## ONLINE APPENDIX FOR:

# "Knowledge of Future Job Loss and Implications for Unemployment Insurance" 

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## A No Trade Condition

This section provides a more formal exposition of the no trade condition in Section 4. To provide a general treatment, I begin by relaxing the condition of uni-dimensional heterogeneity in the population. Individuals are indexed by a heterogeneity parameter, $\theta$, and make choices $\left\{c_{p r e}(\theta), c_{u}(\theta), c_{e}(\theta), a(\theta), p(\theta)\right\} \in \Omega_{\theta}$, where the constraint set varies arbitrarily across types.

Consider a policy that provides a small payment, $d b$, in the event of losing one's job that is financed with a small payment in the event of remaining employed, $d \tau$, offered to those with observable characteristics $X$. By the envelope theorem, the utility impact to type $\theta$ of buying such a policy will be given by

$$
d U=-(1-p(\theta)) v^{\prime}\left(c_{e}(\theta)\right) d \tau+p(\theta) u^{\prime}\left(c_{u}(\theta)\right) d b
$$

which will be positive if and only if

$$
\begin{equation*}
\frac{p(\theta) u^{\prime}\left(c_{u}(\theta)\right)}{(1-p(\theta)) v^{\prime}\left(c_{e}(\theta)\right)} \geq \frac{d \tau}{d b} \tag{21}
\end{equation*}
$$

The LHS of equation (21) is a type $\theta$ 's willingness to pay (i.e. marginal rate of substitution) to move resources from the event of remaining employed to the event of job loss. ${ }^{47}$ The RHS of equation (21), $\frac{d \tau}{d b}$, is the cost per dollar of benefits of the insurance policy.

Let $\bar{\Theta}\left(\frac{d \tau}{d b}\right)$ denote the set of all individuals, $\theta$, who prefer to purchase the additional insurance at price $\frac{d \tau}{d b}$ (i.e. those satisfying equation (21)). An insurer's profit from a type $\theta$ is given by $(1-p(\theta)) \tau-p(\theta) b$. Hence, the insurer's marginal profit from trying to sell a policy with price $\frac{d \tau}{d b}$ is given by

$$
d \Pi=\underbrace{E\left[1-p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right] d \tau}_{\text {Premiums Collected }}-\underbrace{E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right] d b}_{\text {Benefits Paid }}-\underbrace{\left(d E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]\right)(\tau+b)}_{\text {Moral Hazard }}
$$

The first term is the amount of premiums collected, the second term is the benefits paid out, and the third term is the impact of additional insurance on its cost. If more insurance increases the probability of job loss, $d E[p(\theta)]>0$, then it reduces premiums collected, $\tau$, and increases benefits paid, $b .^{48}$

However, for the first dollar of insurance when $\tau=b=0$, the moral hazard cost to the insurer is zero. This insight, initially noted by Shavell (1979), suggests moral hazard does not affect whether insurers' first dollar of insurance is profitable - a result akin to the logic that deadweight loss varies with the square of the tax rate.

The first dollar of insurance will be profitable if and only if

$$
\begin{equation*}
\frac{d \tau}{d b} \geq \frac{E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]}{E\left[1-p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]} \tag{22}
\end{equation*}
$$

[^0]If inequality (22) does not hold for any possible price, $\frac{d \tau}{d b}$, then providing private insurance will not be profitable at any price. Under the natural assumption ${ }^{49}$ that profits are concave in $b$ and $\tau$, the inability to profitably sell a small amount of insurance also rules out the inability to sell larger insurance contracts.

Equation (22) characterizes no trade under an arbitrary dimensionality of unobserved heterogeneity, $\theta$. To provide a clearer expression of how demand relates to underlying fundamentals, such as marginal rates of substitution and beliefs, it is helpful to impose a dimensionality reduction on the unobserved heterogeneity.
Assumption A1. (Uni-dimensional Heterogeneity) Assume the mapping $\theta \rightarrow p(\theta)$ is $1-1$ and continuously differentiable in $b$ and $\tau$ in an open ball around $b=\tau=0$. Moreover, the marginal rate of substitution, $\frac{p}{1-p} \frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}$, is increasing in $p$.

Assumption A1 states that the underlying heterogeneity can be summarized by ones' belief, $p(\theta)$. In this case, the adverse selection will take a particular threshold form: the set of people who would be attracted to a contract for which type $p(\theta)$ is indifferent will be the set of higher risks whose probabilities exceed $p(\theta)$. Let $P$ denote the random variable corresponding to the distribution of probabilities chosen in the population in the status quo world without a private unemployment insurance market, $b=\tau=0 .{ }^{50}$ And, let $c_{u}(p)$ and $c_{e}(p)$ denote the consumption of types $p(\theta)$ in the unemployed and employed states of the world. Under Assumption A1, equation (22) can be re-written as:

$$
\begin{equation*}
\frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)} \leq T(p) \quad \forall p \tag{23}
\end{equation*}
$$

where $T(p)$ is the pooled price ratio defined in Hendren (2013):

$$
T(p)=\frac{E[P \mid P \geq p]}{E[1-P \mid P \geq p]} \frac{1-p}{p}
$$

The market can exist only if there exists someone who is willing to pay the markup imposed by the presence of higher risk types adversely selecting her contract. Here, $\frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}-1$ is the markup individual $p$ would be willing to pay and $T(p)-1$ is the markup that would be imposed by the presence of risks $P \geq p$ adversely selecting the contract. This suggests the pooled price ratio, $T(p)$, is the fundamental empirical magnitude desired for understanding the frictions imposed by private information.

The remainder of this Appendix further discusses the generality of the no trade condition. A. 1 discusses multidimensional heterogeneity. Appendix A. 2 also discusses the ability of the firm to potentially offer menus of insurance contracts instead of a single contract to screen workers. Appendix A. 3 illustrates that while in principle the no trade condition does not rule out non-marginal insurance contracts (i.e. $b$ and $\tau>0$ ), in general a monopolist firm's profits will be concave in the size of the contract; hence the no trade condition also rules out larger contracts.

## A. 1 Multi-Dimensional Heterogeneity and Robustness to Outlier Willingness to Pay

In reality, there are many reasons beyond one's chance of job loss that drive differences in willingness to pay. To understand the impact of multidimensional heterogeneity, this section solves for the no-trade condition in the case where there is an (unbounded) distribution of $\frac{u^{\prime}\left(c_{u}(\theta)\right)}{v^{\prime}\left(c_{e}(\theta)\right)}$ among the set of those with the same risk type, $p(\theta)$. In this case, there is heterogeneous willingness to pay for additional UI for different types $\theta$ with the same $p(\theta)$.

I show that there exists a mapping, $f(p): A \rightarrow \Theta$, that maps $A \subset[0,1]$ into the interior of the type space, $\Theta$, such that the no trade condition reduces to testing

$$
\begin{equation*}
\frac{u^{\prime}\left(c_{u}(f(p))\right)}{u^{\prime}\left(c_{e}(f(p))\right)} \leq T(p) \quad \forall p \tag{24}
\end{equation*}
$$

In this sense, even though some types are willing to pay an unboundedly high amount for UI, their extreme willingness to pay does not directly affect the no trade condition. Rather, one needs to search through an interior subset of the type space. Hence, if there are sufficiently many people of risk type $p$ with very high willingness to pay, then one would expect the type $f(p)$ to be willing to pay the pooled cost of worse risks, so that equation (24) will not hold. But, the results illustrate that a simple addition of individuals with outlier willingness to pay for UI will not open up a market unless there are sufficiently many other types with the similar risk type that are also willing to pay the pooled cost of worse risks.

[^1]I prove this result as follows. First, I assume for simplicity that the distribution of $p(\theta)$ has full support on $[0,1]$ and the distribution of $\frac{u^{\prime}\left(c_{u}(\theta)\right)}{v^{\prime}\left(c_{e}(\theta)\right)}$ has full support on $[0, \infty)$ (this is not essential, but significantly shortens the proof - note this allows for some individuals with unboundedly high willingness to pay). Now, fix a particular policy, $\frac{d \tau}{d b}$, and consider the set of $\theta$ that are willing to pay for this policy:

$$
E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]
$$

Without loss of generality, there exists a function $\tilde{p}\left(\frac{d \tau}{d b}\right)$ such that

$$
E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]=E\left[p(\theta) \left\lvert\, p(\theta) \geq \tilde{p}\left(\frac{d \tau}{d b}\right)\right.\right]
$$

so that the average probability of the types selecting $\frac{d \tau}{d b}$ is equal to the average cost of all types above $\tilde{p}\left(\frac{d \tau}{d b}\right)$. Without loss of generality, one can assume that $\tilde{p}$ is strictly increasing in $\frac{d \tau}{d b}$ so that $\tilde{p}^{-1}$ exists. ${ }^{51}$

I construct $f(p): A \rightarrow \Theta$ as follows. Define $A$ to be the range of $\tilde{p}$ when taking values of $\frac{d \tau}{d b}$ ranging from 0 to $\infty$. For each $p$, define $f(p)$ to be a value(s) of $\theta$ such that the willingness to pay equals $\tilde{p}^{-1}(p)$ :

$$
\frac{p}{1-p} \frac{u^{\prime}\left(c_{e}(f(p))\right)}{v^{\prime}\left(c_{u}(f(p))\right)}=\tilde{p}^{-1}(p)
$$

Now, suppose $\tilde{p}^{-1}(p) \leq T(p)$ for all $p$. One needs to establish that inequality (22) does not hold for any $\frac{d \tau}{d b}$ :

$$
\frac{d \tau}{d b} \leq \frac{E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]}{E\left[1-p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]}
$$

To see this, note that

$$
\frac{E\left[p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]}{E\left[1-p(\theta) \left\lvert\, \theta \in \bar{\Theta}\left(\frac{d \tau}{d b}\right)\right.\right]}=\frac{E\left[p(\theta) \left\lvert\, p(\theta) \geq \tilde{p}\left(\frac{d \tau}{d b}\right)\right.\right]}{1-E\left[p(\theta) \left\lvert\, p(\theta) \geq \tilde{p}\left(\frac{d \tau}{d b}\right)\right.\right]}
$$

so that we wish to show that

$$
\begin{equation*}
\frac{E\left[p(\theta) \left\lvert\, p(\theta) \geq \tilde{p}\left(\frac{d \tau}{d b}\right)\right.\right]}{1-E\left[p(\theta) \left\lvert\, p(\theta) \geq \tilde{p}\left(\frac{d \tau}{d b}\right)\right.\right]} \geq \frac{d \tau}{d b} \tag{25}
\end{equation*}
$$

for all $\frac{d \tau}{d b}$. Note that the set $A$ is generated by the variation in $\frac{d \tau}{d b}$, so that testing equation (25) is equivalent to testing this equation for all $p$ in the range of $A$ :

$$
\frac{E[p(\theta) \mid p(\theta) \geq p]}{1-E[p(\theta) \mid p(\theta) \geq p]} \geq \tilde{p}^{-1}(p) \quad \forall p \in A
$$

which is equivalent to

$$
\frac{E[p(\theta) \mid p(\theta) \geq p]}{1-E[p(\theta) \mid p(\theta) \geq p]} \geq \frac{p}{1-p} \frac{u^{\prime}\left(c_{e}(f(p))\right)}{v^{\prime}\left(c_{u}(f(p))\right)} \quad \forall p \in A
$$

which proves the desired result.
Intuitively, it is sufficient to check the no trade condition for the set of equivalent classes of types with the same willingness to pay for $\frac{d \tau}{d p}$. Within this class, there exists a type that one can use to check the simple uni-dimensional no trade condition.

