Financial crises are supposed to be rare events, yet they occur quite often. According to Reinhart and Rogoff (2009), investors suffer from “this time is different” syndrome, failing to see crises coming because they do not recognize similarities among the different pre-crisis bubbles. As a result, each crisis surprises investors.

Economists typically model financial crises as responses to shocks to which investors attach a low probability ex ante, but which nonetheless materialize. Such shocks (sometimes referred to as “MIT shocks”; e.g., Caballero and Simsek 2013) are consistent with rational expectations in that investors recognize that there is a small chance that the shock might occur, but they are harder to reconcile with the Reinhart Rogoff observation that crises are not that unusual.

The 2008 financial crisis in the US has deepened the challenge, by bringing up direct evidence that investor appreciation of the risks was not entirely rational. Coval, Jurek, and Stafford (2009) show that investors underestimated the probability of mortgage defaults in pricing mortgage backed securities. Foote, Gerardi, and Willen (2012) present direct evidence that investors did not even contemplate the magnitude of home price declines that actually materialized. Rather than being considered unlikely, the risks appear to have been entirely neglected. This evidence is part of a growing body

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1 Universita’ Bocconi and IGIER, Harvard University, and University of Chicago, respectively. Gennaioli thanks the European Research Council (Starting Grant #241114) for financial support.
of research showing that investor expectations are typically extrapolative rather than rational (Greenwood and Shleifer 2014). What we lack is a theory of beliefs consistent with sharp underestimates of the odds of a crisis.

In this paper, we present a psychological theory of the neglect of risk and the financial crises. The theory seeks to explain precisely why the probability estimates of a crisis in the middle of a boom are too low, offering a foundation of “unanticipated” shocks, and of zero probabilities attached to some states of the world by investors (Gennaioli, Shleifer, and Vishny 2012). Our theory yields boom-bust financial crises based entirely on beliefs; we do not incorporate into the model any economic mechanisms that magnify the shocks, such as fire sales or imperfect capital markets.

The theory we present is based on Kahneman and Tversky’s (1972) idea of representativeness, as previously modeled by Barberis, Shleifer, and Vishny (1998), Gennaioli and Shleifer (2010), and Bordalo, Gennaioli, and Shleifer (2014). In our model, representativeness induces people to over-estimate the probability of outcomes that are relatively more likely in light of recently observed data. Representativeness is intimately related to the idea of similarity: after seeing some data, people concentrate their forecasts on outcomes similar to the data observed, neglecting alternative future paths.

This principle has far-reaching implications for finance. After observing a string of good news (internet stocks, housing prices), an investor views them as being generated by a favorable economic scenario. A series of good news is similar to a continuing boom. The investor then puts too much probability weight on that scenario and neglects the risk of bad outcomes. If investor expectations are elicited at this point, they look extrapolative.
Observing some bad news intermixed with good news does not change the investor’s mind. He views the few bad news as an aberration and under-reacts. Only after a string of unfavorable news the bad outcome becomes sufficiently more likely that the representative scenario changes from boom to bust. A pattern of sufficiently dramatic or continuing bad news is similar to the low payoff state, leading to a change in the underlying beliefs. Previously ignored bad news is remembered, leading to a sharp rise in the perceived probability of a crisis and a collapse of prices. The investor now overreacts to the bad news, especially if the true probability of the low state remains low. The possibility of black swans is initially ignored, but ultimately turns into an overstated fear that leads to a self-generating crisis. In contrast to rational expectations, the model yields purely belief-driven boom-bust cycles.

The Model

There is one asset, such as a mortgage, and one investor. The cash flow of the asset, received at the very end, is a random variable taking values in $Y \equiv \{y_h, y_l\}$, where $y_h > y_l$. There are three periods $t = 0, 1, 2$, and the investor receives bits of news about the final payoff between periods. The investor learns about the cash flow distribution based on bits of good and bad news he receives (the news could be viewed as payoff realizations of similar assets). At $t = 0$, the investor’s prior expected probability of $y_k$ is $\pi^0_k$, with $\pi^0_h > \pi^0_l$. We do not think of either state as extremely unlikely, although good times are more common than bad. At time $t$, after observing a sample of $(n_h, n_l)$ bits of good and bad news, a Bayesian investor would update the posterior expected probability
of $y_k$ to $\pi_k^t = (\pi_k^0 + n_k)/(1 + n_h + n_t)$. This updating rule obtains if the prior distribution over $(\pi_h, \pi_l)$ is Dirichlet with parameters $(\pi_h^0, \pi_l^0)$.

