HIV-AIDS and development: A reappraisal of the productivity and factor accumulation effects

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Abstract

We build an economico-epidemiological Solow-Swan model. Mortality and morbidity effects on effective labor are taken into account. A Ben-Porath-like mechanism affects the dynamics of the saving rate and reduces labor productivity. Based on optimal projections of the demographic and economic South-African series on the period 2000-2050, we identify a delayed effect of HIV-AIDS on economic growth: the growth rate gap between the AIDS and no-AIDS scenarios is rather stable between 2010 and 2020, but then it gets sharply larger between 2020 and 2030, keeps increasing at a much lower pace between 2030 and 2040, and finally stabilizes after 2040. The fall in active population is the main factor behind AIDS impact on economic growth during the decade 2020-2030 while the Ben-Porath mechanism on labor productivity is more relevant in the posterior decade. Physical capital accumulation plays a minor role.

Key words: AIDS epidemics, life expectancy, savings, Ben-Porath mechanism

JEL classification: I15, O11, J11, J21

1 Introduction

The impact of epidemics on the economic development process has witnessed a tremendous revival recently due to the worldwide AIDS pandemic and its persistence. Specially the case...
of sub-Saharan Africa is the focus of an increasing number of empirical studies in this respect (see e.g., Kalemli-Ozcan, 2012, de Araujo 2012, Durevall and Lindskog, 2011, Boucekkine et al., 2009, Glick and Sahn, 2007 and de Walque, 2006, 2007).\(^1\)

In a early study, Becker (1990) offered an assessment of the impact of the spread of AIDS on African population growth and economic performance. Deininger et al. (2005) explored the socio-economic implications of the AIDS epidemic for households in Uganda who received foster children between 1992 and 2000. The authors found that addition of a foster child resulted in significant reductions of per capita consumption, income, and household investment which were more pronounced for the poor. Aliber and Walker (2006) examined the impact of HIV/AIDS on land tenure in rural Kenya. The authors found fewer examples of dispossession of widows’ and orphans’ land rights than had been anticipated. They conclude that HIV/AIDS does aggravate tenure insecurity, due to the conjunction of population pressure, stigmatization, and gendered power relations. Wobst and Arndt (2004) analyzed the consequences of the HIV/AIDS pandemic in Tanzania for labor markets and human capital accumulation over 1990-2000. They found a sharp increase in labor force participation rates by 10-14 year olds, while over the same period, estimated education transition displayed an increased tendency to exit primary school. Nunnenkamp and Öhler (2011) assess empirically whether foreign official development assistance (ODA) has been effective in alleviating HIV/AIDS epidemics. The authors did not find that ODA has prevented new infections. They found mixed evidence on significant treatment effects on AIDS-related deaths for the major bilateral source of ODA (from United States and from multilateral organizations). Durevall and Lindskog (2012) studied the HIV-inequality relationship in Malawi and found a positive association between HIV infection and inequality at both the neighborhood and district levels, but no effect of individual poverty. Serieux et al. (2012) have kept a global view by studying the the effect of the global financial crisis on the delivery of HIV and AIDS-related services in Malawi. The authors found that while Malawi’s economy survived the global crisis relatively unscathed, there was clear evidence of a sharp deterioration in funding for agencies engaged in HIV-and AIDS-related programs in 2008 and 2009. Actually, the interest of economists has not been exclusively restricted to AIDS. Many studies have also been devoted to the Black Death or Spanish flu epidemics.

In particular, the empirical evidence on the economic effects of the Spanish flu is highly disputed. The question turns out to be whether say the Spanish flu did induce a fall or rise in per capita income growth in the short run. Empirically, the question is very far from trivial. First of all, one should recall that the Spanish flu occurred after the first world war, and therefore, part of the phenomena that took place in our period of interest is also probably due to the post-war adjustment dynamics. Second, and more generally, disentangling the effects of the epidemic is markedly complicated because one has to control for many other potential explanatory factors, like urbanization, the sectoral composition of the economy, initial GDP and other numerous variables. This seems like a daunting task. However, some very careful studies on this issue

\(^{1}\)See also the symposium on interactions between poverty and HIV/AIDS in *Economic Development and Cultural Change*, 2008, in particular Beegle et al. (2008), Chapoto and Jayne (2008), Glick and Sahn (2008).
have already come out. Brainerd and Siegler (2003) and Bloom and Mahal (1997a) are among the very best.2

Bloom and Mahal (1997a) studied the case of the Spanish flu in India. Precisely, they looked at the acreage sown in India across 13 Indian provinces. They found no relationship between the magnitude of population decline and the variation in acreage sown per capita across provinces. In a more detailed investigation, Brainerd and Siegler (2003) focused on the impact of the Spanish flu in the US. In their study, the dependent variable is the growth rate of per capita income from 1919-1921 to 1930, and the primary explanatory variable is the number of flu and pneumonia deaths per 1000 persons in each state of the US reported in 1918 and 1919. A nice feature of this study is the inclusion of many more variables to control for other potentially important factors (like education levels, initial income, agricultural share of personal income, ethnic composition...). The main result of their econometric regressions is the significant and positive impact of the Spanish flu on the growth rate of per capita income: “... the flu coefficient ranges between 0.219 and 0.235... and is always statistically significant at the 5 percent level or lower...” (Brainerd and Siegler, 2003, p. 17). And the authors conclude that along with conditional convergence and the rise of education, the Spanish flu does significantly matter in the economic growth history of US.

Just like the Spanish flux epidemic’s empirical literature, the debate is strikingly disputed among economists concerning the economic consequences of AIDS, specially in sub-Saharan Africa countries. In a highly influential paper, Bloom and Mahal (1997b) found no significant effect of AIDS on the growth rate of per capita income, and no evidence of reverse causality. They used simple cross-section regression models on a sample of 51 countries from 1982 to 1992. The estimated coefficients were found typically small and insignificant.

Such result went at odds with the results obtained at the same time on more theoretically founded models à la Cuddington and Hancock (1994), which generally predicted a relatively important growth impact of AIDS. An important reference here is the paper of Over (1992). The author used a relatively sophisticated computable general equilibrium model with three classes of workers, and rural versus urban production. This ultimately allowed the author to study the impact of several AIDS scenarios, based on different assumptions about relative levels of HIV infection in educated Vs. uneducated workers... In the most reasonable scenarios (according to Over, 1992), the effect in the 10 most affected sub-Saharan Africa countries would be 0.6 percentage point over the period 1990-2025 if all treatment costs were financed from savings.

