible, then

$$\varphi(F, [1 + \omega] R) \equiv \varphi(F) = \int_{0}^{F} x \, dL + F [1 - L(F)]$$

$$> \int_{[1+\omega]R}^{F} x \, dL + F [1 - L(F)],$$

(A.14)

which means $\Gamma_F$ is bigger if R&D is not a tax-deductible expense. □

Proof of Proposition 4: We can rewrite (24) as:

$$\Omega_D(\xi) = \delta [1 - \theta(\xi)] \bar{q} \left\{ [\mu_H (1 - \tau) + F\tau] - F + [1 + \omega] R\tau \right\}$$

$$+ \left\{ [1 - \theta(\xi)][1 - \delta] \bar{q} + \bar{q} \theta(\xi) \right\} \left\{ -F [1 - L(F)] + \int_{0}^{F} x \, dL - \int_{-\gamma}^{F} x \, dL \right\}$$

$$+ \int_{F}^{F+1+\omega]R} x \, dL + \int_{F+[1+\omega]R}^{\bar{x}_{L}+[1-\gamma]\mu_{m}} x[1 - \tau] \, dL + F\tau [1 - L(F + [1 + \omega] R)]$$

$$+ \tau [1 + \omega] R [1 - L(F + [1 + \omega] R)] \right\}$$

$$= V_T - [1 - \theta(\xi)] \bar{q} \left\{ \delta F + [1 - \delta] [F [1 - L(F)] + A_3] \right\}$$

$$- \bar{q} \theta(\xi) \left\{ F [1 - L(F)] + A_3 \right\} - [1 - \bar{q}] [1 - \theta(\xi)] R + \left[1 - \bar{q}\right] \theta(\xi) R,$$

(A.15)

where the total value of the firm is:

$$V_T \equiv \delta [1 - \theta(\xi)] \bar{q} \left\{ \mu_H [1 - \tau] + F\tau + [1 + \omega] R\tau \right\}$$

$$+ \left\{ [1 - \theta(\xi)][1 - \delta] \bar{q} + \bar{q} \theta(\xi) \right\} \left\{ \int_{0}^{F+1+\omega]R} x \, dL + \int_{F+[1+\omega]R}^{\bar{x}_{L}+[1-\gamma]\mu_{m}} x[1 - \tau] \, dL \right\}$$

$$+ F\tau [1 - L(F + [1 + \omega] R)] + \tau [1 + \omega] R [1 - L(F + [1 + \omega] R)] \right\}$$

$$+ [1 - \bar{q}] [1 - \theta(\xi)] R + \left[1 - \bar{q}\right] \theta(\xi) R.$$ (A.16)

Thus, using (25) to substitute for all the terms other than $V_T$ in (A.15) gives us:

$$\Omega_D(\xi) = V_T - [1 + \omega] R \left[ \hat{s}(\xi) \right]^{-1}.$$ (A.17)
Now,

$$\frac{\partial V_T}{\partial \xi} = -\delta \theta'(\xi) \bar{\eta} X_1 - \theta'(\xi) \left\{ [1 - \delta] \bar{\eta} - \bar{\eta} \right\} X_2 - [1 - \bar{\eta}] \theta'(\xi) R + [1 - \bar{\eta}] \theta'(\xi) R, \quad (A.18)$$

where

$$X_1 \equiv \mu_H [1 - \tau] + F \tau + [1 + \omega] R \tau, \quad (A.19)$$

$$X_2 \equiv \int_{-\tau}^{\bar{x} + [1 + \omega] R} x \, dL + \int_{F + [1 + \omega] R}^{x + [1 + \omega] \nu m} x [1 - \tau] \, dL + F \tau [1 - L (F + [1 + \omega] R)] + \tau (1 + \omega R (1 - L (F + [1 + \omega] R))). \quad (A.20)$$

Simplifying (A.18) yields:

$$\frac{\partial V_T}{\partial \xi} = -\delta \theta'(\xi) \bar{\eta} [X_1 - X_2] - [\bar{\eta} - \bar{\eta}] \theta'(\xi) [X_2 - R]$$

$$< 0. \quad (A.21)$$

Thus, since \(\theta' > 0\), it follows that \(\partial V_T / \partial \xi < 0\). Moreover, since \(\theta'' > 0\), it also follows that \(\partial^2 V_T / \partial ^2 \xi < 0\).

