## Online Appendix of

# Measuring Discounting without Measuring Utility 

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## Online Appendix WA: Further Details for the DM

## WA1. Details of Rounding in the DM Method

As is common with choice lists today, subjects were not given the possibility to express indifference. The latter possibility is known to generate confusions and to be hard to incentivize. Preferences $\alpha_{\{1, \ldots, 24\}} 0<\alpha_{\{25, \ldots, 52\}} 0$ and $\alpha_{\{1, \ldots, 25\}} 0>\alpha_{\{26, \ldots, 52\}} 0$ reveal that $\mathrm{c}_{1 / 2}$ is in the interval $(24,25]$. We denote upper bounds of such intervals by $u$, so that here we write $u_{1 / 2}=25$. As is common, we will use midpoints as estimates. Thus $\mathrm{u}_{1 / 2}-1 / 2$ is our estimate of $\mathrm{c}_{1 / 2}$, which is 24.5 in the above case.

In our adaptive experiment, we only presented integer week durations to subjects, and no noninteger such as $u_{1 / 2}-1 / 2$. Hence we could not use our best approximation $\mathrm{u}_{1 / 2}-1 / 2$ of $\mathrm{c}_{1 / 2}$ in follow-up questions, but had to use an integer approximation. So as to stay away from extreme values we used the convention of rounding values upward for time durations in the first half year and downward for time durations in the second half year. Those rounded integer values were presented to our subjects in the adaptive experiment. We of course correct for the generated and propagated rounding errors in our analyses. We next give details.

We follow the notation of the main text and denote time intervals as $(0, x]$ or, equivalently, as a set $\{1, \ldots, x\}$ of weeks. Similarly, ( $\mathrm{x}, 52]$ denotes $\{\mathrm{x}+1, \ldots, 52\}$. Note that week $x+1$ runs from time point $x$ until time point $x+1$, so that its left starting point is x and not $\mathrm{x}+1$.

For estimating $\mathrm{c}_{1 / 2}$ we measured the subjective midpoint of $(0,52]=\{1, \ldots, 52\}$. The preference switch (and subjective interval-midpoint) was between $u_{1 / 2}-1$ and $u_{1 / 2}$, referring to the notation of the integer $u_{1 / 2}$ introduced before. Thus, for each subject, $\mathrm{u}_{1 / 2}$ was such that
$\left(0, \mathrm{u}_{1 / 2}-1\right]=\left\{1, \ldots, \mathrm{u}_{1 / 2}-1\right\}<\left\{\mathrm{u}_{1 / 2}, \ldots, 52\right\}=\left(\mathrm{u}_{1 / 2}-1,52\right]$
and
$\left(0, \mathrm{u}_{1 / 2}\right]=\left\{1, \ldots, \mathrm{u}_{1 / 2}\right\}>\left\{\mathrm{u}_{1 / 2}+1, \ldots, 52\right\}=\left(\mathrm{u}_{1 / 2}, 52\right]$.
We then assume
( $\left.0, \mathrm{u}_{1 / 2}-1 / 2\right] \sim\left(\mathrm{u}_{1 / 2}-1 / 2,52\right]$ and, hence, estimate
$c_{1 / 2}=u_{1 / 2}-1 / 2$.

To estimate $\mathrm{c}_{1 / 4}$, we measured the preference-midpoint of $\left(0, \mathrm{u}_{1 / 2}\right.$ (weeks $\left\{1, \ldots, \mathrm{u}_{1 / 2}\right\}$ ), denoted $\mathrm{u}_{1 / 4}-1 / 2$, similarly as above. There is a propagation of roundings here, as follows. $u_{1 / 2}$ overestimates $c_{1 / 2}$ by $1 / 2$ (on average, as always) as we saw, implying that the midpoint of $\left(0, \mathrm{u}_{1 / 2}\right]$ will overestimate $\mathrm{c}_{1 / 4}$ by $1 / 4$. Hence we subtract $1 / 4$ from the subjective midpoint $u_{1 / 4}-1 / 2$, and estimate
$\mathrm{c}_{1 / 4}=\mathrm{u}_{1 / 4}-3 / 4$.