More recently, some new contributions putting forward the human capital channel have found large effects of AIDS on growth. For example, Corrigan et al. (2005) have used a calibrated Overlapping Generation (OLG) model to analyze particularly the effect of the drop

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2 Another related known and even classical investigation on the growth effect of epidemics is due to Jack Hirshleifer in his celebrated book, *Economic Behaviour in Adversity*, 1987. Hirshleifer (1987) examined the case of the plague which killed one-third of the European population between 1348 and 1351. The author suggested that the plague by sharply reducing the population size led to a rapid and persistent rise in real wages for laboring classes.
in life expectancy on investment, and the large generation of orphans produced by AIDS. Their results are completely in line with Cuddington and Hancock (1994) and Over (1992). McDonald and Roberts (2006) used an econometric specification combining growth and health capital equations. Applied on African countries, the model predicts substantial effects of the epidemic: the marginal impact on income per capita of a one percent increase in HIV prevalence rate is minus 0.59%. The authors conclude that while the human and social costs of the HIV/AIDS epidemic are major causes for concern, their results do indicate that the macroeconomic effects of the epidemic are by no way negligible. Finally Ferreira and Pessoa (2003) find that in the face of an AIDS-like epidemic schooling time can decline by half, which cannot be neutral for long-run economic growth.

At the same time, another controversy emerges as to the effect of AIDS on fertility. Whether the epidemic has decreased or increased the fertility rates in the countries most affected by AIDS/HIV is of course a sensitive point if one aims at gathering a clear diagnosis on the impact of the epidemic on per capita variables, which happens to be the most frequently used indicators of welfare. In a highly controversial paper, Young (2005) claims that AIDS should lower fertility for two main reasons. On one hand, the epidemic has certainly reduced the willingness to engage in unprotected sexual activity. On the other, the high mortality of adult males and the resulting increasing scarcity of labor are likely to increase the value of woman’s time. Both channels are possibly strong enough to induce a durable decrease in fertility, which may cause future consumption per capita to rise. Using a Barro-Becker based empirical model, the author finds that in the case of South-Africa, this decreasing fertility engine is so strong that it dominates the human capital channel put forward by Corrigan et al. (2005) for example. Hence, AIDS might well be interpreted as a “gift of the dying” for future South African generations. In a more recent study on a panel of African countries, Boucekkine et al. (2009) reach a similar conclusion on the impact of mortality shocks on (net) fertility, but their study, not including an assessment of the impact of mortality shocks on schooling, does not deliver the same optimistic and decisive view of the role of fertility decline in the long-run development process.

Actually, even the fertility decline finding has been strongly criticized in the literature. In particular, Kalemli-Ozcan (2006), who studied the fertility issue on a panel of 44 African countries over the period 1985-2000, finds that the HIV/AIDS epidemic affects the total fertility rates positively and the school enrollment rates negatively. In this paper, we shall adopt the position taken by most demographers (like those of the US Census Bureau), that it is the low perception of HIV/AIDS risks in sub-Saharan Africa makes quite unrealistic the occurrence of drastic changes in fertility which can offset all the other well-known negative effects of epidemics. However, a compelling evidence on the sharp negative effect on schooling has been gathered over the two last decades, and we argue that this is a key point for getting through the empirical literature on AIDS impact on economic growth.

In this paper, we study as to how the interaction of AIDS, life expectancy and productivity

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3This outcome can be rationalized in a model with precautionary demand for children in face of uncertainty about child survival.
over the life cycle influences the macro economic development, and we highlight the influence of life expectancy on growth through savings. For that purpose, we shall extend the framework of Cuddington and Hancock (1994) in order to account for the human capital channel, thanks to the Ben-Porath mechanism, an aspect left in the dark till now. We shall also amend the model in order to cope with some of the important criticisms raised by Bloom and Mahal (1997b) in their posterior econometric study. We shall develop these amendments in detail in the next sections.

Our aim is to develop a simple general equilibrium framework, which in addition to the typical factor accumulation mechanisms inherent to the neoclassical growth theory, also encompasses some of the salient characteristics of AIDS, notably the effect on schooling time and/or life expectancy. Incidentally, we will show in our application to the South African case that there might not be any fundamental conflict between the results obtained by authors like Bloom and Mahal (1997b), and others like Corrigan et al. (2005): A relatively short term assessment à la Bloom and Mahal (1997b) might not reveal any dramatic AIDS growth effect, while a long term perspective, relying on the evolution of key demographic variables like mortality and life expectancy, might yield just the contrary.

The paper is organized as follows. Section 2 presents the Cuddington and Hancock (1994) set-up and discusses its limitations. Section 3 develop an enlarged model incorporating schooling and life expectancy trends. Section 4 provides details on data and methodology for application to the South African case. Section 5 reports the results of the experiments. Section 6 summarizes, discusses and concludes the study.

2 The benchmark model

Cuddington and Hancock (1994) have proposed a very simple accounting exercise to measure to which extent AIDS harms (or could have harmed) GDP growth in some sub-Saharan Africa countries. In their 1994 *Journal of Development Economics* paper, they have applied it to Malawi. Cuddington and Hancock’s set-up is a very useful tool to get an immediate idea about the extent of damages caused by AIDS. In what follows, we shall develop it, and then outline its limitations.

2.1 The Cuddington-Hancock accounting set-up

The set-up is of the Solow type, and it is based on the production function:

\[ Y(t) = A(t) K(t)^{\theta} \left( [1 - \phi(t)] x(t) \right) \mu(t) L(t)^{1-\theta} \]

where \( Y(t) \) denotes the total output (or GDP) of the economy. It is produced with a Cobb-Douglas technology with two factors, physical capital, \( K(t) \), and labor, \( L(t) \), \( \theta \) being the capital share. With respect to the standard Solow model, some epidemic-specific variables are introduced. In particular, a new term, \( \mu(t) \), appears, supposed to capture labor-specific productivity, and in this sense, it could be interpreted as a human capital indicator. Additionally, the new production function includes a term \( x(t) \), which reflects the role of morbidity: a larger \( x(t) \)
amounts to a lower effective labor effort due to morbidity. In a more general setting, such a loss may be reduced by medical care. In Cuddington and Hancock (1994), it is assumed exogenous: the authors consider all the situations when $x(t)$ ranges from 0 to 1. Finally, the production function includes a term $\phi(t)$, which stands for the AIDS prevalence rate at date $t$. Of course, the loss in productivity due to morbidity depends on the spread of the epidemic, and such a characteristic is reasonably captured by the prevalence rate.