Returning to (A.17), we have the optimal \(\xi\), call it \(\xi^o\), satisfying the first-order condition:

$$\frac{\partial \Omega_D (\xi)}{\partial \xi} = \left[ \frac{\partial V_T}{\partial \xi} \right] + [1 + \omega] R \bar{s}(\xi)^{-2} \left[ \frac{\partial \bar{s}}{\partial \xi} \right]$$

$$= 0. \quad (A.22)$$

The second-order condition is:

$$\left[ \frac{\partial^2 V_T}{\partial \xi^2} \right] - 2 [1 + \omega] R \bar{s}(\xi)^{-3} \left[ \frac{\partial \bar{s}}{\partial \xi} \right] + [1 + \omega] R \bar{s}(\xi)^{-2} < 0. \quad (A.23)$$

As shown in (A.3), \(\partial \bar{s} / \partial \xi > 0\), and as shown in (A.4), \(\partial^2 \bar{s} / \partial \xi^2 < 0\). Thus, the second-order condition in (A.23) holds.

Finally, we prove that \(\xi^o > \xi^*\). Compare the first-order-condition (A.7) that is satisfied for \(\xi^*\)
with the first-order condition (A.22) above. Note that \( \partial \Omega / \partial \xi < 0 \) in (A.7) and \( \partial V_T / \partial \xi < 0 \) in (A.22). Thus, if \( |\partial \Omega / \partial \xi| > |\partial V_T / \partial \xi| \), then it will follow that in (A.22): \( \partial \Omega_D(\xi) / \partial \xi |_{\xi=\xi^*} > 0 \), so \( \xi^o > \xi^* \).

Comparing \( |\partial \Omega / \partial \xi| \) and \( |\partial V_T / \partial \xi| \) and collecting all the terms containing \( \mu_H \), it can be seen that \( |\partial \Omega / \partial \xi| > |\partial V_T / \partial \xi| \) if \( \bar{q} \delta [1 - \tau] \mu_H [1 - \delta] \) exceeds all of the terms not containing \( \mu_H \). Thus, for \( \mu_H \) large enough, \( |\partial \Omega / \partial \xi| > |\partial V_T / \partial \xi| \). Thus, \( \xi^o > \xi^* \). ■

**Proof of Proposition 5:** Take the optimal solution, \( \xi^o \), with debt financing and evaluate the total value of the firm at \( \xi^o \). It follows that the loss in firm value due to risk-shifting is

\[
[1 - \tau] \left\{ [1 - \theta(\xi^o)] \bar{q} + q \theta(\xi^o) \right\} \kappa \nu m. \tag{A.24}
\]

The expected debt tax shield is given by \( \Gamma_F(\xi^o) \), where \( \Gamma_F \) is defined in (27). Thus, for \( \tau \) low enough and \( \kappa \nu m \) high enough, (29) holds, so the loss in firm value due to risk-shifting exceeds the debt tax shield at \( \xi^o \). This means that the wealth of the initial shareholders is lower with debt financing (for any \( F \)) than with outside equity financing at \( \xi^o \), and hence also at \( \xi^* \), the optimal disclosure with equity. The rest of the proof follows in a straightforward manner from the definition of the equilibrium. ■

**Proof of Lemma 4:** Note first that

\[
\frac{\partial \Omega}{\partial \xi} = -\theta' \left\{ \left[ \bar{G} + \delta r [\mu_J - \mu_H] \right] \bar{q} - q \mu_L + R [1 - \bar{q} - 1 + \bar{q}] \right\} \\
= - [1 - \kappa] \theta' \left\{ \bar{q} \delta r [\mu_J - \mu_H] + [\bar{q} - q] [\bar{G} - R] + q [\bar{G} - \mu_L] \right\} \\
< 0, \tag{A.25}
\]

and

\[
\frac{\partial^2 \Omega}{\partial \xi^2} = - [1 - \kappa] \theta'' \left\{ \bar{q} \delta r [\mu_J - \mu_H] + [\bar{q} - q] [\bar{G} - R] + q [\bar{G} - \mu_L] \right\} \\
< 0, \tag{A.26}
\]
since \( \theta'' > 0 \). Now substituting (33) in (31), we can write the firm’s objective function as:

\[
\Omega(r, \xi) - [1 + \omega + \Delta] R [\hat{s}(\xi)]^{-1}.
\]  
(A.27)