To estimate $\mathrm{c}_{1 / 8}$, we measured the preference-midpoint of $\left(0, \mathrm{u}_{1 / 4}\right\}$ (weeks $\left\{1, \ldots, \mathrm{u}_{1 / 4}\right\}$ ), denoted $u_{1 / 8}-1 / 2$. Because $u_{1 / 4}$ overestimates $c_{1 / 4}$ by $3 / 4$ as we saw, the subjective midpoint of $\left(0, u_{1 / 4}\right]$ will overestimate $c_{1 / 8}$ by $3 / 8$. Hence we estimate
$c_{1 / 8}=u_{1 / 8}-7 / 8$.

To estimate $\mathrm{c}_{\frac{3}{4}}$, we measured the preference midpoint of ( $\mathrm{u}_{1 / 2}-1,52$ ] (weeks $\left\{u_{1 / 2}, \ldots, 52\right\}$ ), denoted $u_{3 / 4}-1 / 2$. Because $u_{1 / 2}-1$ underestimates $c_{1 / 2}$ by $1 / 2$, the preference midpoint underestimates $c_{3 / 4}$ by $1 / 4$, which is to be added to $u_{3 / 4}-1 / 2$. Hence we estimate $\mathrm{C}_{3 / 4}=\mathrm{u}_{34}-1 / 4$.

To estimate $\mathrm{c}_{7 / 8}$, we measured the preference midpoint of ( $\mathrm{u}_{3_{4}}-1,52$ ] (weeks
$\left\{\mathrm{u}_{34}, \ldots, 52\right\}$ ), denoted $\mathrm{u}_{1 / 8}-1 / 2$. Because $\mathrm{u}_{3 / 4}-1$ underestimates $\mathrm{c}_{3_{4}}$ by $3 / 4$, the preference midpoint underestimates $\mathrm{c}_{7 / 8}$ by $3 / 8$, which is to be added to $\mathrm{u}_{1 / 8}-1 / 2$. Hence we estimate $\mathrm{C}_{1 / 8}=\mathrm{u}_{1 / 8}-1 / 8$.

For the first separability test, we obtained an estimate $s_{1 / 2}$ of $c_{1 / 2}$ alternative to the one obtained before. We now measured the preference midpoint of ( $u_{1 / 4}-1, u_{3_{4}}$ (weeks $\left\{\mathrm{u}_{1 / 4}, \ldots, \mathrm{u}_{3 / 4}\right\}$ ), denoted $\mathrm{s}^{1 / 1 / 2}-1 / 2$. Because $\mathrm{u}_{1 / 4}-1$ underestimates $\mathrm{c}_{1 / 4}$ by $1 / 4$, and $\mathrm{u}_{3 / 4}$ overestimates $\mathrm{c}_{3 / 4}$ by $1 / 4$, the preference midpoint is a good estimate of $\mathrm{c}_{1 / 2}$. That is, we estimated
$\mathrm{s}_{1 / 2}\left(\right.$ alternative for $\left.\mathrm{c}_{1 / 2}\right)=\mathrm{s}^{1 / 1 / 2}-1 / 2$.

For the second separability test, we did not measure a subjective midpoint of a time interval. We obtained an alternative measurement $\mathrm{s}_{\frac{3}{4}}$ of $\mathrm{c}_{3}$, as follows. The basic idea is to find $\mathrm{s}_{3_{4}}$ such that $\left(0, \mathrm{u}_{1 / 4}\right] \sim\left(\mathrm{s}_{3 / 4}, 52\right.$. Roundings are as follows. We found the value $\mathrm{s}^{2}{ }_{3 / 4}$ such that
$\left\{\mathrm{s}_{3_{4}+1}+\ldots, 52\right\}=\left(\mathrm{s}^{2}{ }_{3_{4}, 52}\right]<\left(0, \mathrm{u}_{1 / 4}\right]=\left\{1, \ldots, \mathrm{u}_{1 / 4}\right\}<\left\{\mathrm{s}_{3_{4}, \ldots, 52}^{2}\right\}=\left(\mathrm{s}_{3_{4}-1,52}^{2}\right]$. We estimate
$\left(\mathrm{s}_{3 / 4}^{2}-1 / 2,52\right] \sim\left(0, \mathrm{u}_{1 / 4}\right]$.
Because $u_{1 / 4}$ overestimates $c_{1 / 4}$ by $3 / 4, \mathrm{~s}_{3 / 4}^{2}-1 / 2$ will underestimate $\mathrm{c}_{3 / 4}$ by $3 / 4$. We thus estimate
$\mathrm{S}_{3 / 4}\left(\right.$ alternative for $\left.\mathrm{C}_{3 / 4}\right)=\mathrm{s}_{3_{4}}+1 / 4$.