Another highly interesting aspect of the framework developed by Cuddington and Hancock (1994) is the introduction of the age structure of the labor force in the production function. Of course the epidemic does not affect in the same way all the age classes, such a refinement is therefore not only useful, it is necessary. Call $E(t)$ the effective labor force, that is

$$E(t) = [1 - \phi(t) x(t)] \mu(t) L(t)$$

such a magnitude may be rewritten in a straightforward way taking into account the age distribution:

$$E(t) = \sum_i [1 - \phi_i(t) x_i(t)] \mu_i(t) L_i(t), \quad (1)$$

where $i$ stands for the age index. Cuddington and Hancock (1994) have made further simplifications. First, the authors assume $x_i(t) = \xi$, where $\xi$ is a constant comprised between 0 and 1, $\forall i$ and $\forall t$. Second, it is assumed that $\mu_i(t) = \mu_i$, $\forall t$. Third, the model postulates a simple quadratic form for age-specific productivity:

$$\mu_i = \rho_1 + \rho_2 (i - \bar{i}) - \rho_3 (i - \bar{i})^2, \quad (2)$$

where $\rho_k, k = 1, 2, 3$ are three positive numbers, and where $\bar{i}$ is, for example, the minimal age to enter the labor market.\footnote{Cuddington and Hancock (1994) took $\bar{i} = 15$.} Equation (2) merely states that productivity is a quadratic function of age, and in this sense, it exclusively captures the experience determinant of productivity. The set-up is completed by a capital accumulation equation:

$$K(t) = s Y(t) + (1 - \delta) K_{t-1}, \quad (3)$$

where $s$ stands for the saving rate of the economy (assumed constant by Cuddington and Hancock, 1994), and with $K_0$ given. To be more precise, the authors retrieve a term $xH_t$ from the right hand side of equation (3), where $H_t$ stands for total health expenditures, and $x$ is the fraction of these expenditures related to AIDS. We shall consider here the saving rate $s$ in a broader sense, it is the fraction of income not spent in consumption and health expenditures, which allows us to write capital accumulation as usual.

Using the demographic projections issued by the World Bank for Malawi, Cuddington and Hancock (1994) have studied to which extent the AIDS epidemic has affected and will affect GDP and GDP per capita in this country in the period 1985-2010. The World Bank projections entailing a comparison in terms of mortality and morbidity between AIDS and without AIDS
configurations, Cuddington and Hancock (1994) have also conducted this comparison in more economic terms using such a valuable demographic information (i.e. in variables $L_{it}$, and $A_{it}$). Indeed, the authors distinguished between an extreme AIDS scenario and a medium one: In the former scenario, average real GDP growth over the period 1985-2010 would cost 1.2 to 1.5 percentage points relative to the non-AIDS counter-factual case, while in the latter the figure drops to only 0.2 to 0.3.\(^5\) Concerning annual growth rate of real GDP per capita, the study shows an average depression of 0.25 percentage points through the year 2010.

2.2 Limitations of the benchmark model

Whatever the shortcomings of the benchmark framework, which does not incorporate and is not aimed at incorporating all the economic mechanisms induced by an AIDS epidemic, the results of Cuddington and Hancock (1994) have the merit to suggest that the growth effects of AIDS could be indeed sizeable in some African countries. However, some reservations have been raised, among others by Bloom and Mahal (1997b). These limitations are related to the absence of economic mechanisms induced by the AIDS epidemic that we summarize in a few points.

1. Bloom and Mahal (1997b) questioned the treatment of Cuddington and Hancock (1994) on the specific ground of the labor market in sub-Saharan Africa countries. According to Bloom and Mahal (1997b), the presence of a labor surplus could mitigate the output losses that might otherwise be associated with AIDS morbidity and mortality. Apparently, such a criticism does not seem to have a decisive scope, at least in certain countries. Indeed, in a companion paper, Cuddington (1993) has shown that his results are not that sensitive to the presence of surplus labor in the Tanzanian case.

2. A clearer shortcoming of the setting is the treatment of morbidity. The variable $x(t)$ is taken exogenous (and indeed, it is constant) while it should depend on medication. We shall amend this aspect of the original modelling closely.

3. Bloom and Mahal (1997b) also questioned the way health expenditures enter the accumulation equation. In Cuddington and Hancock (1994) setting, health expenditures show up exclusively as a decrease in savings channeled into capital accumulation. This might not be the case in real life: health expenditures are also detrimental to ordinary consumption expenditures. Overall, there is a very interesting issue of how to deal with savings in a context of epidemics. In our enlarged model, we shall use the analysis and findings of Freire (2002) to overcome this important difficulty.

4. A last limitation would be the way productivity, through variable $\mu_i$, is modelled, only relying on experience. Clearly, such a variable should also reflect the education level and other related socioeconomic determinants (like the gender). Also, the time-independence could be questioned in a more long term perspective: With life expectancy dropping from

\(^5\)The range is generated by letting $\xi$ and $x$ move from 0 to 1.
about 60 years to 40, one is tempted to suspect that human capital accumulation would be toughly affected, which would induce a downward trend in productivity. Actually, with the numerical values considered by Cuddington and Hancock (1994) for parameters \( \rho_i, i = 1, 2, 3 \) and \( \tilde{i} \), the productivity variable \( \mu_i \) is maximal when the individual is 60 years old. The issue is whether such picture is consistent with the recent evolution of life expectancy in sub-Saharan Africa.

### 3 The enlarged model

In this next section, we shall amend Cuddington and Hancock (1994) set-up by integrating the Ben-Porath (1967) mechanism, meaning that we shall incorporate schooling and life expectancy trends.

#### 3.1 The Ben-Porath’s mechanism: update debate

At this stage of our study, it is worth to clarify the mechanism of Ben-Porath which is a strong point of our contribution. This mechanism has recently sparked a strong debate in the literature. Following the seminal contribution of Ben-Porath (1967), the idea emerged that the gains in life expectancy positively impact schooling by increasing the horizon over which investments in schooling have been paid off. The rational of the Ben-Porath (1967) model is that individuals choose their human capital according to the future rewards that this human capital will receive. Several prominent predictions have been based on this mechanism, including the fact that an increase in rental rate on human capital will increase future rewards to human capital and as a result, increase investment in schooling.