## A. 2 Robustness to Menus

Here, I illustrate how to nest the model into the setting of Hendren (2013), then apply the no trade condition in Hendren (2013) to rule out menus in this more complex setting with moral hazard. I assume here that there are no additional choices, $a$, other than the choice $p$, although the presence of such additional choices should not alter the proof as long as they are not observable to the insurer. With this simplification, the only distinction relative to Hendren (2013) is the introduction of the moral hazard problem in choosing $p$. This section shows that allowing $p$ to be a choice doesn't make trade any easier than in a world where $p(\theta)$ is exogenous and not affected by the insurer's contracts; hence the no trade condition results from Hendren (2013) can be applied to rule out menus.

[^2]I consider the maximization program of a monopolist insurer offering a menu of insurance contracts. Whether there exists any implementable allocations other than the endowment corresponds to whether there exists any allocations other than the endowment which maximize the profit, $\pi$, subject to the incentive and participation constraints.

Without loss of generality, the insurer can offer a menu of contracts to screen types, $\{\nu(\theta), \Delta(\theta)\}_{\theta \in \Gamma}$ where $\nu(\theta)$ specifies a total utility provided to type $\theta, v(\theta)=p(\theta) u\left(c_{u}(\theta)\right)+(1-p(\theta)) v\left(c_{e}(\theta)\right)-\Psi(p ; \theta)$, and $\Delta(\theta)$ denotes the difference in utilities if the agent becomes unemployed, $\Delta(\theta)=u\left(c_{u}(\theta)\right)-v\left(c_{e}(\theta)\right)$. Note that $\nu(\theta)$ implicitly contains the disutility of effort.

Given the menu of contracts offered by the insurer, individuals choose their likelihood of unemployment. Let $\hat{q}(\Delta, \theta)$ denote the choice of probability of employment for a type $\theta$ given the utility difference between employment and unemployment, $\Delta$, so that the agent's effort cost is $\Psi(\hat{q}(\Delta ; \theta) \theta)$. Note that a type $\theta$ that accepts a contract containing $\Delta$ will choose a probability of employment $\hat{q}(\Delta ; \theta)$ that maximizes their utility. I assume that $\hat{q}$ is weakly increasing in $\Delta$ for all $\theta$.

Let $C_{u}(x)=u^{-1}(x)$ and $C_{e}(x)=v^{-1}(x)$ denote the consumption levels required in the employed and unemployed state to provide utility level $x$. Let $\pi(\Delta, \nu ; \theta)$ denote the profits obtained from providing type $\theta$ with contract terms $\nu$ and $\Delta$, given by

$$
\pi(\Delta, \nu ; \theta)=\hat{q}(\Delta ; \theta)\left(c_{e}^{e}-C_{e}(v-\Psi(\Delta ; \theta))\right)+(1-\hat{q}(\Delta ; \theta))\left(c_{u}^{e}-C_{u}(\nu-\Delta-\Psi(\Delta ; \theta))\right)
$$

Note that the profit function takes into account how the agents' choice of $p$ varies with $\Delta$.
Throughout, I maintain the assumption that profits of the monopolist are concave in $(\nu, \Delta)$. Such concavity can be established in the general case when $u$ is concave and individuals do not choose $p$ (see Hendren (2013)). But, allowing individuals to make choices, $p$, introduces potential non-convexities into the analysis. However, it is natural to assume that if a large insurance contract would be profitable, then so would a small insurance contract. In Section A. 3 below, I show that global concavity of the firm's profit function follows from reasonable assumptions on the individuals' utility function. Intuitively, what ensures global concavity is to rule out a case where small amounts of insurance generate large increases in marginal utilities (and hence increase the demand for insurance).

I prove the sufficiency of the no trade condition for ruling out trade by mapping it into the setting of Hendren (2013). To do so, define $\tilde{\pi}(\nu, \Delta ; \theta)$ to be the profits incurred by the firm in the alternative world in which individuals choose $p$ as if they faced their endowment (i.e. face no moral hazard problem). Now, in this alternative world, individuals still obtain total utility $\nu$ by construction, but must be compensated for their lost utility from effort because they can't re-optimize. But, note this compensation is second-order by the envelope theorem. Therefore, the marginal profitability for sufficiently small insurance contracts is given by

$$
\pi(\nu, \Delta ; \theta) \leq \tilde{\pi}(\nu, \Delta ; \theta)
$$

Now, define the aggregate profits to an insurer that offers menu $\{\nu(\theta), \Delta(\theta)\}_{\theta}$ by

$$
\Pi(\nu(\theta), \Delta(\theta))=\int \pi(\nu(\theta), \Delta(\theta) ; \theta) d \mu(\theta)
$$

and in the world in which $p$ is not affected by $\Pi$,

$$
\tilde{\Pi}(\nu(\theta), \Delta(\theta))=\int \pi(\nu(\theta), \Delta(\theta) ; \theta) d \mu(\theta)
$$

So, for small variations in $\nu$ and $\Delta$, we have that

$$
\Pi(\nu(\theta), \Delta(\theta)) \leq \tilde{\Pi}(\nu(\theta), \Delta(\theta))
$$

$\underset{\tilde{I}}{ }$ because insurance causes an increase in $p$. Now, Hendren (2013) shows that the no trade condition implies that $\tilde{\Pi} \leq 0$ for all menus, $\{\nu(\theta), \Delta(\theta)\}$. Therefore, the no trade condition also implies $\Pi \leq 0$ for local variations in the menu $\{\nu(\theta), \Delta(\theta)\}$ around the endowment. Combining with the concavity assumption, this also rules out larger deviations.

Conversely, if the no trade condition does not hold, note that the behavioral response is continuous in $\Delta$, so that sufficiently small values of insurance allow for a profitable insurance contract to be traded.

## A. 3 Concavity Assumption and Sufficient Conditions for Concavity

The presence of moral hazard in this multi-dimensional screening problem induces the potential for non-convexities in the constraint set. Such non convexities could potentially limit the ability of local variational analysis to characterize the set of implementable allocations. To be specific, let $\pi(\Delta, \mu ; \theta)$ denote the profit obtained from type $\theta$ if she is provided with total utility $\mu$ and difference in utilities $\Delta$,

$$
\pi(\Delta, \mu ; \theta)=(1-\hat{p}(\Delta ; \theta))\left(c_{e}^{e}-C_{v}(\mu-\Psi(1-\hat{p}(\Delta ; \theta)))\right)+\hat{p}(\Delta ; \theta)\left(c_{u}^{e}-C_{u}(\mu-\Delta-\Psi(1-\hat{p}(\Delta ; \theta)))\right)
$$

To guarantee the validity of our variational analysis for characterizing when the endowment is the only implementable allocation, it will be sufficient to require that $\pi(\Delta, \mu ; \theta)$ is concave in $(\Delta, \mu)$.
Assumption. $\pi(\Delta, \mu ; \theta)$ is concave in $(\Delta, \mu)$ for each $\theta$
This assumption requires the marginal profitability of insurance to decline in the amount of insurance provided. If the agents choice of $p$ is given exogenously (i.e. does not vary with $\Delta$ ), then concavity of the utility functions, $u$ and $v$, imply concavity of $\pi(\Delta, \mu ; \theta)$. Assumption A. 3 ensures that this extends to the case when $p$ is a choice and can respond to $\theta$.
Claim. If $\Psi^{\prime \prime \prime}(q ; \theta)>0$ for all $\theta$ and $\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2$ then $\pi$ is globally concave in $(\mu, \Delta)$.
For simplicity, we consider a fixed $\theta$ and drop reference to it. Profits are given by

$$
\pi(\Delta, \mu)=\hat{q}(\Delta)\left(c_{e}^{e}-C_{e}(\mu-\Psi(\hat{q}(\Delta)))\right)+(1-\hat{q}(\Delta))\left(c_{u}^{e}-C_{u}(\mu-\Delta-\Psi(\hat{q}(\Delta)))\right)
$$

The goal is to show the Hessian of $\pi$ is negative semi-definite. I proceed in three steps. First, I derive conditions which guarantee $\frac{\partial^{2} \pi}{\partial \Delta^{2}}<0$. Second, I show that, in general, we have $\frac{\partial^{2} \pi}{\partial \mu^{2}}<0$. Finally, I show the conditions provided to guarantee $\frac{\partial^{2} \pi}{\partial \Delta^{2}}<0$ also imply the determinant of the Hessian is positive, so that both eigenvalues of the Hessian must be negative and thus the matrix is negative semi-definite.

## A.3.1 Conditions that imply $\frac{\partial^{2} \pi}{\partial \Delta^{2}}<0$

Taking the first derivative with respect to $\Delta$, we have

$$
\begin{aligned}
\frac{\partial \pi}{\partial \Delta}= & \frac{\partial \hat{q}}{\partial \Delta}\left(c_{e}^{e}-c_{u}^{e}+C_{u}(\mu-\Delta-\Psi(\hat{q}(\Delta)))\right) \\
& -(1-\hat{q}(\Delta)) C_{u}^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))-\hat{q}(\Delta) C_{e}^{\prime}(\mu-\Psi(\hat{q}(\Delta)))
\end{aligned}
$$

Taking another derivative with respect to $\Delta$, applying the identity $\Delta=\Psi^{\prime}(\hat{p}(\Delta))$, and collecting terms yields

$$
\begin{aligned}
\frac{\partial^{2} \pi}{\partial \Delta^{2}}= & -\left[(1-\hat{q}(\Delta))(1+\Delta)^{2} C_{u}^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))+\hat{q}(\Delta)\left(\Delta \hat{q}^{\prime}(\Delta)\right)^{2} C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta)))\right] \\
& +\frac{\partial \hat{q}}{\partial \Delta}\left[(1-\hat{q}(\Delta)) C^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))+\hat{q}(\Delta) C^{\prime}(u-\Psi(\hat{q}(\Delta)))-\left(2+2 \Delta \hat{q}^{\prime}(\Delta)\right) C^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))\right] \\
& +\frac{\partial^{2} \hat{q}}{\partial \Delta^{2}}\left[c_{e}^{e}-c_{u}^{e}+C(\mu-\Delta-\Psi(\hat{q}(\Delta)))-C(\mu-\Psi(\hat{q}(\Delta)))+(1-\hat{q}(\Delta)) \Delta C^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))+\hat{q}(\Delta) C^{\prime}(\mu-\Psi(\hat{q}(\Delta)\right.
\end{aligned}
$$

We consider these three terms in turn. The first term is always negative because $C^{\prime \prime}>0$. The second term, multiplying $\frac{\partial \hat{q}}{\partial \Delta}$, can be shown to be positive if

$$
(1+\hat{q}(\Delta)) C^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) \geq \hat{q}(\Delta) C^{\prime}(\mu-\Delta)
$$

which is necessarily true whenever

$$
\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2
$$

This inequality holds as long as people are willing to pay less than a $100 \%$ markup for a small amount of insurance, evaluated at their endowment.