## WA2. Details of Qualitative Preference Conditions for the DM

We first give the p-values obtained.
TEST 1: $\mathrm{H}_{0}: \mathrm{c}_{1 / 2} \geq 26$ (no or negative impatience) is rejected to the favor of $\mathrm{H}_{1}: \mathrm{c}_{1 / 2}<26$ (impatience; $\mathrm{p}<0.001$ ).

TEST 2: $\mathrm{H}_{0}: \mathrm{c}_{1 / 4} \geq \mathrm{c}_{1 / 2} / 2$ (no or negative impatience) is rejected to the favor of $\mathrm{H}_{1}: \mathrm{c}_{1 / 4}<$ $\mathrm{C}_{1 / 2} / 2$ (impatience; $\mathrm{p}<0.001$ ).
TEST 3: $\mathrm{H}_{0}: \mathrm{c}_{1 / 2} \geq\left(\mathrm{c}_{1 / 4}+\mathrm{c}_{3 / 4}\right) / 2$ (no or negative impatience) is marginally rejected to the favor of $\mathrm{H}_{1}: \mathrm{c}_{1 / 2}<\left(\mathrm{c}_{1 / 4}+\mathrm{c}_{3 / 4}\right) / 2$ (impatience; $\mathrm{p}=0.09$ ).
TEST 4: $\mathrm{H}_{0}: \mathrm{c}_{3 / 4} \geq\left(\mathrm{c}_{1 / 2}+52\right) / 2$ (no or negative impatience) is rejected to the favor of $\mathrm{H}_{1}$ : $\mathrm{c}_{3 / 4}<\left(\mathrm{c}_{1 / 2}+52\right) / 2$ (impatience; $\mathrm{p}<0.001$ ).

TEST 5. $\mathrm{H}_{0}: \mathrm{c}_{1 / 8} \geq \mathrm{c}_{1 / 4} / 2$ (no or negative impatience) is rejected to the favor of $\mathrm{c}_{1 / 8}<\mathrm{c}_{1 / 4} / 2$ (impatience; $\mathrm{p}=0.001$ ).

TEST 6. $\mathrm{H}_{0}: \mathrm{c}_{7 / 8}<\left(52+\mathrm{c}_{3 / 4}\right) / 2$ (no or negative impatience) is rejected to the favor of $\mathrm{c}_{7 / 8}<$ $\left(52+\mathrm{c}_{34}\right) / 2$ (impatience; $\mathrm{p}<0.001$ ).
Test 7. We tested constant impatience by comparing impatience in ( $0, \mathrm{c}_{1 / 2}$ ] versus $\left(\mathrm{c}_{1 / 2}, 52\right]$, testing $\mathrm{c}_{1 / 2} / 2-\mathrm{c}_{1 / 4}=\left(\mathrm{c}_{1 / 2}+52\right) / 2-\mathrm{c}_{3 / 4}$ two-sided. We found constant impatience rejected to the favor of decreasing impatience (with > instead of $=; \mathrm{p}<0.001$ ).
TEST 8. We tested constant impatience by comparing impatience in ( $0, \mathrm{c}_{1 / 4}$ ] versus $\left(\mathrm{c}_{3 / 4}, 52\right]$, testing $\left.\mathrm{c}_{1 / 4} / 2-\mathrm{c}_{1 / 8}=\left(\mathrm{c}_{3 / 4}+52\right) / 2-\mathrm{c}_{1 / 8}\right)$ two-sided. We found constant impatience rejected to the favor of increasing impatience (with <instead of $=; \mathrm{p}=0.001$ ).