At $t = 1$, debt is issued to the investor against the asset’s cash flow. Issuers maximize profits. The investor is assumed to be risk neutral as long as the expected default probability is below $\rho$, but infinitely risk averse if the expected probability of default is higher than $\rho$, where $\rho < \pi_l^0$. This discontinuity in risk bearing capacity may reflect an institutional constraint facing the investor, such as a value-at-risk constraint.

To see what happens in a boom, assume that, between $t = 0$ and $t = 1$, a string of $n_h^0$ good draws is observed, and no bad news. By Bayesian updating, the expected probability of state $h$ at $t = 1$ is $\pi_h^1 = \frac{\pi_h^0 + n_h^0}{1 + n_h^0} > \pi_h^0$. To make our points, we assume:

A.1 $\rho < \pi_h^1$.

Good news increases the expected probability of a good state, but not enough to make it tolerable for investors to bear default risk in the low state $y_l$. We then have:

**Lemma 1** (rational benchmark) Under A.1, observation of $n_h^0$ bits of good news, the amount of debt issued at $t = 1$ and its price are $d_1 = p(d_1) = y_l$.

A moderate amount of good news does not change the Bayesian posterior enough. As a consequence, the amount of debt issued and its value do not change relative to what would in principle have happened at $t = 0$ if debt were issued then. The rational expectations funding policy is very conservative. This (low) amount of debt is completely information insensitive, so its price does not change at $t = 2$ either.
The Boom Under Thinking through Representativeness

In contrast to the rational benchmark, consider the case in which, as in Gennaioli, Shleifer, and Vishny (2012, 2013), investors inflate the probability of cash flow realizations that more easily come to mind. As in Gennaioli and Shleifer (2010), we assume that belief formation is guided by representativeness. In particular, what is representative at time $t$ depends on a comparison with the past, $t - 1$.

**Definition 1** At time $t$, the representativeness of cash flow $y_k$ is formally defined as:

$$ R(y_k, t) = \frac{\pi_k^t}{\pi_k^{t-1}}. $$

Investors then deflate by a factor $\delta \in [0,1]$ the odds of the less representative cash flow. Equally representative cash flows are deflated by the same factor.

Representativeness maps reality into what investors are thinking about. The most representative cash flow at $t$ is the one whose probability exhibits the largest percentage increase in light of the data. The probability of this cash flow is inflated relative to the less representative one (but probabilities still add up to one). The intuition is that investors weigh recent data too much in their assessments.

Parameter $\delta$ captures the severity of the distortion of probabilities. When $\delta = 0$, investors only think about the most representative cash flow, forgetting the other. This case corresponds to a complete neglect of risk, as in Gennaioli, Shleifer, and Vishny.

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2 Kahneman and Tversky (1972) write that “an attribute is representative of a class is it is very diagnostic; that is, if the relative frequency of this attribute is much higher in that class than in a relevant reference class”. In line with this definition, our model specifies that a cash flow realization is representative of a sequence of data if such realization becomes relatively much more frequent after the data are observed.
(2012). When $\delta = 1$, investors hold rational expectations. For intermediate $\delta$'s, investors overestimate the likelihood of representative states.

Consider now the implications of this logic. Consider first a stable situation in which no updating occurs and the distribution $\pi_k^0$ is always the same as $\pi_k^0$. By Equation (1), in this case all cash flows are equally representative, since $R(y_k, t) = \pi_k^0 / \pi_k^0 = 1$. Even under representativeness, then, the rational benchmark $d_1^r = p^r(d_1^r) = y_l$ obtains.

Consider what happens in a boom under representativeness. Now, observing $n_h^0$ bits of good news exerts a more drastic effect on beliefs than under rational expectations. Under representativeness, this news does not just upgrade the probability of the high cash flow state, but it also renders such state representative. The following result holds:

**Proposition 1** Under representativeness, after observing $n_h^0$ pieces of good news the beliefs $\pi_k^{r,1}$ of investors at $t = 1$ are distorted in favor of higher cash flows:

$$
\pi_k^{r,1} = \frac{(\pi_h^0 + n_h^0)}{(\pi_h^0 + n_h^0) + \pi_l^0 \delta} > \pi_k^1,
$$

$$
\pi_l^{r,1} = \frac{\pi_l^0 \delta}{(\pi_h^0 + n_h^0) + \pi_l^0 \delta} < \pi_l^1,
$$

where $\pi_k^1$ is the Bayesian posterior. If $\delta$ is small enough, after observing $n_h^0$ bits of good news the debt issued at $t = 1$ and its price are $d_1^r = y_h$, $p^r(d_1^r) = y_h - \pi_l^{r,1}(y_h - y_l)$.