Hazan (2009) challenged this view by claiming that an increase in expected lifetime labor supply is a necessary condition for an increase in longevity to induce more investment in schooling. Hazan (2009) then presents evidence of a sharp reduction in expected total working hours for U.S. workers born in the period 1840-1970 that the author interprets as pointing to a violation of the necessary condition and concludes that the reduction in mortality rates in the U.S. over this period cannot account for any of the increase in education attainment. This conclusion has very important policy implications since it challenges the view that reducing mortality and improving health conditions may promote the acquisition of human capital, since it questions the empirical rationale of studying the relation between mortality and human capital.

Recently, Cervellati and Sunde (2013) pointed that the model in Hazan (2009) assumes a perfectly rectangular survival probability and a linear human capital production function, meaning that individuals are assumed to survive with probability one during all their life, and die with probability one when reaching their life expectancy. As result, mortality can affect the education decision only by extending the maximum longevity, but not by changing the probability of surviving during working ages. The assumption in Hazan (2009) is a strong counterfactual and hides the effect of observed changes in age-specific mortality rates on the costs and benefits of education which is presents most theoretical frameworks that study endogenous...
schooling in the context of changing mortality, e.g. de la Croix and Licandro, (1999), Boucekkine et al. (2002, 2003), Soares (2005), and Cervellati and Sunde (2005).\textsuperscript{6}

Cervellati and Sunde (2013) generalized Hazan’s (2009) model and show that, in general, the necessary condition for a reduction in mortality rates to induce more years of schooling is that the increase in longevity is related to an increase in the benefits of schooling relative to the opportunity costs of a delayed entry into the labor market. The authors also replicate the empirical analysis of Hazan (2009), and found no evidence that greater longevity has been associated with a decline in the relative benefits of schooling. This closes the debate on the Ben-Porath mechanism which is still valid in explaining the data.

3.2 Incorporating schooling and life expectancy trends

Our starting point is the following: as shown by many authors, the observed fall in life expectancy in most sub-Saharan Africa countries, one of the main consequences of the AIDS pandemic, should have induced a decline in schooling time, in addition to other dramatic effects on savings incentives. Ferreira and Pessoa (2003) find that in the face of an AIDS-like epidemic schooling time can decline by half, which is in our view quite fundamental for long run growth rate. In order to adapt the benchmark Cuddington-Hancock model to account for such crucial features, we introduce the following modifications.

1. Concerning the production function, we have incorporated AIDS-related health expenditures in the measurement of productivity, exactly as in Corrigan et al. (2005).\textsuperscript{7} In order to capture the gender-specific characteristics of the epidemics, we also distinguish between males and females (index $f = 1, 2$):

$$E(t) = \sum_{i,f} [1 - \phi_{i,f}(t) \Phi(m_{i,f}(t))] \mu_{i,f}(t) L_{i,f}(t),$$

where $m_{i,f}(t)$ measure AIDS-related health expenditures for an individual belonging to the age class $i$ and with gender $f$ at time $t$. The introduction of a gender variable seems to us an important step. A crucial recent feature of HIV/AIDS in sub-Saharan Africa (and notably in South Africa) is the increasing percentage of females affected. In its 2004 report, UNAIDS mentioned that close to 60% of HIV/AIDS infected people are females in sub-Saharan Africa, the youngest being the most exposed to the infection risk for some obvious reasons.\textsuperscript{8}

\textsuperscript{6}In a theoretical setting, Boucekkine et al. (2008) considered physical capital accumulation, schooling, health expenditures and supply effects within a Blanchard two-sector economy to capture life-cycle effects of AIDS-like epidemics.

\textsuperscript{7}Since it is a Solow model, we don’t have to determine the optimal pace of health expenditures given the demographic and epidemiological characteristics of AIDS. This is done properly in Feichtinger et al.(2004), and Almeder et al. (2006).

2. The productivity variables $\mu$ are specified in order to capture the effect of the declining life expectancy on productivity at work. We do this as follows. Notice that with the benchmark specification (2), the age at which $\mu_i$ is maximal is equal to $\hat{i} + 2 \frac{\alpha_i}{\beta_i}$. With a declining life expectancy, such a magnitude is likely to go down. This comes mainly through the Ben-Porath mechanism, as pointed out by Boucekkine et al. (2002), according to which a decreasing life expectancy lowers the schooling time. We simply capture this mechanism by endogenizing the coefficient $\rho_2$ and assuming the following functional relationship:

$$\rho_2(i, f, t) = \alpha_{i,f} \nu_{i,f,t}^\beta,$$

where $\nu_{i,f,t}$ is the life expectancy at birth of workers of age $i$ (thus born at $t - i$) and of gender $f$. $\alpha_{i,f}$ and $\beta$ are calibrated. $^9$ With such a new specification, the age-specific productivities become time and gender dependent via life expectancy:

$$\mu_{i,f,t} = \rho_1 + \rho_2(i, f, t) (i - \hat{i}) - \rho_3 (i - \hat{i})^2, \quad (5)$$

For the calculation of $\rho_2$, we set for the reference year, $\rho_2(i, f, t_0) = \alpha_i \nu_{i,f,t_0}^\beta = 0.005$ for a given $\beta$, then we calibrate $\alpha_i = \frac{0.005}{\nu_{i,f,t_0}^\beta}$, where 0 indicates the base year (2000). The determination of $\alpha_i$ at the basic year allows us to determine the $\rho_2$. We set the values of the other parameters as follows: $\rho_1 = 0.8$, $\rho_3 = -0.0001$ and we analyze the cases where $\beta$ takes different values from 0 (no Ben-Porath mechanism) to 1 (a “linear” mechanism).

3. Determination of $E$, $K$ and $Y$

i) In the no AIDS case, the prevalence rates are set to zero. Then we have, $E(t) = \sum_{i,f} \mu_{i,f(t)} L_{i,f}(t)$ with $L_{i,f}(t) = (pans - u)h$, where $pans$ indicates the active population without AIDS by age and sex, $u$ is the number of unemployed people by age and sex, and $h$ is the number of worked hours in a year (we use 49 weeks and 40 hours by week, that is $h = 1960$).