Finally, the third term is positive as long as $\Psi^{\prime \prime \prime}>0$. To see this, one can easily verify that the term multiplying $\frac{\partial^{2} \hat{q}}{\partial \Delta^{2}}$ is necessarily positive. Also, note that $\frac{\partial^{2} \hat{q}}{\partial \Delta^{2}}=\frac{-\Psi^{\prime \prime \prime}}{\left(\Psi^{\prime \prime}\right)^{2}}$. Therefore, if we assume that $\Psi^{\prime \prime \prime}>0$, the entire last term will necessarily be negative. In sum, it is sufficient to assume $\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2$ and $\Psi^{\prime \prime \prime}>0$ to guarantee that $\frac{\partial^{2} \pi}{\partial \Delta^{2}}<0$.

## A.3.2 Conditions that imply $\frac{\partial^{2} \pi}{\partial \mu^{2}}<0$

Fortunately, profits are easily seen to be concave in $\mu$. We have

$$
\frac{\partial \pi}{\partial \mu}=-(1-\hat{q}(\Delta)) C^{\prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))-\hat{q}(\Delta) C^{\prime}(\mu-\Psi(\hat{q}(\Delta)))
$$

so that

$$
\frac{\partial^{2} \pi}{\partial \mu^{2}}=-(1-\hat{q}(\Delta)) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))-\hat{q}(\Delta) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta)))
$$

which is negative because $C^{\prime \prime}>0$.

## A.3.3 Conditions to imply $\frac{\partial^{2} \pi}{\partial \Delta^{2}} \frac{\partial^{2} \pi}{\partial \mu^{2}}-\left(\frac{\partial^{2} \pi}{\partial \Delta \partial \mu}\right)>0$

Finally, we need to ensure that the determinant of the Hessian is positive. To do so, first note that

$$
\frac{\partial^{2} \pi}{\partial \mu \partial \Delta}=(1-\hat{q}(\Delta)) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))\left(1+\Delta \hat{q}^{\prime}(\Delta)\right)+\hat{q}(\Delta) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta))) \Delta \hat{q}^{\prime}(\Delta)
$$

Also, we note that under the assumptions $\Psi^{\prime \prime \prime}>0$ and $\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2$, we have the inequality

$$
\frac{\partial^{2} \pi}{\partial \Delta^{2}}<-\left[(1-\hat{q}(\Delta))(1+\Delta)^{2} C_{u}^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta)))+\hat{q}(\Delta)\left(\Delta \hat{q}^{\prime}(\Delta)\right)^{2} C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta)))\right]
$$

Therefore, we can ignore the longer terms in the expression for $\frac{\partial^{2} \pi}{\partial \Delta^{2}}$ above. We multiply the RHS of the above equation with the value of $\frac{\partial^{2} \pi}{\partial \mu^{2}}$ and subtract $\left(\frac{\partial^{2} \pi}{\partial \Delta \partial \mu}\right)^{2}$. Fortunately, many of the terms cancel out, leaving the inequality

$$
\begin{aligned}
\frac{\partial^{2} \pi}{\partial \Delta^{2}} \frac{\partial^{2} \pi}{\partial \mu^{2}}-\left(\frac{\partial^{2} \pi}{\partial \Delta \partial \mu}\right)^{2} \geq & (1-\hat{q}(\Delta)) \hat{q}(\Delta)\left(1+\Delta \hat{q}^{\prime}(\Delta)\right)^{2} C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta))) \\
& +\hat{q}(\Delta)(1-\hat{q}(\Delta))\left(\Delta \hat{q}^{\prime}(\Delta)\right)^{2} C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta))) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) \\
& -2(1-\hat{q}(\Delta)) \hat{q}(\Delta)\left(1+\Delta \hat{q}^{\prime}(\Delta)\right) \Delta \hat{q}^{\prime}(\Delta) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta)))
\end{aligned}
$$

which reduces to the inequality

$$
\frac{\partial^{2} \pi}{\partial \Delta^{2}} \frac{\partial^{2} \pi}{\partial \mu^{2}}-\left(\frac{\partial^{2} \pi}{\partial \Delta \partial \mu}\right)^{2} \geq \hat{q}(\Delta)(1-\hat{q}(\Delta)) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta))) K(\mu, \Delta)
$$

where

$$
\begin{aligned}
K(\mu, \Delta) & =\left(1+\Delta \hat{q}^{\prime}(\Delta)\right)^{2}+\left(\Delta \hat{q}^{\prime}(\Delta)\right)^{2}-2 \Delta \hat{q}^{\prime}(\Delta)-2\left(\Delta \hat{q}^{\prime}(\Delta)\right)^{2} \\
& =1
\end{aligned}
$$

So, since $C^{\prime \prime}>0$, we have that the determinant must be positive. In particular, we have

$$
\frac{\partial^{2} \pi}{\partial \Delta^{2}} \frac{\partial^{2} \pi}{\partial \mu^{2}}-\left(\frac{\partial^{2} \pi}{\partial \Delta \partial \mu}\right)^{2} \geq \hat{q}(\Delta)(1-\hat{q}(\Delta)) C^{\prime \prime}(\mu-\Delta-\Psi(\hat{q}(\Delta))) C^{\prime \prime}(\mu-\Psi(\hat{q}(\Delta)))
$$

## A.3.4 Summary

As long as $\Psi^{\prime \prime \prime}>0$ and $\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2$, the profit function is globally concave. Empirically, I find that $\frac{u^{\prime}\left(c_{u}^{e}\right)}{v^{\prime}\left(c_{e}^{e}\right)} \leq 2$. Therefore, the unsubstantiated assumption for the model is that the convexity of the effort function increases in $p, \Psi^{\prime \prime \prime}>0$. An alternative statement of this assumption is that $\frac{\partial^{2} \hat{q}}{\partial \Delta^{2}}<0$, so that the marginal impact of $\Delta$ on the employment probability is declining in the size of $\Delta$. Put differently, it is an assumption that providing utility incentives to work has diminishing returns.

Future work can derive the necessary conditions when individuals can make additional actions, $a(\theta)$, in response to unemployment. I suspect the proofs can be extended to such cases, but identifying the necessary conditions for global concavity would be an interesting direction for future work.

## B Details of Empirical Approach

## B. 1 Details on Lower Bounds on Average Pooled Price Ratio

This section provides details on the estimation of the lower bounds on the average pooled price ratio. I begin by providing theoretical motivation for the average pooled price ratio by showing it characterizes when an insurer can earn positive profits if it enters with a particular random pricing strategy. Then, I provide conditions under which the average pooled price defined by the predicted values provides a lower bound on the average pooled price ratio, $T_{Z} \leq E[T(P)]$.

## B.1.1 Motivating the Average Pooled Price Ratio when Insurers don't know $P$

To see the theoretical relevance of $E[T(P)]$, suppose an insurer seeks to start an insurance market by randomly drawing an individual from the population and, perhaps through some market research, learns exactly how much this individual is willing to pay. The insurer offers a contract that collects $\$ 1$ in the event of being employed and pays an amount in the unemployed state that makes the individual perfectly indifferent to the policy. If $p$ is the probability this individual will become unemployed, then all risks $P \geq p$ will choose to purchase the policy as well. The profit per dollar of revenue will be

$$
r(p)=\frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}-T(p)
$$

So, if the original individual was selected at random from the population, the expected profit per dollar would be positive if and only if

$$
E\left[\frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}\right] \geq E[T(P)]
$$

If the insurer is randomly choosing contracts to try to sell, the average pooled price ratio, $E[T(P)]$, provides information on whether or not a UI market would be profitable.

## B.1.2 Conditions under which $E\left[T_{Z}\left(P_{Z}\right)\right] \leq E[T(P)]$

Here, I provide conditions under which $E\left[T_{Z}\left(P_{Z}\right)\right]$ provides a lower bound on the average pooled price ratio, $E[T(P)]$. To begin, assume that (a) the elicitations, $Z$, have no more information about $U$ than do true beliefs, $P$. Stated formally: $\operatorname{Pr}\{U \mid X, Z, P\}=\operatorname{Pr}\{U \mid X, P\}$. Second, assume that beliefs are unbiased, so that $\operatorname{Pr}\{U \mid X, P\}=P$. Hendren (2013) shows that these two assumptions imply that $E\left[m\left(P_{Z}\right)\right] \leq E[m(P)]$. This suggests that $E\left[T_{Z}\left(P_{Z}\right)\right] \leq 1+\frac{E[m(P)]}{\operatorname{Pr}\{U\}}$. So, what remains to show is that $1+\frac{E[m(P)]}{\operatorname{Pr}\{U\}} \leq E[T(P)]$. For this, we make one additional assumption that $\operatorname{cov}\left(\frac{m(P)}{P}, P\right) \leq 0$. This is a natural assumption because $m(p)$ is, on average, a decreasing function in $p$ (because $m(1)=0$ ), so dividing by $P$ renders it an even more strongly decreasing function in $P$. Indeed, I have been unable to find a random variable $P$ for which $\operatorname{cov}\left(\frac{m(P)}{P}, P\right)>0$.

Given these assumptions note that

$$
\begin{aligned}
E[T(P)] & =E_{p}\left[\frac{E[P \mid P \geq p]}{p} \frac{1-p}{1-E[P \mid P \geq p]}\right] \\
& \geq E_{p}\left[1+\frac{m(p)}{p}\right] \\
& \geq 1+E\left[\frac{m(P)}{P}\right]
\end{aligned}
$$

where $E_{p}$ represents the expectation with respect to drawing $p$ from the distribution of $P$. Note the second line follows from the fact that $E[P \mid P \geq p] \geq p$.

So, it suffices to show that $E\left[\frac{m(P)}{P}\right] \geq \frac{E[m(P)]}{E[P]}$. Clearly

$$
E[m(P)]=E\left[\frac{m(P)}{P}\right] E[P]+\operatorname{cov}\left(P, \frac{m(P)}{P}\right)
$$

so that

$$
E\left[\frac{m(P)}{P}\right]=\frac{E[m(P)]-\operatorname{cov}\left(P, \frac{m(P)}{P}\right)}{E[P]}
$$

Imposing $\operatorname{cov}\left(\frac{m(P)}{P}, P\right) \leq 0$ yields $E[T(P)] \geq 1+\frac{E[m(P)]}{E[P]}$, which in turn implies $E[T(P)] \geq E\left[T_{Z}\left(P_{Z}\right)\right]$.