The first-order condition for the optimal \( \xi \), call it \( \xi^{**} \), is:

\[
\frac{\partial \Omega}{\partial \xi} + [1 + \omega + \Delta] R [\hat{s}(\xi)]^{-2} \left[ \frac{\partial \hat{s}}{\partial \xi} \right] = 0.
\]  
(A.28)

The second-order condition is:

\[
\Theta \equiv \frac{\partial^2 \Omega}{\partial \xi^2} - 2 [1 + \omega + \Delta] R [\hat{s}(\xi)]^{-3} \left[ \frac{\partial \hat{s}}{\partial \xi} \right]^2 + [1 + \omega + \Delta] R [\hat{s}(\xi)]^{-2} \left[ \frac{\partial^2 \hat{s}}{\partial \xi^2} \right] < 0.
\]  
(A.29)

Since \( \frac{\partial^2 \Omega}{\partial \xi^2} < 0 \) and \( \frac{\partial^2 \hat{s}}{\partial \xi^2} < 0 \), it is clear that (A.29) holds. Thus, a unique optimum \( \xi^{**} \) exists.

Now, totally differentiate the first-order condition (A.28) to write

\[
\Theta \left[ \frac{d\xi^*}{dr} \right] + \frac{\partial^2 \Omega}{\partial \xi \partial r} = 0,
\]  
(A.30)

which gives

\[
\frac{d\xi^*}{dr} = -\left[ \frac{\partial^2 \Omega/\partial \xi \partial r}{\Theta} \right].
\]  
(A.31)

Using (A.25), we can write:

\[
\frac{\partial^2 \Omega}{\partial \xi \partial r} = -\theta' \left\{ \left[ \bar{q} - q \right] \delta [\mu_J - \mu_H] \right\} < 0.
\]  
(A.32)

Since \( \Theta < 0 \), it follows from (A.31) and (A.32) that \( d\xi^*/dr < 0 \). ■

**Proof of Lemma 5:** Consider \( r_1 < r_2 \) and suppose the arbitrator asks each firm to report its \( r \) and then implement the first-best solution. Let \( \xi_i \) and \( f_i \) be the disclosure level and ownership fraction sold by the firm corresponding to a report of \( r_i \). Then if the \( r_1 \) firm reports \( r_2 \), its insiders’
expected utility is

\[ [1 - f_2] \Omega (r_1, \xi_2) > [1 - f_2] \Omega (r_1, \xi_1) \]
\[ > [1 - f_1] \Omega (r_1, \xi_1), \]  
(A.33)

where the first inequality follows since \( \Omega \) is decreasing in \( \xi \) and \( \xi_1 > \xi_2 \) (which follows from Lemma 4, which states that the first-best \( \xi \) is strictly decreasing in \( r \)), and the second inequality follows since \( f_1 > f_2 \). Note that \( f_1 > f_2 \) follows from (33) and the fact that \( \Omega (r, \xi) \) defined in (32) is strictly increasing in \( r \) and the right-hand side of (A.33) is a constant. Thus, the \( r_1 \) firm will misreport its type as \( r_2 \).  

\[ \blacksquare \]

**Proof of Lemma 6:** Substituting from (41) into (39), we can write (suppressing \( \xi \) as an argument of the functions):

\[
U(r) = \left[ \Omega (r) - \frac{[1 + \omega + \Delta]}{\hat{s}} + P_0 - P_0 l^{-1} \right] \pi (r)
\]
\[
= \pi (r) \left[ \Omega (r) - \frac{[1 + \omega + \Delta]}{\hat{s}} R - [l^{-1} - 1] P_0 \right]. \]  
(A.34)

We will first show that (40) implies parts 1 and 2 of the lemma. From (40) we have that \( U(r \mid r) \geq U(\tilde{r} \mid r) \), so:

\[
\pi (r) \left[ \Omega (r) - \frac{[1 + \omega + \Delta]}{\hat{s}} R - [l^{-1} - 1] P_0 (r) \right]
\]
\[
\geq \pi (\tilde{r}) \left[ \Omega (\tilde{r} \mid r) - \frac{[1 + \omega + \Delta]}{\hat{s} (\tilde{r})} R - [l^{-1} - 1] P_0 (\tilde{r} \mid r) \right]
\]
\[
= \pi (\tilde{r}) \left[ \Omega (\tilde{r}) - \frac{[1 + \omega + \Delta]}{\hat{s} (\tilde{r})} R - [l^{-1} - 1] P_0 (\tilde{r}) \right] + B_1 (\tilde{r}) \delta [\mu_J - \mu_H] \pi (\tilde{r})
\]
\[
- B_1 (\tilde{r}) \delta [\mu_J - \mu_H] \pi (\tilde{r}) + [l^{-1} - 1] B_1 (\tilde{r}) \left[ \frac{\delta [1 - r] [\xi - x_L]^2}{2 [x_H - x_L]} \right] \pi (\tilde{r})
\]
\[
- [l^{-1} - 1] B_1 (\tilde{r}) \left[ \frac{\delta [1 - \tilde{r}] [\xi - x_L]^2}{2 [x_H - x_L]} \right] \pi (\tilde{r})
\]
\[
= U(\tilde{r}) + B_1 \delta [r - \tilde{r}] \pi (\tilde{r}) \left[ \mu_J - \mu_H \right] + [l^{-1} - 1] \left\{ \frac{[\xi - x_L]^2}{2 [x_H - x_L]} \right\} . \]  
(A.35)
Thus,
\[ U(r) - U(\tilde{r}) \geq [r - \tilde{r}] N(\tilde{r}), \tag{A.36} \]
where
\[ N(\tilde{r}) \equiv \pi(\tilde{r}) [1 - \kappa] B_1 \delta \left[ [\mu_j - \mu_H] + [t^{-1} - 1] \left\{ \frac{[\xi - x_L]^2}{2 [x_H - x_L]} \right\} \right]. \tag{A.37} \]

Similarly (reversing the roles of \(r\) and \(\tilde{r}\)):
\[ U(\tilde{r}) - U(r) \geq [\tilde{r} - r] N(r), \tag{A.38} \]
which implies
\[ U(r) - U(\tilde{r}) \leq [r - \tilde{r}] N(r). \tag{A.39} \]
Combining (A.36) and (A.39) yields:
\[ [r - \tilde{r}] N(\tilde{r}) \leq U(r) - U(\tilde{r}) \leq [r - \tilde{r}] N(r). \tag{A.40} \]

Inspection of (A.40) shows that if \(r > \tilde{r}\), then the function \(N(r)\) is non-decreasing. Given this monotonicity, we can divide through by \(r - \tilde{r}\) and take the limit as \(\tilde{r} \to r\) to write:
\[ \lim_{\tilde{r} \to r} \frac{U(r) - U(\tilde{r})}{\tilde{r} - r} = U'(r) = N(r) > 0 \text{ almost everywhere.} \tag{A.41} \]

Since \(N(r)\) is non-decreasing, it follows that \(U'' \geq 0\) almost everywhere. Thus we have shown that (40) implies parts 1 and 2 of the Lemma.

Next, we will show that parts 1 and 2 of the lemma imply (40). Note that
\[ U(r \mid r) - U(\tilde{r} \mid r) = U(r \mid r) - U(\tilde{r} \mid r) + [r - \tilde{r}] N(\tilde{r}) \]
\[ = \int_{\tilde{r}}^{r} U'(t \mid t) dt - [r - \tilde{r}] U'(r \mid \tilde{r}) \]
\[ \geq 0, \tag{A.42} \]
using part 1 of the lemma, \(U'' \geq 0\), and the mean value theorem for integrals.
Proof of Lemma 7: Since the global I.C. constraint has been shown to be equivalent to $U'(r) = N(r)$ almost everywhere in the previous lemma, let us integrate that condition to obtain:

$$\int_{r_a}^{r} U'(\tilde{r}) \, d\tilde{r} = \int_{r_a}^{r} N(\tilde{r}) \, d\tilde{r}, \quad (A.43)$$

which means

$$U(r) - U(r_a) = \int_{r_a}^{r} N(\tilde{r}) \, d\tilde{r} \quad \Rightarrow U(r) = U(r_a) + \int_{r_a}^{r} N(\tilde{r}) \, d\tilde{r}. \quad (A.44)$$