ii) As previously stated, our production function is of the type

$$Y_t = (1 + \gamma)^t E_t^{1-\theta} K_t^\theta, \quad (6)$$

then $K_0$ is given by the following relation

$$K_0 = K_{2000} = \left( \frac{Y_{2000}}{\gamma^0 E_{2000}^{1-\theta}} \right)^\frac{1}{\theta}, \quad (7)$$

where $Y_{2000}$ is the GDP of the base year 2000. The physical capital $K(t)$ is obtained with the relation

$$K_{t+1} = s_t Y_t + (1 - \delta) K_t \quad (8)$$

$^9$In particular, the double sequence $\alpha_{i,f}$ is calibrated in such a way that $\rho_2(i, f, t_0) = \alpha_{i,f} \nu_{i,f,t_0}^\beta$, for $\beta$ fixed, $t_0$ is the base year and $\rho_2(i, f, t_0)$ is equal to the constant coefficient $\rho_2$ considered by Cuddington and Hancock (1994).
To make our results comparable to the previous findings of the literature, we use the same parameter values as Corrigan et al. (2005), meaning that we set $\theta = 0.33$, $\gamma = 0.012$ and $\delta = 0.05$. The exogeneity of productivity growth can be questioned in a setting like ours emphasizing the impact of human capital and long-term impact of epidemics. We don’t endogenize $\gamma$ in this paper for two reasons. First, as mentioned just above, we want to keep some comparability with the seminal experiments of Cuddington and Hancock (1994). Second, even if one endogenizes productivity growth, for example by aggregating the human capital indicators $\mu_{i,t}(t)$ and tracking the evolution over time of the constructed aggregate, this wouldn’t change the main result of this paper, that’s the long-term impact of AIDS is much more important than its short time. In this sense, one could interpret the long-term effect computed in this paper as a lower bound. This lower bound is large enough to make neatly the point of this paper.

iii) In the case with AIDS, we of course account for the AIDS prevalence rates ($\phi_{i,t}(t)$) and AIDS related expenditures, and we use life expectancy at birth with AIDS in the determination of $\mu_{i,t}$ as explained before.

iv) However, we have faced a data unavailability problem when collecting AIDS-related health expenditures. Instead of the intended indicators $\Phi(m_{i,t}(t))$, we have been forced to use $\Phi(m(t))$ where $m(t)$ is given by the relation: $m(t) = txHIV \frac{M_t}{HIV^+}$ where $txHIV$ represents the percentage of AIDS related expenditures in the total health expenditures ($M_t$), and $HIV^+$ is the number of infected people. As in Corrigan et al. (2005), we pick the following analytical for $\Phi(.)$:

$$\Phi(m(t)) = 1 - \psi_1 + (\psi_1 - \psi_0) \frac{\zeta}{m(t) + \zeta},$$  

(9)

with: $\Phi(0) = 1 - \psi_0$, $\lim_{x \to \infty} \Phi(x) = 1 - \psi_1$, $0 < \psi_0 < \psi_1 < 1$, $\Phi'(x) < 0$ and $\Phi''(x) > 0$; $\psi_1$, $\psi_0$ and $\zeta$ are positive productivity parameters to be fixed. As AIDS-related expenditures rise, function $\Phi(.)$ goes down, which induces a lower productivity gap due to morbidity. In our numerical experiments, we fix $\psi_1 = 1$, $\psi_0 = 0.5$, and we let $\zeta$ vary from 1 to 10, with $\zeta = 5$ in the reference simulation, as in Corrigan et al. (2005).

4. Concerning the saving behavior, we rely on the previous empirical work of Freire (2002) on the South African case. Freire’s work is based on the seminal model of Blanchard (1985), and as such, it is much likely to capture, among others, the effects of increasing mortality on saving decisions than the very arbitrary computation rule adopted by Cuddington and Hancock, which was so toughly criticized by Bloom and Mahal (1997b). Actually, our treatment is intermediate between the “pessimistic” modelling adopted by Cuddington and Hancock, according to whom all AIDS-related health expenditures are fully detrimental to accumulation, and the excessively “neutral” modelling of Young (2005), who postulates a constant saving rate in a Solow-like setting.
4 Application to AIDS effects on growth in South Africa: Data and methodology

4.1 Data

We start with a brief review of the data used for the main economic and demographic indicators of the model and their source.

- **Economically active population, by age and sex (1980-2020).** The data comes from International Labor Organization. The database contains world, regional and country estimates and projections of the total population, the activity rates and the economically active population (labour force) by sex and five-year age groups (from 10 to 64 years and 65 years and over). These estimates and projections are for international comparisons and are neither superior nor necessarily inferior to national estimates and projections, which are produced using country-specific additional information. The economically active population comprises all persons of either sex who furnish the supply of labour for the production of goods and services during a specified time-reference period.

- **HIV-seroprevalence (1980-2015).** The data is provided by U.S. Census Bureau, International Programs Center. Estimated HIV adult prevalence trends from 1980 to 2015. These estimates were derived from the Epidemic Projection Package, an epidemiologically sound computer model that allows for a “best fit” of HIV prevalence data from antenatal clinic women who come in for their first antenatal visit. The HIV prevalence is defined as the percentage of women surveyed testing positive for HIV. Each year a national survey of HIV prevalence among women attending public antenatal clinics in South Africa is conducted by the Department of Health. The Annual HIV antenatal survey provides South Africa with annual HIV trends among pregnant women and further provides the basis for making other estimates and projections on HIV/AIDS trends.

- **HIV+ (1990-2015).** This indicator is defined as the number of people infected. The Demographic impact of HIV/AIDS in South Africa follows from National Indicators for 2004.

- **Life expectancy at birth by sex (1920-2015).** The data is provided by World Development Indicators, Health Nutrition and population and League of Nations, Northwestern University. This is the number of years that a new born could live if the normal conditions of mortality at his birth should be the same ones throughout its life.

- **Total health expenditure (1960-2000).** The data is extracted from the Health Nutrition and Population database.


The series on unemployment shown here relate in principle to the entire geographical area of a country. In 1982, the Thirteenth International Conference of Labour Statisticians adopted a new Resolution concerning Statistics of the Economically Active Population, Employment, Unemployment and Underemployment, in which the definition of unemployment is revised. The new definition is to a large extent similar to the earlier definition adopted by the Eighth Conference. It, however, introduces some amplifications and modifications concerning, in particular, the criteria of seeking work and current availability for work, the statistical treatment of persons temporary laid off, persons currently available for work but not actively seeking work, etc. The changes are aimed to make it possible to measure unemployment more accurately and more meaningfully both in developed and developing countries.

- GDP per capita (1960-2000). The data comes from Penn World Table 6.1.

- Saving rates with and without AIDS. We use data from Freire (2002).

4.2 Methodology

In this section, we present the forecasting methodology and the projection of HIV prevalence. The forecasting needed first the estimation of the parameters of an assumed econometric specification underlying the data generating process. For this purpose, we retain a Gaussian ARMA($p,q$) process for which we describe below the estimation and the forecasting procedure.\(^\text{10}\) Further details on these statistical methods can be found in Gouriéroux and Monfort (1990) and Hamilton (1994).