TEST 9. For separability, we tested $\mathrm{s}_{1 / 2}=\mathrm{c}_{1 / 2}$, but rejected it ( $\mathrm{p}<0.01$ ) to the favor of $\mathrm{s}_{1 / 2}$ $<\mathrm{C}_{1 / 2}$.
TEST 10. For separability, we tested $\mathrm{s}_{\frac{3}{4}}=\mathrm{c}_{3}$, which was accepted $(\mathrm{p}=0.14)$.

We next discuss an alternative rounding assumption for testing qualitative preference conditions. There was a considerable group of subjects who had $u_{1 / 4}=13$, $\mathrm{u}_{1 / 2}=26$, and $\mathrm{u}_{3 / 4}=39$, being 37 subjects. It suggests that many of these subjects are constant or very weak discounters, and our roundings may have been too much downward for them. Some hypotheses that we tested could have been favored or disfavored by the rounding chosen for these subjects. Hence we repeated all tests
with the 60 subjects that remained after removing those 37 subjects. Removing subjects with constant discounting as done here should not affect the directional hypotheses tested. We found the same conclusions, with the same p-values, with the following exceptions. The main changes concern the tests of constant impatience. The decreasing impatience in test $7\left(\mathrm{c}_{3 / 4}-26-\mathrm{c}_{1 / 4}>0\right)$ is no more significant $(\mathrm{p}=0.22$ two-sided), and neither is the increasing impatience in test $8\left(\mathrm{c}_{1 / 4} / 2-\mathrm{c}_{1 / 8}>\left(\mathrm{c}_{3 / 4}+52\right) / 2-\right.$ $\left.\mathrm{c}_{7 / 8}\right)(\mathrm{p}=0.19$ two-sided $)$. Some minor changes: Test $5\left(\mathrm{c}_{3 / 4}<\left(\mathrm{c}_{1 / 2}+52\right) / 2\right)$ now has $\mathrm{p}=$ 0.003 ; test $9\left(\mathrm{~s}_{1 / 2}=\mathrm{c}_{1 / 2}\right)$ now has $\mathrm{p}=0.017$; test $10\left(\mathrm{~s}_{1 / 4}=\mathrm{c}_{1 / 4}\right)$ now has $\mathrm{p}=0.81$.

## WA3. Further Results for the DM

The interval midpoints used in the graph of the discount factors that were derived from the cumulative discount weighting are $2.77,8.51,17.96,31.12,41.13$, and 48.25 weeks, respectively. The corresponding discount factors for the vertical axis are 1 , $0.94,0.855,0.835,0.826$, and 0.74 .

For all $\mathrm{c}_{\mathrm{p}}$ values, all the median values exceed the mean values, indicating negative skewness with the left tail longer than the right tail. It is confirmed by histogram and kernel density functions in Figure WA1.

Figure WA1. Histograms and kernel density curves for the $c_{p}$ observations


Negative skewness is confirmed by the skewness/kurtosis tests for normality, with p< 0.05 for all kurtosis tests and four of the five skewness tests, and $\mathrm{p}=0.09$ for the remaining skewness test. Therefore, no $\mathrm{c}_{\mathrm{p}}$ is normally distributed.

Table WA1

| Skewness/Kurtosis tests for Normality_DM |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Variable | Observations | $\operatorname{Pr}$ (Skewness) | $\operatorname{Pr}$ (Kurtosis) | Joint |  |
|  |  |  |  | Adj chi2(2) | Prob > chi2 |
| $\mathrm{c}_{1 / 8}$ | 97 | 0.0924 | 0.0370 | 6.66 | 0.0358 |
| $\mathrm{c}_{1 / 4}$ | 97 | 0.0000 | 0.0008 | 28.22 | 0.0000 |
| $\mathrm{c}_{1 / 2}$ | 97 | 0.0000 | 0.0000 | 39.42 | 0.0000 |
| $\mathrm{c}_{3 / 4}$ | 97 | 0.0000 | 0.0000 | 33.28 | 0.0000 |
| $\mathbf{c}_{7 / 8}$ | 97 | 0.0002 | 0.0126 | 16.21 | 0.0003 |

We next give the statistics showing that the difference between the area under the DM cumulative discount weight function and the area under the diagonal is positive, confirming impatience.