## B. 2 Specification for Point Estimation

I follow Hendren (2013) by assuming that $Z=P+\epsilon$, where $\epsilon$ has the following structure. With probability $\lambda$, individuals report a noisy measure of their true belief $P$ that is drawn from a $[0,1]$-censored normal distribution with mean $P+\alpha(X)$ and variance $\sigma^{2}$. With this specification, $\alpha(X)$ reflects potential bias in elicitations and $\sigma$ represents the noise. While this allows for general measurement error in the elicitations, it does not produce the strong focal point concentrations shown in Figure 1 and documented in existing work (Gan et al. (2005); Manski and Molinari (2010)). To capture these, I assume that with probability $1-\lambda$ individuals take their noisy report with the same bias
$\alpha(X)$ and variance $\sigma^{2}$, but censor it into a focal point at 0,50 , or 100 . If their elicitation would have been below $\kappa$, they report zero. If it would have been between $\kappa$ and $1-\kappa$, they report 50 ; and if it would have been above $1-\kappa$, they report 1. Hence, I estimate four elicitation error parameters: $(\sigma, \lambda, \kappa, \alpha(X))$ that capture the patterns of noise and bias in the relationship between true beliefs, $P$, and the elicitations reported on the surveys, $Z$.

Specifically, the p.d.f./p.m.f. of $Z$ given $P$ is given by

$$
f(Z \mid P, X)=\left\{\begin{array}{clc}
(1-\lambda) \Phi\left(\frac{-P-\alpha(X)}{\sigma}\right)+\lambda \Phi\left(\frac{\kappa-P-\alpha(X)}{\sigma}\right) & \text { if } & Z=0 \\
\lambda\left(\Phi\left(\frac{1-\kappa-P-\alpha(X)}{\sigma}\right)-\Phi\left(\frac{\kappa-P-\alpha(X)}{\sigma}\right)\right) & \text { if } Z=0.5 \\
(1-\lambda) \Phi\left(\frac{1-P-\alpha(X)}{\sigma}\right)+\lambda\left(1-\Phi\left(\frac{1-\kappa-P-\alpha(X)}{\sigma}\right)\right) & \text { if } Z=1 \\
\frac{1}{\sigma} \phi\left(\frac{Z-P-\alpha(X)}{\sigma}\right) & \text { if } & \text { o.w. }
\end{array}\right.
$$

where $\phi$ denotes the standard normal p.d.f. and $\Phi$ the standard normal c.d.f. I estimate four elicitation error parameters: $(\sigma, \lambda, \kappa, \alpha(X)) . \sigma$ captures the dispersion in the elicitation error, $\lambda$ is the fraction of focal point respondents, $\kappa$ is the focal point window. I allow the elicitation bias term, $\alpha(X)$, to vary with the observable variables, $X$. This allows elicitations to be biased, but maintains the assumption that true beliefs are unbiased. This approach builds upon Manski and Molinari (2010) by thinking of the focal point responses as "interval data" (i.e. 50/50 corresponds to some region around $50 \%$, but not exactly $50 \%$ ). However, the present approach differs from Manski and Molinari (2010) by allowing the response to be a noisy and potentially biased measure of this response (as $50 / 50$ corresponds to a region around $50 \%$ for the noisy $Z$ measure, not the true $P$ measure).

Ideally, one would flexibly estimate the distribution of $P$ given $X$ at each possible value of $X$. This would enable separate estimates of the minimum pooled price ratio for each value of $X$. However, the dimensionality of $X$ prevents this in practice. Instead, I again follow Hendren (2013) and adopt an index assumption on the cumulative distribution of beliefs, $F(p \mid X)=\int_{0}^{p} f_{P}(\tilde{p} \mid X) d \tilde{p}$,

$$
\begin{equation*}
F(p \mid X)=\tilde{F}(p \mid \operatorname{Pr}\{U \mid X\}) \tag{26}
\end{equation*}
$$

where I assume $\tilde{F}(p \mid q)$ is continuous in $q$ (where $q \in\{0,1\}$ corresponds to the level of $\operatorname{Pr}\{U \mid X\}$ ). This assumes that the distribution of private information is the same for two observable values, $X$ and $X^{\prime}$, that have the same observable unemployment probability, $\operatorname{Pr}\{U \mid X\}=\operatorname{Pr}\left\{U \mid X^{\prime}\right\}$. Although one could perform different dimension reduction techniques, controlling for $\operatorname{Pr}\{U \mid X\}$ is particularly appealing because it nests the null hypothesis of no private information $(F(p \mid X)=1\{p \leq \operatorname{Pr}\{U \mid X\}\}) .{ }^{52}$

Beta versus Point-Mass Distribution Hendren (2013) flexibly approximates $F(p \mid q)$ using mixtures of Beta distributions. In the current context, A key difficulty with using functions to approximate the distribution of $P$ is that much of the mass of the distribution is near zero. Continuous probability distribution functions, such as Beta distributions, require very high degrees for the shape parameters to acquire a good fit. Therefore, I approximate $P$ as a sum of discrete point-mass distributions. ${ }^{53}$ Formally, I assume

$$
\tilde{F}(p \mid q)=w 1\{p \leq q-a\}+(1-w) \Sigma_{i} \xi_{i} 1\left\{p \leq \alpha_{i}\right\}
$$

where $\alpha_{i}$ are a set of point masses in $[0,1]$ and $\xi_{i}$ is the mass on each point mass. I estimate these point mass parameters using maximum likelihood estimation. For the baseline results, I use 3 mass points, which generally provides a decent fit for the data. Appendix Table IV presents the raw estimates for these point mass distributions.

Given the estimate of $\tilde{F}(p \mid q)$, I then compute the pooled price ratio at each mass point and report the minimum across all values aside from the largest mass point. Mechanically, this has a value of $T(p)=1$. As noted in Hendren (2013), estimation of the minimum $T(p)$ across the full support of the type distribution is not feasible because of an extremal quantile estimation problem. To keep the estimates "in-sample", I report values for the mean value of $q=\operatorname{Pr}\{U\}=0.031$; but estimates at other values of $q$ are similarly large.

[^3]
## C Willingness to Pay Metrics

## C. 1 Taylor Expansion

Note that $u(c)=v(c)$ so that

$$
\begin{aligned}
\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} & \approx \frac{u^{\prime}\left(c_{e}(p)\right)+u^{\prime \prime}\left(c_{e}(p)\right)\left(c_{u}(p)-c_{e}(p)\right)+\frac{1}{2} u^{\prime \prime \prime}\left(c_{e}(p)\right)\left(c_{u}(p)-c_{e}(p)\right)^{2}}{u^{\prime}\left(c_{e}(p)\right)} \\
& =1+\frac{u^{\prime \prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \frac{c_{u}(p)-c_{e}(p)}{c_{e}(p)} \\
& =1+\frac{-c_{e}(p) u^{\prime \prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \frac{c_{e}(p)-c_{u}(p)}{c_{e}(p)}+\frac{c_{e}(p) u^{\prime \prime \prime}\left(c_{e}(p)\right)}{u^{\prime \prime}\left(c_{e}(p)\right)} \frac{c_{e}(p) u^{\prime \prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \frac{1}{2}\left(\frac{c_{e}(p)-c_{u}(p)}{c_{e}(p)}\right)^{2} \\
& =1+\sigma \frac{\Delta c}{c}(p)\left[1+\frac{\gamma}{2} \frac{\Delta c}{c}(p)\right]
\end{aligned}
$$

And, under an assumption of constant relative risk aversion, we have $\gamma=\sigma+1$

$$
\begin{aligned}
\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1 & \approx \sigma \frac{\Delta c}{c}(p)\left[1+\frac{\sigma+1}{2} \frac{\Delta c}{c}(p)\right] \\
& =\sigma \frac{\Delta c}{c}(p)+\sigma \frac{\sigma+1}{2}\left(\frac{\Delta c}{c}(p)\right)^{2}
\end{aligned}
$$

## C. 2 Proof of Proposition 1

Note under state independence, the Euler equation implies

$$
u^{\prime}\left(c_{\text {pre }}(p)\right)=p u^{\prime}\left(c_{u}(p)\right)+(1-p) u^{\prime}\left(c_{e}(p)\right)
$$

so that

$$
u^{\prime \prime}\left(c_{p r e}(p)\right) \frac{d c_{p r e}}{d p}=u^{\prime}\left(c_{u}(p)\right)-u^{\prime}\left(c_{e}(p)\right)+p u^{\prime \prime}\left(c_{u}(p)\right) \frac{d c_{u}}{d p}+(1-p) u^{\prime \prime}\left(c_{e}(p)\right) \frac{d c_{e}}{d p}
$$

Dividing,
$u^{\prime}\left(c_{p r e}(p)\right) \frac{u^{\prime \prime}\left(c_{p r e}(p)\right)}{u^{\prime}\left(c_{p r e}(p)\right)} \frac{d c_{p r e}}{d p}=u^{\prime}\left(c_{e}\right) \frac{u^{\prime}\left(c_{u}(p)\right)-u^{\prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+p u^{\prime}\left(c_{u}(p)\right) \frac{u^{\prime \prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{u}(p)\right)} \frac{d c_{u}}{d p}+(1-p) u^{\prime}\left(c_{e}(p)\right) \frac{u^{\prime \prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \frac{d c_{e}}{d p}$ or
$u^{\prime}\left(c_{p r e}(p)\right) \sigma \frac{-d \log \left(c_{p r e}\right)}{d p}=u^{\prime}\left(c_{e}\right) \sigma\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]+p u^{\prime}\left(c_{u}(p)\right) \sigma \frac{-d \log \left(c_{u}(p)\right)}{d p}+(1-p) u^{\prime}\left(c_{e}(p)\right) \sigma \frac{-d \log \left(c_{e}(p)\right)}{d p}$
So, dividing by $u^{\prime}\left(c_{e}(p)\right)$ yields:

$$
\frac{u^{\prime}\left(c_{p r e}(p)\right)}{u^{\prime}\left(c_{e}\right)} \sigma \frac{-d \log \left(c_{p r e}\right)}{d p}=\sigma\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]+p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \sigma \frac{-d \log \left(c_{u}(p)\right)}{d p}+(1-p) \sigma \frac{-d \log \left(c_{e}(p)\right)}{d p}
$$