4.2.1 Estimation strategy

A Gaussian ARMA($p,q$) process is described as

\[
Y_t = \alpha + \phi_1 Y_{t-1} + \phi_2 Y_{t-2} + \cdots + \phi_p Y_{t-p} + u_t \\
+ \theta_1 u_{t-1} + \theta_2 u_{t-2} + \cdots + \theta_q u_{t-q} \quad t = 1, \cdots, T
\]  \hspace{1cm} (10)

where $u_t \sim i.i.d N(0, \sigma^2)$, and where the vector of population parameters $\theta = (\alpha, \phi_1, \phi_2, \cdots, \phi_p, \theta_1, \theta_2, \cdots, \theta_q, \sigma^2)'$ is to be estimated. The approximation to the likelihood function

\(^{10}\text{Prior to using the ARMA process, we have considered a more flexible forecasting AFRIMA (Fractional Integrated ARMA) framework: } AFRIMA(p,d,q), \text{ where } d \text{ is the degree of integration. Indeed, while proved to be a good alternative forecasting method, the ARMA approach has an inherent weakness against distinguishing between unit root non-stationarity and 'gradual' non-stationarity (i.e., between stationary and unit-root). Estimation results based on data at hand show that } d \approx 0, \text{ which turns out to be a typical ARMA process.}
is conditioned on both initial values of the $y$’s and $u$’s. Assuming that the initial values for $y_0 = (y_0, y_{-1}, \cdots, y_{-p+1})'$ and $u_0 = (u_0, u_{-1}, \cdots, u_{-p+1})'$ are given, the sequence $\{u_1, u_2, \cdots, u_T\}$ can be computed from $\{y_1, y_2, \cdots, y_T\}$ by iterating on

$$u_t = y_t - \alpha - \phi_1 y_{t-1} - \phi_2 y_{t-2} - \cdots - \phi_p y_{t-p} - \theta_1 u_{t-1} - \theta_2 u_{t-2} - \cdots - \theta_q u_{t-q} \quad t = 1, \cdots, T$$

(11)

The conditional log likelihood is given by:

$$L(\theta) = \ln f_{y_T, y_{T-1}, \cdots, y_1 | y_0, u_0} (y_T, y_{T-1}, \cdots, y_1 | y_0, u_0; \theta) = -\frac{T}{2} \ln(2\pi) - \frac{T}{2} \ln(\sigma^2) - \sum_{t=1}^{T} \frac{u_t^2}{2\sigma^2}$$

(12)

In maximizing this log likelihood, we set the initial $y$’s and $u$’s to their expected values. That is $y_s = \alpha/(1 - \phi_1 - \phi_2 - \cdots - \phi_p)$ for $s = 0, -1, \cdots, -p+1$, and $u_s = 0$ for $s = 0, -1, \cdots, -p+1$. Then, we proceed with iteration in (11) for $t = 1, \cdots, T$. We estimate a multiple $ARMA(p, q)$ model with $p = 2$ and $q = 2$ which turns out to be an estimate of six models. We finally select the model that optimizes the Schwarz Criterion. The selected model is used for forecasting purpose.

### 4.2.2 Forecasting

Now, consider forecasting the stationary and invertible $ARMA(p, q)$:

$$(1 - \phi_1 L - \phi_2 L^2 - \cdots - \phi_p L^p)(Y_t - \mu) = (1 + \theta_1 L + \theta_2 L^2 + \cdots + \theta_q L^q)u_t$$

(13)

where $L$ is the lag operator and $\mu$ is the unconditional mean $\mathbb{E}(Y_t)$. The one-period-ahead forecast ($s = 1$) is given by

$$(\hat{Y}_{t+1|t} - \mu) = \phi_1 (Y_t - \mu) + \phi_2 (Y_{t-1} - \mu) + \cdots + \phi_p (Y_{t-p+1} - \mu) + \theta_1 \hat{u}_t + \theta_2 \hat{u}_{t-1} + \cdots + \theta_q \hat{u}_{t-q+1}$$

(14)

with $\hat{u}$ generated recursively from $\hat{u} = Y_t - \hat{Y}_{t|t-1}$. Finally the $s$-period-ahead forecasts based on the Wiener-Kolmogorov prediction formula is

$$(\hat{Y}_{t+s|t} - \mu) = \begin{cases} 
\phi_1 (\hat{Y}_{t+s-1|t} - \mu) + \cdots + \phi_p (\hat{Y}_{t+s-p|t} - \mu) + \theta_s \hat{u}_t + \cdots + \theta_q \hat{u}_{t+s-q} & s = 1, \cdots, q \\
\phi_1 (\hat{Y}_{t+s-1|t} - \mu) + \cdots + \phi_p (\hat{Y}_{t+s-p|t} - \mu) & s = q + 1, \cdots 
\end{cases}$$

(15)

where $\hat{Y}_{t|t} = Y_t$ for $\tau \leq t$. 
4.2.3 Projection of HIV prevalence

To obtain the projected HIV prevalence, we fit a double logistic curve of the form

\[ p(t) = \frac{e^{\alpha(t-\tau)}}{1 + e^{\alpha(t-\tau)}} \left[ \frac{ae^{-\beta(t-\tau)}}{1 + e^{\beta(t-\tau)}} + b \right] \]  

(16)

where \( \alpha \) is the rate of increase at the start of the epidemic, \( a \) denotes the peak value, \( \beta \) is the rate of convergence, \( b \) is the final prevalence level and \( \tau \) shifts the whole curve backward. The value of \( \alpha \) is chosen so that the doubling time is 1.5 years. The latter is chosen so that the doubling time at the beginning of the epidemic can be \( \ln(2) / \alpha \). This means that \( \alpha = \ln(2) / 1.5 \).

As a result, for a given \( \beta \), we have to find (numerically) the parameters \( a, b \) and \( \tau \) solution of the nonlinear system

\[ \begin{align*}
S(a, b, \tau) &= \begin{cases}
p(0) = 0.1916 = \frac{e^{-\alpha \tau}}{1 + e^{-\alpha \tau}} \left[ \frac{ae^{-\beta \tau}}{1 + e^{-\beta \tau}} + b \right] \\
p(2015) = 0.194 = \frac{e^{\alpha(15-\tau)}}{1 + e^{\alpha(15-\tau)}} \left[ \frac{ae^{-\beta(15-\tau)}}{1 + e^{-\beta(15-\tau)}} + b \right] \\
\dot{p}(t) = 0 \iff \frac{e^{\alpha(t-\tau)}}{1 + e^{\alpha(t-\tau)}} \left[ \frac{ae^{-\beta(t-\tau)}}{1 + e^{-\beta(t-\tau)}} + b \right] = \frac{a\beta e^{-\beta(t-\tau)}}{1 + e^{-\beta(t-\tau)}} \] 
\end{cases}
\]  

(17)

where \( \dot{p}(t) = \frac{dp(t)}{dt} \). The first equation of the system corresponds to the starting period \((t = 0 \text{ for year 2000 where the prevalence is 0.1916})\), the second denotes the ending period \((t = 16 \text{ for year 2015 where the prevalence is 0.194})\) and the third equation expresses the peak of the epidemic. The value \( t = 3 \) represents the difference between the peak year 2003 and the starting date 2000.