Taking the expectation of (A.44) yields:

$$\int_{r_a}^{r_b} U(r)z(r)dr = U(r_a) + \int_{r_a}^{r} \left[ \int_{r_a}^{r} N(t) dt \right] z(r)dr$$

$$= U(r_a) + \int_{r_a}^{r} N(t) \left[ \int_{t}^{r} z(r)dr \right] dt$$

$$= U(r_a) + \int_{r_a}^{r_b} \phi(r)N(r)z(r)dr, \quad (A.45)$$

where $\phi(r) \equiv \frac{[1-Z(r)]}{z(r)}$. Now we know from (39) that

$$\pi(r) \left[ \Omega(\xi,r) - P_0(r)l^{-1} \right] = U(r) + \pi(r)f\Omega(r). \quad (A.46)$$

Substituting in (A.46) for $f\Omega$ from (41) gives us:

$$\pi(r) \left[ \Omega(\xi,r) - P_0(r)l^{-1} \right] = U(r) + \pi(r) \left[ \frac{1 + \omega + \Delta}{\hat{s}} R - P_0(r) \right]. \quad (A.47)$$

Substituting (A.47) into (37) yields the objective function:

$$\int_{r_a}^{r_b} \left\{ U(r) + \pi(r) \left[ \frac{1 + \omega + \Delta}{\hat{s}} R + \alpha(r) - \Omega(\xi^*) - P_0(r) \right] \right\} z(r)dr. \quad (A.48)$$

The arbitrator can give insiders of the lowest type $(r = r_a)$ their expected utility with market financing. Let this expected utility be $\overline{u}_a$. Then set $U(r_a) = \overline{u}_a$ and substitute (A.45) in (A.48)
above to get

$$\pi_a + \int_{r_a}^{r_b} \left\{ \phi(r) N(r) + \pi(r) \left[ \frac{1 + \omega + \Delta}{{\hat{s}}} - \alpha(r) - \Omega(\xi^*) - P_0(r) \right] \right\} z(r) dr. \quad (A.49)$$

Now use (A.37) and write

$$N(r) = \pi(r) C_1 \left[ C_2 + \left[ l^{-1} - 1 \right] \left\{ \frac{[\zeta - x_L]^2}{2[x_H - x_L]} \right\} \right], \quad (A.50)$$

so that the arbitrator’s objective function (A.49) can be written as:

$$\pi_a + \int_{r_a}^{r_b} \pi(r) \left\{ \phi(r) \left[ C_1 C_2 + C_1 \left[ l^{-1} - 1 \right] \left\{ \frac{[\zeta - x_L]^2}{2[x_H - x_L]} \right\} \right] + \frac{1 + \omega + \Delta}{{\hat{s}}} + \alpha(r) - \Omega(\xi^*) - P_0(r) \right\} z(r) dr. \quad (A.51)$$

This completes the proof since maximizing (A.51) is equivalent to maximizing (48) because $\pi_a$ is a constant (i.e. independent of the mechanism design functions). ■

**Proof of Proposition 6:** Let us first prove (51). From optimal control theory, we know that the value function $\zeta$ that maximizes (A.51) is the one that involves maximizing the integral pointwise. Thus, the first-order condition for $\zeta$ is:

$$\phi(r) \left[ l^{-1} - 1 \right] B_1 \delta \left[ \zeta - x_L \right] [x_H - x_L]^{-1}$$

$$- \left\{ B_1 \delta [1 - r] \left[ \zeta - x_L \right] [x_H - x_L]^{-1} - B_1 [1 - \delta] - B_2 - B_3 \right\} = 0, \quad (A.52)$$

which yields (51) upon rearranging. The second-order condition is:

$$\phi(r) \left[ l^{-1} - 1 \right] B_1 \delta [x_H - x_L]^{-1} - B_1 \delta [1 - r] [x_H - x_L]^{-1} < 0, \quad (A.53)$$

which requires

$$B_1 \delta [x_H - x_L]^{-1} \left\{ \phi(r) \left[ l^{-1} - 1 \right] - [1 - r] \right\} < 0, \quad (A.54)$$
which holds since (47) tells us that
\[
\frac{1 - r}{\phi(r)} > l^{-1} - 1. \tag{A.55}
\]

Moreover, \(\partial \zeta / \partial r > 0\), also given (47). Inspection of (A.51) also reveals that the arbitrator will set \(\pi = 1\) whenever the term multiplying \(\pi(r)\) in (A.51) is positive and set \(\pi = 0\) otherwise. Since \(U'(r) > 0\) in equilibrium, it follows that \(\exists r^*\) such that \(\pi(r) = 1 \ \forall \ r \geq r^*\) and \(\pi(r) = 0\) otherwise.
\[\blacksquare\]
References