And, using the Euler equation, $p u^{\prime}\left(c_{u}(p)\right)+(1-p) u^{\prime}\left(c_{e}(p)\right)=u^{\prime}\left(c_{p r e}(p)\right)$,

$$
\begin{aligned}
& \frac{p u^{\prime}\left(c_{u}(p)\right)+(1-p) u^{\prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \sigma \frac{-d \log \left(c_{p r e}(p)\right)}{d p}=\frac{u^{\prime}\left(c_{u}(p)\right)-u^{\prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \sigma \frac{-d \log \left(c_{u}(p)\right)}{d p}+(1-p) \sigma \frac{-d \log \left(c_{e}(p)\right)}{d p} \\
& \left(p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+1-p\right) \sigma \frac{-d \log \left(c_{p r e}(p)\right)}{d p}=\frac{u^{\prime}\left(c_{u}(p)\right)-u^{\prime}\left(c_{e}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+\left(p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+1-p\right) \sigma \frac{-d \log \left(c_{e}(p)\right)}{d p}+p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)} \sigma\left(\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right)
\end{aligned}
$$

so that

$$
\sigma \frac{-d \log \left(c_{p r e}\right)}{d p}=\frac{\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(p e e^{\prime}(p)\right.}-1}{1+p\left(\frac{\left.u^{\prime}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1\right)}+\sigma \frac{-d \log \left(c_{e}(p)\right)}{d p}+\frac{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}}{p} \sigma\left(\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right)
$$

or

$$
\frac{-d \log \left(c_{p r e}\right)}{d p}=\frac{\frac{1}{\sigma}\left(\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(u_{e}(p)\right)}-1\right)}{1+p\left(\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1\right)}+\frac{-\operatorname{dlog}\left(c_{e}(p)\right)}{d p}+\frac{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}}{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+1-p}\left(\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right)
$$

Note that the assumption is maintained that $\log \left(c_{p r e}\right)$ is linear in $p$, in addition to $\log \left(c_{e}\right)$ and $\log \left(c_{u}\right)$ being linear in $p$. This is of course an approximation in practice, as the equation above illustrates this cannot simultaneously be true for all $p$. Therefore, I assume it is true only in expectation, so that
$\frac{-d \log \left(c_{p r e}\right)}{d p}=\frac{1}{\sigma}\left(\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1\right) E\left[\frac{1}{1+p\left(\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1\right)}\right]+\frac{-\operatorname{dlog}\left(c_{e}(p)\right)}{d p}+E\left[\frac{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}}{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+1-p}\left(\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right)\right]$
which if it holds for all $p$ must also hold for the expectation taken with respect to $p$. Let $\kappa=E\left[\frac{1}{1+p\left(\frac{u^{\prime}\left(u_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1\right)}\right]$. Note also that

$$
\frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}-1 \approx \sigma E\left[\log \left(c_{e}(p)\right)-\log \left(c_{u}(p)\right)\right]
$$

which implies

$$
\frac{-d \log \left(c_{p r e}\right)}{d p}=E\left[\log \left(c_{e}(p)\right)-\log \left(c_{u}(p)\right)\right] \kappa+\frac{-\operatorname{dlog}\left(c_{e}(p)\right)}{d p}+E\left[\frac{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}}{p \frac{u^{\prime}\left(c_{u}(p)\right)}{u^{\prime}\left(c_{e}(p)\right)}+1-p}\left(\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right)\right]
$$

Now, consider the impact of unemployment on the first difference of consumption. Define $\Delta^{F D}$ as the estimated impact on the first difference in consumption:

$$
\Delta^{F D}=E\left[\log (c)-\log \left(c_{-1}\right) \mid U=1\right]-E\left[\log (c)-\log \left(c_{-1}\right) \mid U=0\right]
$$

Adding and subtracting $E\left[\log \left(c_{e}\right) \mid U=1\right]$ yields

$$
\Delta^{F D}=E[\log (c) \mid U=1]-E\left[\log \left(c_{e}\right) \mid U=1\right]+E\left[\log \left(c_{e}\right) \mid U=1\right]-E[\log (c) \mid U=0]-\left(E\left[\log \left(c_{-1}\right) \mid U=1\right]-E\left[\log \left(c_{-1}\right) \mid U=0\right]\right)
$$

Note that $c=c_{u}$ for those with $U_{t}=1$ and $c=c_{e}$ for those with $U=0$. The following three equations help expand $\Delta^{F D}$ :

$$
E\left[\log \left(c_{-1}\right) \mid U=1\right]-E\left[\log \left(c_{-1}\right) \mid U=0\right]=\frac{d \log \left(c_{\text {pre }}\right)}{d p} \frac{\operatorname{var}(P)}{\operatorname{var}(U)}
$$

and

$$
\begin{aligned}
E[\log (c) \mid U=1]-E\left[\log \left(c_{e}\right) \mid U=0\right] & =E\left[\log \left(c_{u}\right) \mid U=1\right]-E\left[\log \left(c_{e}\right) \mid U=1\right] \\
& =E\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]+\frac{d\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]}{d p}(E[P \mid U=1]-E[P])
\end{aligned}
$$

and

$$
\begin{aligned}
E\left[\log \left(c_{e}\right) \mid U=1\right]-E[\log (c) \mid U=0] & =E\left[\log \left(c_{e}\right) \mid U=1\right]-E\left[\log \left(c_{e}\right) \mid U=0\right] \\
& =\frac{d \log \left(c_{e}\right)}{d p} \frac{\operatorname{var}(P)}{\operatorname{var}(U)}
\end{aligned}
$$

So, substituting these into $\Delta^{F D}$ yields:
$\Delta^{F D}=E\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]-\frac{\operatorname{var}(P)}{\operatorname{var}(U)}\left[\kappa\left(E\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]\right)+E[P] \frac{u^{\prime}\left(c_{u}\right)}{u^{\prime}\left(c_{e}\right)} \frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right]+\left[\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}\right](E[P \mid U=1]-E[P])$
Let $\frac{d \Delta}{d p}=\frac{d\left[\log \left(c_{e}\right)-\log \left(c_{u}\right)\right]}{d p}$ denote how the consumption drop varies with $p$. Solving for $E\left[\log \left(c_{e}\right)-\log \left(c_{e}\right)\right]$ yields

$$
E\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]=\frac{\Delta^{F D}+\frac{d \Delta}{d p}(E[P \mid U=1]-E[P])}{1-\frac{\operatorname{var}(P)}{\operatorname{var}(U)} \kappa-\bar{p} \sigma \frac{d \Delta}{d p}}
$$

where $\kappa=$ which yields the desired result. Note that if the consumption drop does not vary with $p$, then this reduces to

$$
E\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]=\frac{\Delta^{F D}}{1-\frac{\operatorname{var}(P)}{\operatorname{var}(U)} \kappa} \equiv \Delta^{I V}
$$

More generally, if the size of the consumption drop is increasing with $p$, then $E\left[\log \left(c_{u}\right)-\log \left(c_{e}\right)\right]>\Delta^{I V}$.

## C. 3 Maximum Willingness to Pay

While the analysis to this point estimates the average causal effect of unemployment, Equation (8) requires comparing the willingness to pay for all $p$ to the pooled price ratio. Therefore, it is also useful to understand the heterogeneity in the potential willingness to pay across the population. How much might some people be willing to pay for insurance?

Estimating minima and maxima is always more difficult than estimating means; but this section attempts to make a bit of progress to help shed light on this important question. Let $\Delta^{\text {min }}$ denote the largest causal effect of unemployment in the population,

$$
\begin{equation*}
\Delta^{\min }=\min _{p}\left[\log \left(c_{u}(p)\right)-\log \left(c_{e}(p)\right)\right] \tag{27}
\end{equation*}
$$

Following equation (9), note that the willingness to pay satisfies

$$
\begin{equation*}
\frac{u^{\prime}\left(c_{u}\right)-u^{\prime}\left(c_{e}\right)}{u^{\prime}\left(c_{e}\right)} \geq \sigma\left(-\Delta^{\min }\right)\left(1+\frac{\gamma}{2}\left(-\Delta^{\min }\right)\right) \tag{28}
\end{equation*}
$$

Therefore, $\Delta^{\min }$ generates a upper bound on the willingness to pay (note that $\Delta^{\min }<0$ ).
This motivates the question: How big can the causal impact of unemployment be? To address this, note that one can write the causal effect as the sum of two first differences:

$$
\log \left(c_{u}(p)\right)-\log \left(c_{e}(p)\right)=\log \left(c_{u}(p)\right)-\log \left(c_{t-1}(p)\right)-\left(\log \left(c_{e}(p)\right)-\log \left(c_{t-1}(p)\right)\right)
$$

where the first term captures consumption change if unemployed and the second term is the consumption change if employed. Let $\Delta_{e}^{\max }=\max _{p}\left\{\log \left(c_{e}(p)\right)-\log \left(c_{t-1}(p)\right)\right\}$ denote the maximum consumption change experienced by those who did not lose their job. And, let $\Delta_{u}^{\min }=\min _{p}\left\{\log \left(c_{u}(p)\right)-\log \left(c_{t-1}(p)\right)\right\}$ denote the minimum consumption change experienced by those who lose their job. Note that we expect $\Delta_{e}^{\max }>0$ and $\Delta_{u}^{\min }<0$. The Euler equation ((6)) combined with the assumption of CRRA preferences implies that $c_{t-1}$ lies between $c_{u}(p)$ and $c_{e}(p), c_{t-1}(p) \in\left[c_{u}(p), c_{e}(p)\right]$ for all $p$. Under this natural assumption, the causal impact of unemployment is bounded below by the difference between these drops:

$$
\Delta^{\min } \geq \Delta_{u}^{\min }-\Delta_{e}^{\max }
$$

Therefore, one can bound the causal effect of unemployment on consumption by the largest consumption drop minus the smallest consumption increase. The question now becomes: how large can the consumption drop upon unemployment be, $\Delta_{u}^{m i n}$ ? And, how large can the consumption increase upon learning that you didn't lose your job be, $\Delta_{e}^{\max }$ ?

If one observed consumption directly, one could estimate the full distribution of first differences in consumption for those who become unemployed, $\log \left(c_{u}(p)\right)-\log \left(c_{t-1}(p)\right)$, and remain employed, $\log \left(c_{e}(p)\right)-\log \left(c_{t-1}(p)\right)$. Then, one could in principle find $\Delta_{u}^{\min }$ and $\Delta_{e}^{\max }$ directly from the data.

However, consumption data in the PSID and other datasets is quite noisy in practice (see for example Zeldes (1989); Meghir and Pistaferri (2011)). ${ }^{54}$ Therefore, I proceed as follows. Note that the Euler equation implies that $c_{t-1}(p) \in\left[c_{u}(p), c_{e}(p)\right]$ for all $p$. In particular, this implies that the log consumption change should always drop for those who lose their job, $c_{t-1}(p) \geq c_{u}(p)$. Therefore, I use the extent to which one observes consumption increases for those who become unemployed to provide information about how the consumption change distribution and its minimum, $\Delta_{u}^{\text {min }}$, is affected by measurement error.

I begin by removing systematic variation in consumption changes due to life cycle and year effects. In particular, I regress the consumption change on the observables, $X$, in Equation (4) (an age cubic and year dummies) and let $\Delta_{i t}^{*}$ denote the residuals. ${ }^{55}$ Online Appendix Figure VI plots the distributions of $\Delta_{i t}^{*}$ for those with $U_{i t}=1$ and $U_{i t}=0$. As one can see, the wide dispersion is suggestive of considerable measurement error, as noted in previous literature.