5 Results of experiments

In this section we summarize our findings and provide a robustness check.

5.1 Selected forecasting results

Using the optimal forecasting procedure described above, we have generated several projections for the key variables of the model for time horizons approaching 2050.\(^\text{11}\) In order to save space, we only comment on the most important of them, those which will definitely matter in the interpretation of our findings.

\begin{figure}
\caption{Figures 1 to 5 here}
\end{figure}

\(^{11}\)In some cases, we use the procedure to extend previous forecasts available for shorter horizons to 2050. This is the case of saving rate forecasts, see Figures 3 and 4 below: Freire’s forecasts extend to 2015; we take as given and then we use the optimal forecasting procedure to go beyond 2015.
Criterion is optimized by and $ARMA(2, 0)$ for life expectancy at birth, and an $ARMA(1, 1)$ both for saving and GDP.\footnote{For example, the forecast of GDP at 2000 is used to compute the initial capital in the case without AIDS.} We can observe that the forecasts for life expectancy at birth with AIDS for female (Figure 1) and male (Figure 2) display nonlinear patterns. However, there is clear decreasing trend for both over the whole horizon, 1990 to 2050. The declining trend is indeed sizeable, and could not be omitted in any serious long-run analysis of AIDS. The forecast for saving without (Figure 3) and with AIDS (Figure 4) are very stable over time, after 2020. The confidence intervals are rather excellent for both. We shall notably observe here that the gap in saving rates between the AIDS and non-AIDS cases does not deepen tragically after 2020. It is about 2\% in 2015 and it is in average around 3\% after 2020. It is sizeable drop but our forecasts do not deliver any dramatic fall in savings, induced by AIDS, that one can \textit{a priori} fear given the multiple mechanisms undermining accumulation in such a situation. Finally note that GDP forecasts with or without AIDS (like in Figure 5 for the non-AIDS case) show a non-ambiguous increasing tendency. In particular, AIDS epidemics, while massive, is not likely to induce negative growth over long periods of time.

\begin{center} \textbf{Figures 6 to 8 here} \end{center}

We turn now to mortality and prevalence rates. Mortality shows up clearly in the declining patterns of the active population. Figure 6 is an example, it displays the forecasting of economically active population for females with AIDS. More clearly than any other forecast so far, the figure shows the dreadful long-run demographic impact of AIDS, a marked decline especially after 2020.

Figure 7 is a plot of HIV prevalence rate from 1980 to 2015 as constructed by the US Census Bureau. In order to obtain HIV prevalence projections, we first solve numerically the nonlinear system given by $S(a, b, \tau)$ for $a$, $b$ and $\tau$. We obtain $a = 0.4045$, $b = 0.0003$ and $\tau = -9.356$. These values are then plugged into relation (16) to determine HIV prevalence from 2016 to 2050. The result is provided in Figure 8. The scenario studied is therefore a continuous (but not very fast) decrease in this rate after 2015, which seems reasonable.

\section{5.2 The economic growth of AIDS quantified}

The most salient ingredients of the model are demographic. As explained just above, the heavy trends in mortality and life expectancy induced by AIDS will be definitely more dreadful after 2020. For example, the forecasted series of life expectancy at birth reach their trough around 2009, with about 44 years for both sexes, while the starting values are about 60 years. This aspect and other relevant demographic conditions are likely to induce a delayed effect of AIDS on economic growth. The channels are the size of active population in the medium-run (say between 2020 and 2040), and because we assume by (5) that life expectancy at birth is a determinant of individuals productivity at their working age, we are likely to get a delayed impact of AIDS on productivity, at least when the sensitivity of productivity to life expectancy (that is parameter
\( \beta \) is large enough. Actually the delayed effect turns out to be strong in all our simulations, as it transpires from the following figures for growth per capita when \( \beta \) varies from 0 to 1.\(^{13}\)

**Figure 9 to 10 here**

One can notice the following. First of all, whatever the value of \( \beta \), the gap between the AIDS and no-AIDS scenarios is rather stable between 2010 and 2020, but then it gets sharply larger between 2020 and 2030. The gaps keep increasing but at an apparently much lower pace between 2030 and 2040. Finally, the gap seems to be stable (or shrinks very slightly) after 2040. One can therefore extract at least three main qualitative conclusions from the simulations.

1. The demographic impact of AIDS has a clear delayed effect on economic growth, according to our simulations.

2. The most “dangerous” period for economic growth is the decade 2020-2030, where the gap between the AIDS and the non-AIDS scenarios gets deepened.

3. Though the gap does not increase so sharply after 2030, all our simulation feature a long run economic growth effect of AIDS.

Let us move now to a more quantitative assessment. To start with a benchmark case, let us consider a “linear” Ben-Porath case, that is \( \beta = 1 \). Table 1 gives the results for different values of the health expenditures productivity parameter \( \zeta \).

**Table 1 here**

Consider the case \( \zeta = 5 \) as in the benchmark considered by Corrigan et al. (2005). One can see that the gap in growth of GDP per capita does not move significantly between 2010 and 2020. From 2020 to 2030, the gap sharply moves from 0.89% to 2.78%, which translated in annual rates means that AIDS causes GDP per capita to decline by 0.19% in the period 2020-2030, while such a decline is around 0.09% in 2000-2010 for example. Accordingly, the economic growth impact of AIDS in 2020-2030 more than doubles its counterpart value over the decade 2000-2010. The gap keeps increasing from 2030 to 2040, it reaches 3.18% in 2040 but at a lower pace. Finally, the gap shrinks to 2.84% at 2050 mainly due to HIV-AIDS prevalence rates’ values at this horizon.