When the investor assesses risk by representativeness, he overreacts to good news. Good news increases the probability of $y_h$, but the investor extrapolates too much from this favorable change. As a result, he downplays the probability of $y_l$ which facilitates greater debt issuance at higher prices. If $\delta \rightarrow 0$ these effects are so strong that debt is viewed as absolutely safe, so its price equals the maximum $p^r(d_0^r) = y_h$. 


Although investors fail to fully anticipate the risk of losses, they do so not because losses occur with a low probability. In fact, the loss state $y_l$ may be quite likely. Losses are neglected because they are not representative of the good news that market participants have observed. This is a form of “this time is different syndrome”: the good news creates too much faith in good fundamentals, which leads to neglect of risk and excessive debt issuance. Extrapolation of good times and the neglect of downside risk are part of the same psychological mechanism of representativeness.

This mechanism highlights two major differences between this psychologically founded model and the canonical “unanticipated shock”. First, markets will get exposed to the risk of losses rather frequently: even relatively likely outcomes such as $y_l$ may be neglected. Second, the risks that get neglected endogenously depend on actual fundamental changes and news. This is a testable implication.

**The Bust under Thinking Through Representativeness**

Another key difference between the psychology of neglected risks and the canonical “unanticipated shock” is how crises unfold. Under representativeness, a few disappointing bits of data intermixed with good news are not enough for neglected risks to become salient. Enough bad news must accumulate for the bad scenario to become representative. As a consequence, investors initially under-react to bad news, but when enough bad news accumulates, investors over-react because their representation changes, causing them to overestimate the probability of the low state. There is an exact parallel here between the psychology of booms and busts.
To see how this works, suppose that after \( t = 1 \) a number \( n_t^1 \) of low realizations is observed intermixed with \( n_h^1 \) of good realizations, so that the news sample at \( t = 1 \) is \((n_t^1, n_h^1)\). At \( t = 2 \), then, the market beliefs \( \pi^{r,2} \) and outcomes are:

**Proposition 2 (Under and over reaction)** Suppose that psychological biases are severe, namely \( \delta \to 0 \). Then the market reacts to news \((n_t^1, n_h^1)\) as follows:

1) If \( n_t^1 / n_h^1 < \pi^0 / (\pi_h^0 + n_h^0) \), the market neglects the bad news and still believes that debt is perfectly safe, namely \( \pi^{r,2} = 1 \) and \( p^r(d^1) = y_h \).

2) If \( n_t^1 / n_h^1 < \pi^0 / (\pi_h^0 + n_h^0) \), the market over-reacts to the bad news. It now believes that \( y_i \) occurs with probability 1, namely \( \pi^{r,2} = 1 \) and \( p^r(d_0^i) = y_l \).

This result is particularly stark due to the extreme assumption \( \delta \to 0 \), but it brings out our main points. First, provided only a few bits of bad news are observed, investors disregard them, and continue to extrapolate from the more representative good news. Second, after sufficiently many bits of bad news are observed, the low state with large losses on debt becomes representative. At this point, investors discard the good news as mere instances of chance and exaggerate the likelihood of future losses. Investors become pessimistic according to the same psychology that caused euphoria at \( t = 1 \).

In Proposition 2, low probability outcomes require relatively few observations to become representative (formally \( n_t^1 \) can be low precisely when \( \pi^0 \) is low). Bad news episodes are dangerous because they very quickly change representation, not because of the objective (and unlikely) consequences they bring about. More generally, representativeness can cause large swings in confidence and thus in market outcomes in response to news, increasing volatility relative to rational expectations.
Conclusion

We have outlined a psychological model of beliefs in financial markets in which investors attach excessive probabilities to states of the world that are representative for the news they observe. In this model, optimism and pessimism are outcomes of the same psychological mechanisms. The very simple model yields several results.

First, it explains how moderate probability events are first neglected, but then exaggerated when news pattern becomes consistent with them. It thus accounts for “this time is different” phenomenon without recourse to low probability shocks.

Second, it provides a unified psychological interpretation of neglect of risk and extrapolation that have been seen as central to the accounts of boom and bust cycles. This framework also allows for thinking about under- and over-reaction to information that has been a central set of phenomena in behavioral finance, but has not yet been obtained with a unified psychological model (see Barberis, Shleifer, and Vishny 1998).

Third, it explains how boom and bust cycles in debt valuation and issuance can arise purely through volatility in expectations, even without standard economic mechanisms of magnification.

Obviously we have presented a very rudimentary version of this analysis, and much remains to be done. Yet the objective of having a unified psychological model of various aspects of financial instability appears a little closer.
References