Let $Q(\alpha, U)$ denote the $\alpha$-quantile of the distribution of $\Delta_{i t}^{*}$ as a function of unemployment status, $U_{t}$. Appendix Table II reports that $41.7 \%$ of the sample who become unemployed have $\Delta_{i t}^{*}>0$ (i.e. $Q(58.3,1)=0$ ), even after controlling for age and year effects. Because the Euler equation suggests consumption changes should not be positive,

[^4]it suggests the excess dispersion is the result of measurement error. The key assumption I impose is that the impact of measurement error is symmetric across the distribution of consumption changes. In particular, I assume that the probability that the observed consumption change lies above the maximum plausible consumption change of 0 is less than or equal to the probability that the observed consumption change is below the minimum actual consumption change, $\operatorname{Pr}\left\{\Delta_{i t}^{*} \leq \Delta_{u}^{m i n} \mid U_{i t}=1\right\} \geq \operatorname{Pr}\left\{\Delta_{i t}^{*} \geq 0 \mid U_{i t}=1\right\}$, where $\operatorname{Pr}\left\{\Delta_{i t}^{*} \geq 0 \mid U_{i t}=1\right\}=41.7 \%$. Appendix Figure V shows that the observed distribution of consumption changes is fairly symmetric, which would be consistent with the underlying assumptions needed for Equation (29) to hold. ${ }^{56}$ With this assumption,
\[

$$
\begin{equation*}
\Delta_{u}^{\min } \geq Q\left(\operatorname{Pr}\left\{\Delta_{i t}^{*} \geq 0 \mid U_{i t}=1\right\}, 1\right) \tag{29}
\end{equation*}
$$

\]

Because $\operatorname{Pr}\left\{\Delta_{i t}^{*} \geq 0 \mid U_{i t}=1\right\}=41.7 \%$, one can bound the consumption drop by the 41.7 th quantile of the observed consumption drop distribution. This equals $-13.7 \%$, as shown in Appendix Table II.

Similarly, one can impose an analogous assumption on the distribution of consumption changes for the employed that the observed fraction of the population that experiences a consumption decline when remaining employed is less than or equal to the fraction who experience a consumption increase that is above $\Delta_{e}^{\max }, \operatorname{Pr}\left\{\Delta_{i t}^{*} \leq 0 \mid U_{i t}=0\right\}=$ $\operatorname{Pr}\left\{\Delta_{i t}^{*} \geq \Delta_{e}^{\text {max }} \mid U_{i t}=0\right\}$. Under this assumption,

$$
\begin{equation*}
\Delta_{e}^{\max } \leq Q\left(\operatorname{Pr}\left\{\Delta_{i t}^{*} \leq \mid U_{i t}=0\right\}, 0\right) \tag{30}
\end{equation*}
$$

Appendix Table II shows this maximal consumption increase equals $0.5 \%$. Combining equations (29) and (30) yields the lower bound on the causal impact of unemployment on consumption:

$$
\Delta^{\min } \geq Q\left(\operatorname{Pr}\left\{\Delta_{i t}^{*} \geq 0 \mid U_{i t}=1\right\}, 1\right)-Q\left(\operatorname{Pr}\left\{\Delta_{i t}^{*} \leq \mid U_{i t}=0\right\}, 0\right)
$$

where the right hand side equals $-13.7 \%-0.5 \%=14.2 \%$ (s.e. $1.1 \%$ ), as reported in Table V, Column (7). Therefore, the maximum causal impact on food expenditure is $14.2 \%$, or roughly twice as large as the mean consumption drop. The lower rows in Table V scale this estimate by various values of risk aversion. With a conservative estimate of 3, it suggests the maximum markup individuals would be willing to pay is $54.7 \%$.

## C. 4 Proof of Proposition 2

Differentiating the Euler equation under assumption (b) yields

$$
u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)=v^{\prime \prime}\left(c_{\text {pre }}(p)\right) \frac{d c_{p r e}}{d p}
$$

Now, dividing by $v^{\prime}\left(c_{e}\right)$ yields

$$
\frac{u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)}{v^{\prime}\left(c_{e}\right)}=\frac{v^{\prime \prime}\left(c_{p r e}(p)\right)}{v^{\prime}\left(c_{e}\right)} \frac{d c_{p r e}}{d p}
$$

and expanding the RHS yields

$$
\frac{u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)}{v^{\prime}\left(c_{e}\right)}=\frac{v^{\prime}\left(c_{\text {pre }}(p)\right)}{v^{\prime}\left(c_{e}\right)} \frac{c_{\text {pre }}(p) v^{\prime \prime}\left(c_{\text {pre }}(p)\right)}{v^{\prime}\left(c_{\text {pre }}(p)\right)} \frac{1}{c_{\text {pre }}(p)} \frac{d c_{\text {pre }}}{d p}
$$

And, imposing the Euler equation to replace $v^{\prime}\left(c_{p r e}(p)\right)$ in the numerator on the RHS $\left(v^{\prime}\left(c_{p r e}(p)\right)=p u^{\prime}\left(c_{u}\right)+\right.$ $\left.(1-p) v^{\prime}\left(c_{e}\right)\right)$ yields,

$$
\frac{u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)}{v^{\prime}\left(c_{e}\right)}=\left[p \frac{u^{\prime}\left(c_{u}\right)}{v^{\prime}\left(c_{e}\right)}+(1-p)\right] \frac{c_{p r e}(p) v^{\prime \prime}\left(c_{p r e}(p)\right)}{v^{\prime}\left(c_{p r e}(p)\right)} \frac{1}{c_{p r e}(p)} \frac{d c_{p r e}}{d p}
$$

Dividing by $p \frac{u^{\prime}\left(c_{u}\right)}{v^{\prime}\left(c_{e}\right)}+(1-p)$ and taking expectations over $p$ yields

$$
\kappa \frac{u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)}{v^{\prime}\left(c_{e}\right)}=E\left[\frac{c_{\text {pre }}(p) v^{\prime \prime}\left(c_{\text {pre }}(p)\right)}{v^{\prime}\left(c_{\text {pre }}(p)\right)} \frac{1}{c_{\text {pre }}(p)} \frac{d c_{\text {pre }}}{d p}\right]
$$

Now, imposing $\sigma=\frac{-c_{p r e}(p) v^{\prime \prime}\left(c_{\text {pre }}(p)\right)}{v^{\prime}\left(c_{\text {pre }}(p)\right)}$ for all $p$, noting that $\frac{1}{c_{\text {pre }}(p)} \frac{d c_{\text {pre }}}{d p}=\frac{d \log \left(c_{\text {pre }}\right)}{d p}$, and dividing by $\kappa$ yields:

$$
\frac{u^{\prime}\left(c_{u}\right)-v^{\prime}\left(c_{e}\right)}{v^{\prime}\left(c_{e}\right)}=\frac{\sigma}{\kappa} E\left[\frac{-d \log \left(c_{\text {pre }}\right)}{d p}\right]
$$

[^5]
## C. 5 Ex-ante labor supply derivation

This section illustrates how to use the spousal labor supply response, combined with known estimates of the spousal labor response to labor earnings, to estimate the ex-ante willingness to pay for UI.

To begin, one needs a model of extensive margin labor supply response. I assume spousal labor force participation generates income, $y$, but has an additively separable effort cost, $\eta(\theta)$. I assume a spouse labor supply decision, $l \in\{0,1\}$, is a binary decision and is contained in the set of other actions, $a$. Formally, let utility be given by

$$
v\left(c_{p r e}\right)+p u\left(c_{u}\right)+(1-p) v\left(c_{e}\right)+1\{l=1\} \eta(\theta)+\tilde{\Psi}_{i}(1-p, \tilde{a}, \theta)
$$

where $\eta(\theta)$ is the disutility of labor for type $\theta$, distributed $F_{\eta}$ in the population.
Let $k(y, l, p)$ denote the utility value to a type $p$ of choosing $l$ to obtain income $y$ when they face an unemployment probability of $p$. The labor supply decision is

$$
k(y, 1, p)-k(0,0, p) \geq \eta(\theta)
$$

so that types will choose to work if and only if it increases their utility. This defines a threshold rule whereby individuals choose to work if and only if $\eta(\theta) \leq \bar{\eta}(y, p)$ and the labor force participation rate is given by $\Phi(y, p)=$ $F(\bar{\eta}(y, p))$.

Now, note that

$$
\frac{d \Phi}{d p}=f(\bar{\eta}) \frac{\partial \bar{\eta}}{\partial p}=f(\bar{\eta})\left[\frac{\partial k(y, 1, p)}{\partial p}-\frac{\partial k(0,0, p)}{\partial p}\right]
$$

and making an approximation that the impact of the income $y$ does not discretely change the instantaneous marginal utilities (i.e. because it will be smoothed out over the lifetime or because the income is small), we have

$$
\frac{d \Phi}{d p} \approx f(\bar{\eta}) \frac{\partial^{2} k}{\partial p^{2}} y
$$

Finally, note that $\frac{\partial k}{\partial y}=v^{\prime}\left(c_{p r e}(p)\right)$ is the marginal utility of income. So,

$$
\frac{d \Phi}{d p} \approx f(\bar{\eta}) \frac{d}{d p}\left[v^{\prime}\left(c_{p r e}(p)\right)\right] y
$$

and integrating across all the types $p$ yields

$$
E_{p}\left[\frac{d \Phi}{d p}\right] \approx E_{p}\left[f(\bar{\eta}) \frac{d}{d p} v^{\prime}\left(c_{p r e}(p)\right) y\right]
$$

To compare this response to a wage elasticity, consider the response to a $\$ 1$ increase in wages

$$
\frac{d \Phi}{d y}=f(\bar{\eta}) \frac{\partial k}{\partial y}
$$

so,

$$
E_{p}\left[\frac{d \Phi}{d p}\right] \approx E_{p}\left[\frac{d \Phi}{d y} y \frac{\frac{d}{d p} v^{\prime}\left(c_{p r e}(p)\right)}{v^{\prime}\left(c_{p r e}(p)\right)}\right]
$$

Now, let $\epsilon^{\text {semi }}=\frac{d \Phi}{d \log (y)}$ denote the semi-elasticity of spousal labor force participation. This yields

$$
\frac{E_{p}\left[\frac{d \Phi}{d p}\right]}{\epsilon^{s e m i}} \approx E_{p}\left[\frac{\frac{d}{d p} v^{\prime}\left(c_{\text {pre }}(p)\right)}{v^{\prime}\left(c_{\text {pre }}(p)\right)}\right]
$$

so that the ratio of the labor supply response to $p$ divided by the semi-elasticity of labor supply with respect to wages reveals the average elasticity of the marginal utility function. Assuming this elasticity is roughly constant and noting that a Taylor expansion suggests that for any function $f(x)$, we have $\frac{f(1)-f(0)}{f(0)} \approx \frac{d}{d x} \log (f)$,

$$
\frac{E_{p}\left[\frac{d \Phi}{d p}\right]}{\epsilon^{s e m i}} \approx \frac{v^{\prime}(1)-v^{\prime}(0)}{v^{\prime}(0)}
$$