Our figures for the growth gaps are a bit lower than those put forward by Over (1992) for the ten most affected sub-Saharan Africa countries for the period 1990-2025. It is not fair to discuss here who has the most accurate estimate since all the set-ups developed to this end, including ours, have their own shortcomings and limitations. Most studies, like Over’s and ours, point at sizeable effects. In our case, the growth gap can be close to 0.2% for yearly growth \(^{13}\)

---

\(^{13}\)The growth rates reported in the figures are “cumulative” growth rates over the successive decades. In order to get an average annual growth rate over a given decade, one has to divide the associated growth rate registered during the decade by 10.
rate of GDP per capita, which is considerable. Our distinctive contribution is in the timing of the growth effect after the incorporation of the most likely medium and long-run demographic trends induced by AIDS (in the econometric sense of the expression “more likely”). According to our forecasts, the largest part of AIDS negative impact on economic growth is likely to take place between 2020 and 2030. Another striking finding is that the growth differential between the two scenarios tend to be almost stable from 2030 to 2050 featuring a kind of long-run effect of AIDS.

Incidentally our exercise shows that there might not be any conflict between the results obtained by authors like Bloom and Mahal (1997b), and others like Corrigan et al. (2005) or McDonald and Roberts (2006): A relatively short term assessment à la Bloom and Mahal might not reveal any dramatic AIDS growth effect, while a medium/long term perspective, relying on the evolution of the determinants of human capital accumulation, might deliver the opposite message. It seems reasonable to think that the observed sharply declining pattern of life expectancy must have delayed effects, and the governments should act from now on to alleviate the expected effects of such a trend.

5.3 Robustness check

We conduct two kinds of sensitivity analysis. First, we allow the coefficient $\beta$ to vary taking the values 0, 1/7, 1/5, 1/2 and 1. The second sensitivity analysis concerns function $\Phi(m(t))$ (relation 9). We allow $\zeta$ to vary from 1 to 10 for each value of $\beta$. The results are given in the tables below.

| Tables 2 to 6 here |

A first conclusion should be that the variation of parameter $\zeta$ of the health expenditures function does not change generally the first two decimals of the obtained growth per capita gap figures. The same type of findings is reported by Corrigan et al. (2005). Much more importantly, and not surprisingly, the gap figures increase with the sensitivity parameter $\beta$. A comparison between the polar cases $\beta = 0$ and $\beta = 1$ is useful to dig deeper in the findings. In the first case (and $\zeta = 5$), the gap jumps from 0.65 percentage point in 2020 to 2.65 percentage points in 2030, rises slightly to 2.87 in 2040, before coming back to the 2030 level in 2050. When $\beta = 1$, the size of the jump between 2020 and 2030 is naturally bigger, but the difference is even larger in 2040: the difference between the two gaps is about 0.13 in 2030, it is more than the double (equal to 0.31) in 2040. Therefore, while the fall in active population is probably, and by far, the main factor behind AIDS impact on economic growth during the decade 2020-2030, the Ben-Porath mechanism seems more relevant in the posterior decade. Both demographic factors are consequently key to understand the medium and long-run economic growth effects of AIDS in our scenarios, contrary to physical capital accumulation which does not seem to be the main story for these time horizons.
6 Conclusion

In this paper, we have first reviewed the main aspects of the empirical debate on the economic growth impact of epidemics. More specifically, we have focused on the debate on AIDS/HIV impact. We have shown how this debate is actually extremely disputed. A view however emerges according to which the loss in human capital might be truly devastating for long-run growth. We develop a simple general equilibrium model extending previous work by Cuddington and Hancock (1994). In particular, the sharply declining life expectancy patterns are clearly reflected in the enlarged model in the production function through a generic Ben-Porath mechanism (shorter lives imply shorter schooling times and therefore lower labor productivity). AIDS-related health expenditures are incorporated as well. Applied to the South African case, the model enhances the following aspect: while a relatively short term assessment might not reveal any dramatic AIDS growth effect, the medium/long run impact can be truly sizeable.

Our main contribution is to put forward a reasonable timing for the economic growth impact of AIDS under some widely accepted demographic scenarios. We first point out that the demographic impact of AIDS has a clear delayed effect on economic growth. Therefore, there might not be any fundamental conflict between the results obtained by authors like Bloom and Mahal (1997b), and others like Corrigan et al. (2005): A relatively short term assessment à la Bloom and Mahal (1997b) might not reveal any dramatic AIDS growth effect, while a long term perspective, relying on the evolution of key demographic variables like mortality and life expectancy, might yield just the contrary. Second, we show that the most “dangerous” period for economic growth is the decade 2020-2030, where the gap between the AIDS and the non-AIDS scenarios gets deepened. Finally, though the gap does not increase so sharply after 2030, all our simulation feature a long run economic growth effect of AIDS.

Acknowledgements

We would like to thank Matteo Cervellati, Miguel Perez-Nievas, Noel Bonneuil, Frédéric Dufourt, Frédéric Docquier and Vladimir Veliov for helpful comments on previous versions of this paper. Raouf Boucekkine acknowledges the support of the Belgian research programmes ‘Pôles d’Attraction interuniversitaires’ PAI P5/21, and ‘Action de Recherches Concertée’ ARC on sustainability. The usual disclaimer applies.

References


Table 1: Growth rates (in %) of GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 1$

<table>
<thead>
<tr>
<th>Year</th>
<th>$\zeta = 1$</th>
<th>$\zeta = 2.5$</th>
<th>$\zeta = 5$</th>
<th>$\zeta = 10$</th>
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<td>2020</td>
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Table 2: Growth rates (in %) of GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 1/2$

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Table 3: Growth rates (in %) of GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 1/5$

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<td>2.69</td>
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### Table 4: Growth rates (in %) of GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 1/7$

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### Table 5: Growth rates of both GDP and GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 1/10$

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### Table 6: Growth rates (in %) of GDP per capita: gap between the AIDS and no-AIDS scenarios for varying the health productivity parameter $\zeta$ for $\beta = 0$

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Figure 1: Forecasting of life expectancy at birth, female
Figure 2: Forecasting of life expectancy at birth, male
Figure 3: Forecasting of saving without AIDS based on Freire (2002)
Figure 4: Forecasting of saving with AIDS based on Freire (2002)
Figure 5: Forecasting of GDP without AIDS
Figure 6: Forecasting of economically active population with AIDS, female
Figure 7: HIV prevalence in percent 1988-2015

Figure 8: HIV prevalence 2016-2050
Figure 9: GDP growth rate per capita with and without AIDS
Figure 10: GDP growth rate per capita with and without AIDS: polar cases ($\beta = 0$ and $\beta = 1$)