Now, how does one estimate $\frac{d \Phi}{d p}$ ? Regressing labor force participation, $l$, on $Z$ will generate an attenuated coefficient because of measurement error in $Z$. If the measurement error is classical, one can inflate this by the ratio of the variance of $Z$ to the variance of $P$, or

$$
\frac{v^{\prime}(1)-v^{\prime}(0)}{v^{\prime}(0)} \approx \beta \frac{1}{\epsilon^{\text {semi }}} \frac{\operatorname{var}(Z)}{\operatorname{var}(P)}
$$

APPENDIX TABLE I
Information Realization Between t-2 and t-1 ("First Stage")

|  | Full Sample | Male | Female | Age > 55 | Age $<=55$ | Year < 1997 | Year > 1997 | $\begin{gathered} \text { Male, Age }<=55, \\ \text { Year }<=1997 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (7) |
| Panel 1: Regression of Job Loss on elicitations |  |  |  |  |  |  |  |  |
| Job Loss (Next 12 months) | 0.1968 | 0.1956 | 0.1978 | 0.2079 | 0.1806 | 0.2316 | 0.1829 | 0.2089 |
| s.e. | 0.0120 | 0.0190 | 0.0156 | 0.0159 | 0.0195 | 0.0246 | 0.0140 | 0.0624 |
| Panel 2: Regression of job loss in subsequent 12-24 months on Z |  |  |  |  |  |  |  |  |
| Job Loss (12-24 months) | 0.0937 | 0.0613 | 0.1199 | 0.0893 | 0.0994 | 0.1080 | 0.0847 | 0.0454 |
| s.e. | 0.0120 | 0.0190 | 0.0156 | 0.0159 | 0.0195 | 0.0246 | 0.0140 | 0.0624 |
| Difference | 0.1031 | 0.1343 | 0.0779 | 0.1186 | 0.0812 | 0.1236 | 0.0982 | 0.1635 |
| bootstrap s.e. | 0.0120 | 0.0190 | 0.0156 | 0.0159 | 0.0195 | 0.0246 | 0.0140 | 0.0624 |
| Num of Obs. | 26,640 | 10,740 | 15,900 | 15,506 | 11,134 | 8,571 | 18,069 | 1,210 |

Note: This table presents estimates from regressions of the elicitation, Z, on unemployment measured in both (a) the subsequent 12 months and (b) the subsequent 12 -24 months. The first row corresponds to the heterogeneity in the estimates by subgroup. Columns (2)-(3) restrict the sample to males and females.Columns (4)-(5) restrict the sample to those above and below age 55 . Columns (6)-(7) restrict the sample to before and after 1997. Standard errors are computed using 500 bootstrap repetitions resampling at the household level.

## APPENDIX TABLE II

Maximum Causal Effect of Unemployment on Food Expenditure

|  | Baseline Sample |
| :---: | :---: |
|  | (1) |
| $\begin{aligned} & \text { Estimate for } \max \left\{\log \left(\mathrm{c}_{\mathrm{u}}(\mathrm{p})\right)-\log \left(\mathrm{c}_{\mathrm{e}}(\mathrm{p})\right)\right\}, \Delta^{\min } \\ & \text { s.e. } \end{aligned}$ | $\begin{aligned} & -0.137 \\ & (0.02) \end{aligned}$ |
| Lower bound for drop when unemployed, $\Delta_{\mathrm{u}}^{\text {min }}$ s.e. | $\begin{aligned} & -0.138 \\ & (0.02) \end{aligned}$ |
| Upper bound for increase when unemployed, $\Delta_{\mathrm{e}}{ }^{\text {max }}$ s.e. | $\begin{gathered} -0.001 \\ (0.002) \end{gathered}$ |
| Fraction unemployed with positive consumption change Fraction employed with negative consumption change | $\begin{aligned} & 0.415 \\ & 0.499 \end{aligned}$ |
| Num of Obs. <br> Num of HHs | $\begin{gathered} 65,808 \\ 9,562 \end{gathered}$ |
| Note: This table presents the calculation for the maximum resulting estimate, $\Delta^{\min }$. The second rows present the esti third rows present the estimates for the upper bound for fraction of people who are unemployed, $\mathrm{U}_{\mathrm{it}}=1$, who expe $\mathrm{U}_{\mathrm{it}}=0$, who experience a negative consumption change, $\Delta$ (10nn ranatitinnal | unemployment on er bound on the co sumption when e consumption chang errors are constru |

APPENDIX TABLE III
Alternative Lower Bound Specifications

| Specification: | Baseline | Linear (vs Probit) | Alternative Aggregation Windows |  |  | Alternative Subj. Prob Spec |  | Alternative Outcomes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) |
| $\begin{gathered} \mathrm{E}\left[\mathrm{~T}_{\mathrm{Z}}\left(\mathrm{P}_{\mathrm{Z}}\right)-1\right] \\ \text { s.e. } \end{gathered}$ | $\begin{gathered} 0.7687 \\ (0.058) \end{gathered}$ | $\begin{aligned} & 0.6802 \\ & (0.051) \end{aligned}$ | $\begin{gathered} 0.7716 \\ (0.05) \end{gathered}$ | $\begin{gathered} 0.7058 \\ (0.048) \end{gathered}$ | $\begin{aligned} & 0.7150 \\ & (0.048) \end{aligned}$ | $\begin{aligned} & 0.7462 \\ & (0.051) \end{aligned}$ | $\begin{aligned} & 0.7681 \\ & (0.054) \end{aligned}$ | $\begin{aligned} & 0.5296 \\ & (0.033) \end{aligned}$ | $\begin{gathered} 0.3675 \\ (0.04) \end{gathered}$ | $\begin{aligned} & 0.5790 \\ & (0.086) \end{aligned}$ |
| $\begin{gathered} \mathrm{E}\left[\mathrm{~m}_{\mathrm{z}}\left(\mathrm{P}_{\mathrm{z}}\right)\right] \\ \text { s.e. } \end{gathered}$ | $\begin{aligned} & 0.0239 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0209 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0237 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0217 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0220 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0229 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0236 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0314 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0147 \\ & (0.002) \end{aligned}$ | $\begin{aligned} & 0.0067 \\ & (0.001) \end{aligned}$ |
| p-value | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| $\operatorname{Pr}\{\mathrm{U}=1\}$ | 0.0310 | 0.0307 | 0.0307 | 0.0307 | 0.0307 | 0.0307 | 0.0307 | 0.0593 | 0.0401 | 0.0115 |
| Controls |  |  |  |  |  |  |  |  |  |  |
| Demographics | X | X | X | X | X | X | X | X | X | X |
| Job Characteristics | X | X | X | X | X | X | X | X | X | X |
| Elicitation Specification |  |  |  |  |  |  |  |  |  |  |
| Polynomial Degree | 3 | 3 | 3 | 3 | 3 | 1 | 4 | 3 | 3 | 3 |
| Focal pt dummies (0, 50, 100) | X | X | X | X | X | X | X | X | X | X |
| Aggregation Window | Age x Gender | Age x Gender | Constant | Age x Gender x Industry | Age x Gender x Occupation | Age x Gender | Age x Gender | Age x Gender | Age x Gender | Age x Gender |
| Unemployment Outcome Window | 12 months | 12 months | 12 months | 12 months | 12 months | 12 months | 12 months | 24 months | 6-24 months | 6-12 months |
| Error Specification | Probit | Linear | Probit | Probit | Probit | Probit | Probit | Probit | Probit | Probit |
| Num of Obs. | 25516 | 26640 | 26640 | 26640 | 26640 | 26640 | 26640 | 26640 | 26640 | 26640 |
| Num of HHs | 3467 | 3467 | 3467 | 3467 | 3467 | 3467 | 3467 | 3467 | 3467 | 3467 |

[^6]| Specification |  |  |  | X TABLE IV <br> on of $\mathrm{F}(\mathrm{p} \mid \mathrm{X})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Baseline | Alternative Controls |  | Sub-Samples |  |  |  |  |  |
|  |  | Demo | Health | Age $<=55$ | Age > 55 | Below Median Wage | Above <br> Median Wage | $\begin{gathered} \text { Tenure }>5 \\ \text { yrs } \end{gathered}$ | $\begin{gathered} \text { Tenure }<=5 \\ \text { yrs } \end{gathered}$ |
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) |
| 1st mass |  |  |  |  |  |  |  |  |  |
| Location <br> s.e. | $\begin{gathered} 0.001 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.012 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.002 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.001 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.002 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.007 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.000 \\ (0.000) \end{gathered}$ | $\begin{gathered} 0.022 \\ (0.003) \end{gathered}$ |
| Weight <br> s.e. | $\begin{gathered} 0.446 \\ (0.024) \end{gathered}$ | $\begin{gathered} 0.713 \\ (0.071) \end{gathered}$ | $\begin{gathered} 0.449 \\ (0.054) \end{gathered}$ | $\begin{gathered} 0.437 \\ (0.035) \end{gathered}$ | $\begin{gathered} 0.461 \\ (0.030) \end{gathered}$ | $\begin{gathered} 0.530 \\ (0.032) \end{gathered}$ | $\begin{gathered} 0.452 \\ (0.034) \end{gathered}$ | $\begin{gathered} 0.422 \\ (0.036) \end{gathered}$ | $\begin{gathered} 0.612 \\ (0.034) \end{gathered}$ |
| T(p) | 63.839 | 6.301 | 39.032 | 101.038 | 36.986 | 12.413 | 262.088 | $6.9 \mathrm{E}+08$ | 5.052 |
| s.e. | $6.1 \mathrm{E}+06$ | $1.7 \mathrm{E}+00$ | $1.8 \mathrm{E}+06$ | $1.0 \mathrm{E}+07$ | $1.1 \mathrm{E}+06$ | $3.2 \mathrm{E}+00$ | $7.6 \mathrm{E}+07$ | $2.5 \mathrm{E}+08$ | $6.0 \mathrm{E}-01$ |
| 2nd mass |  |  |  |  |  |  |  |  |  |
| Location | 0.031 | 0.031 | 0.032 | 0.030 | 0.031 | 0.037 | 0.024 | 0.018 | 0.0575 |
| s.e. | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |
| Weight <br> s.e. | $\begin{gathered} 0.471 \\ (0.024) \end{gathered}$ | $\begin{gathered} 0.202 \\ (0.071) \end{gathered}$ | $\begin{gathered} 0.470 \\ (0.052) \end{gathered}$ | $\begin{gathered} 0.483 \\ (0.035) \end{gathered}$ | $\begin{gathered} 0.456 \\ (0.030) \end{gathered}$ | $\begin{gathered} 0.365 \\ (0.032) \end{gathered}$ | $\begin{gathered} 0.486 \\ (0.034) \end{gathered}$ | $\begin{gathered} 0.508 \\ (0.037) \end{gathered}$ | $\begin{gathered} 0.2771 \\ (0.0341) \end{gathered}$ |
| $\mathrm{T}(\mathrm{p})$ | 4.360 | 8.492 | 4.228 | 4.325 | 4.442 | 5.217 | 4.223 | 5.736 | 4.7392 |
| s.e. | 0.203 | 4.194 | 4.576 | 0.306 | 0.279 | 0.417 | 2.181 | 3.008 | 0.5227 |
| 3rd Mass |  |  |  |  |  |  |  |  |  |
| Location <br> s.e. | $\begin{gathered} 0.641 \\ (0.004) \end{gathered}$ | $\begin{gathered} 0.639 \\ (0.004) \end{gathered}$ | $\begin{gathered} 0.642 \\ (0.028) \end{gathered}$ | $\begin{gathered} 0.639 \\ (0.005) \end{gathered}$ | $\begin{gathered} 0.643 \\ (0.005) \end{gathered}$ | $\begin{gathered} 0.626 \\ (0.005) \end{gathered}$ | $\begin{gathered} 0.649 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.641 \\ (0.005) \end{gathered}$ | $\begin{gathered} 0.6420 \\ (0.0055) \end{gathered}$ |
| Weight <br> s.e. | $\begin{gathered} 0.082 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.086 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.081 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.081 \\ (0.003) \end{gathered}$ | $\begin{gathered} 0.083 \\ (0.003) \end{gathered}$ | $\begin{gathered} 0.105 \\ (0.003) \end{gathered}$ | $\begin{gathered} 0.061 \\ (0.003) \end{gathered}$ | $\begin{gathered} 0.070 \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.1105 \\ (0.0040) \end{gathered}$ |
| Controls |  |  |  |  |  |  |  |  |  |
| Demographics | X | X | X | X | X | X | X | X | X |
| Job Characteristics | X |  | X | X | X | X | X | X | X |
| Health Characteristics |  |  | X |  |  |  |  |  |  |
| Num of Obs. | 26,640 | 26,640 | 22,831 | 11,134 | 15,506 | 13,320 | 13,320 | 17,850 | 8,790 |
| Num of HHs | 3,467 | 3,467 | 3,180 | 2,255 | 3,231 | 2,916 | 2,259 | 2,952 | 2,437 |
| Notes: This table presents estimates of the distribution of private information about unemployment risk, P. Column (1) reports the baseline specification. Columns (2) uses only demographic controls; Column (3) uses demographic, job characteristics, and health characteristics. Columns (4)-(9) report results for the baseline specification on various subsamples including below and above age 55 (Columns 4 and 5), above and below-median wage earners (Columns 6 and 7) and above and below 5 years of job tenure. The $F(p)$ estimates report the location and mass given to each point mass, evaluated at the mean $q=\operatorname{Pr}\{U=1\}=0.031$. For example, in the baseline specification, the results estimate a point mass at $0.001,0.031$, and 0.641 with weights $0.446,0.471$ and 0.082 . The values of $\mathrm{T}(\mathrm{p})$ represent the markup that individuals at this location in the distribution would have to be willing to pay to cover the pooled cost of worse risks. All parameter estimates are constructed using maximum likelihood. Because of the nonconvexity of the optimization program, I assess the robustness to 1000 initial starting values. All standard errors are constructed using bootstrap re-sampling using 1000 resamples at the household level. |  |  |  |  |  |  |  |  |  |

## ONLINE APPENDIX FIGURE I: "First Stage" Impact of Unemployment on Beliefs



Notes: This figure presents the estimated coefficients of a regression of the elicitations (elicited in year $t$ ) on unemployment indicators in year $t+j$ for $j=1, . ., 8$. To construct the unemployment indicators for each year $t+j$, I construct an indicator for involuntary job loss in any survey wave (occurring every 2 years). I then use the data on when the job loss occurred to assign the job loss to either the first or second year in between the survey waves. Because of the survey design, this definition potentially misses some instances of involuntary separation that occur in back-to-back years in between survey waves. To the extent to which such transitions occur, the even-numbered years in the Figure are measured with greater measurement error. The figure presents estimated $5 / 95 \%$ confidence intervals using standard errors clustered at the household level.

ONLINE APPENDIX FIGURE II: Impact of Unemployment on Total Consumption Expenditure (2-year intervals)


Notes: This figure presents the estimated coefficients of a regression of leads and lags of log household consumption expenditure on an indicator for unemployment. The figure replicates the sample and specification in Figure IV (Panel B) by replacing the dependent variable with log total consumption expenditure on a sample beginning in 1999, surveyed every two years. I restrict the sample to household heads who are employed in $t-2$ or $t-4$. Following the baseline specification, the sample is restricted to observations with less than a threefold change in consumption expenditures. Note that after 1999, the PSID asks a broader set of consumption questions but is conducted only every two years, which prevents analyzing total 1-year interval responses to unemployment.


Notes: This figure re-constructs the analysis in Figure IV using job loss instead of unemployment. I define job loss as an indicator for being laid off or fired from the job held in the previous wave of the survey. The figure present coefficients from separate regressions of leads and lags of the log change in food expenditure on an indicator of job loss, along with controls for year indicators and a cubic in age. Sample is restricted to household heads who are employed in years $t-1$ and $t-2$.

## ONLINE APPENDIX FIGURE IV: Household Income Pattern Around Unemployment



Notes: This figure presents the estimated coefficients of a regression of leads and lags of log household income on an indicator for unemployment. The figure replicates the sample and specification in Figure IV by replacing the dependent variable with log household income as opposed to the change in log food expenditure. I restrict the sample to household heads who are not unemployed in $t-1$ or $t-2$.

# ONLINE APPENDIX FIGURE V: Illustration of No Trade Condition Using Demand and Average Cost Curves 

## A. MRS versus Average Cost


B. Pooled Price Ratio versus 1 + Willingness to pay (Markup)


Notes: This figure illustrates the no trade condition using the marginal and average cost curves as in Einav, Finkelstein and Cullen (2010). Panel A presents an illustrative example for the demand for a contract that pays $\$ 1$ in the event of becoming unemployed. The willingness to pay out of income if employed is given by the marginal rate of substitution, $\frac{p}{1-p} \frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}$. Under a standard single crossing condition, all types $P \geq p$ would also purchase the insurance policy (see text for discussion of multi-dimensional heterogeneity). Therefore, the cost to the insurer of the contract is given by the average likelihood that the payment is made, $E[P \mid P \geq p]$ relative to the likelihood the payment is received, $1-E[P \mid P \geq p], \frac{E[P \mid P \geq p]}{1-E[P \mid P \geq p]}$. Panel B normalizes by $\frac{1-p}{p}$ to illustrate the empirical approach that compares the pooled price ratio, $T(p)=\frac{1-p}{p} \frac{E[P[P \geq p]}{1-E[P \mid P \geq p]}$, to one plus the markup individuals are willing to pay for insurance, $\frac{u^{\prime}\left(c_{u}(p)\right)}{v^{\prime}\left(c_{e}(p)\right)}$. The empirical results suggest the willingness to pay lies below the pooled price ratio, as depicted in Panels A and B.

ONLINE APPENDIX FIGURE VI: Distribution of Reported Log Food Expenditure Growth, $\Delta_{i t}^{*}$, for Employed and Unemployed
A. Unemployed $\left(U_{i t}=1\right)$


Notes: This figure plots histograms of $\Delta_{i t}^{*}$ for those who are employed, $U_{i t}=0$, and unemployed, $U_{i t}=1 . \Delta_{i t}^{*}$ is defined as the residual from a regression of $\log \left(c_{i t}\right)-\log \left(c_{i t-1}\right)$ on an age cubic and year dummies, $X$. I restrict the sample to household heads who are employed in $t-1$ and $t-2$. Following the baseline specification, the sample is restricted to observations with less than a threefold change in consumption expenditures.


[^0]:    ${ }^{47}$ Note that, because of the envelope theorem, the individual's valuation of this small insurance policy is independent of any behavioral response. While these behavioral responses may impose externalities on the insurer or government, they do not affect the individuals' willingness to pay.
    ${ }^{48}$ To incorporate observable characteristics, one should think of the expectations as drawing from the distribution of $\theta$ conditional on a particular observable characteristic, $X$.

[^1]:    ${ }^{49}$ See Appendix A. 3 for a micro-foundation of this assumption.
    ${ }^{50}$ In other words, the random variable $P$ is simply the random variable generated by the choices of probabilities, $p(\theta)$, in the population.

[^2]:    ${ }^{51}$ If $\tilde{p}$ is not strictly increasing (e.g. because of "advantageous selection"), it will be strictly more profitable to an insurance company to sell the insurance at a higher price. Hence, one need not test the no trade condition for such intermediate values of $\frac{d \tau}{d b}$ where $\tilde{p}$ is decreasing in $p$.

[^3]:    ${ }^{52}$ Moreover, it allows the statistical model to easily impose unbiased beliefs, so that $\operatorname{Pr}\{U \mid X\}=E[P \mid X]$ for all $X$.
    ${ }^{53}$ This has the advantage that it does not require integrating over high degree of curvature in the likelihood function. In practice, it will potentially under-state the true variance in $P$ in finite sample estimation. As a result, it will tend to produce lower values for $T(p)$ than would be implied by continuous probability distributions for $P$ since the discrete approximation allows all individuals at a particular point mass to be able to perfectly pool together when attempting to cover the pooled cost of worse risks.

[^4]:    ${ }^{54}$ This "left-hand-side" measurement error was necessarily not a problem for estimating the mean consumption impact of unemployment (assuming the error is classical). But, for estimating properties of the distribution of consumption changes such as minima and maxima, this measurement error becomes a significant limitation.
    ${ }^{55}$ This residualization can be formalized by assuming there are known time and year preference shocks affecting the marginal utility of consumption that are common across individuals. Note the residuals now satisfy the ex-ante Euler equation, $E\left[\Delta_{i t}^{*}\right]=0$. But, the means of the residuals will differ for those who do and do not experience unemployment, $E\left[\Delta_{i t}^{*} \mid U_{i t}=1\right] \leq 0$ and $E\left[\Delta_{i t}^{*} \mid U_{i t}=0\right] \geq 0$.

[^5]:    ${ }^{56}$ While the symmetry assumption is not directly testable, it can be micro-founded from many common assumptions on measurement error distributions. For example, if the true distribution of consumption changes is symmetric and the distribution of measurement error is symmetric and unbiased, then it is straightforward to show that $\operatorname{Pr}\left\{\Delta_{i t}^{*} \leq \Delta_{u}^{\min } \mid U_{i t}=1\right\} \geq \operatorname{Pr}\left\{\Delta_{i t}^{*} \geq x \mid U_{i t}=1\right\}$, where $x \leq 0$ is the maximum consumption change for those who become unemployed. Symmetric and median-unbiasedness is a common assumption measurement error models (see, e.g., Bollinger (1998); Hu and Schennach (2008)).

[^6]:    
    
    
    
    
     Column (10) defines unemployment as an indicator for job loss in the 6-12 months after the survey wave.