Table WA2
Signrank DM_area $=0$
Wilcoxon signed-rank test

| Sign | Obervations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 81 | 4221 | 2327.5 |
| Negative | 14 | 434 | 2327.5 |
| Zero | 1 | 1 | 1 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties -1148.25
adjustment for zeros $\quad-0.25$
adjusted variance 73735.50
$\mathrm{H}_{0}$ :

$$
\begin{aligned}
\text { DM_area } & =0 \\
z & =6.97 \\
\text { Prob }> & z=0.0000
\end{aligned}
$$

## WA4. The Control Question

After subjects had completed a choice list, they clicked on a "submit my choices" button to go to the next page, which showed an implication of their choices (Figure WA2). For instance, if a subject chose as in Figure 1 in the main text, with indifference value 5.5 , then after clicking the "submit my choices" button, the page shown in Figure WA2 appeared. Subjects had to confirm the implied preferences to go to the next question. If they did not confirm, they went back to the previous page and filled out the choice list again.

Figure WA2. Implication of the choice

| Your choices mean that you prefer to |
| :---: |
| gain $€ 20$ per week, starting week 1 and ending (after) week 6 [6] |
| rather than |
| gain $€ 20$ per week, starting week 7 and ending (after) week 13 [7] |
| Are you sure about your choices? |
| Yes, go to the next question |
| No, go back to the previous question |

## Online Appendix WB: Further Details for the UM

For each variable $\mathrm{d}_{\mathrm{j}}^{\mathrm{u}}$, the median is larger than the mean, indicating negative skewness and failure of normal distribution. The following table confirms this using statistical tests, and rejecting normal distributions.

TABLE WB1. Skewness/kurtosis tests rejecting normality of UM observations

| Skewness/Kurtosis tests for Normality_UM |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Joint |  |
| Variable | Observations | $\operatorname{Pr}$ (Skewness) | $\operatorname{Pr}$ (Kurtosis) | Adj chi2(2) | Prob>chi2 |
| $\mathrm{d}_{4}^{\mathrm{u}}$ | 96 | 0 | 0.0004 | 33.81 | 0 |
| $\mathrm{d}_{12}^{\mathrm{u}}$ | 96 | 0 | 0.06 | 16.94 | 0.0002 |
| $\mathrm{d}_{20}^{\mathrm{u}}$ | 96 | 0.0001 | 0.13 | 14.23 | 0.0008 |
| $\mathrm{d}_{28}^{\mathrm{u}}$ | 96 | 0.01 | 0.14 | 7.72 | 0.02 |
| $\mathrm{d}_{36}^{\mathrm{u}}$ | 96 | 0.04 | 0.004 | 10.94 | 0.004 |
| $\mathrm{d}_{44}^{\mathrm{u}}$ | 96 | 0.046 | 0.002 | 11.45 | 0.003 |
| $\mathrm{d}_{52}^{\mathrm{u}}$ | 96 | 0.13 | 0.0001 | 14.72 | 0.0006 |

By impatience, switching values $\lambda$ in $90_{3} 0 \sim \lambda_{j} 0$ should be increasing in duration j. 15 subjects violate this requirement at least once.

The weeks used in the graph of the discount factors are $3,4,12,20,28,36,44$ and 48.25 weeks ${ }^{1}$. The corresponding discount factors for the vertical axis are $1,0.93$, $0.874,0.84,0.79,0.77,0.75$ and 0.74 . The latter value suggests an annual discount factor of $30 \%$.

Wilcoxon signed-rank tests confirmed impatience (discount factors decreasing over time) by comparing each consecutive discount factor. Impatience is confirmed (always $\mathrm{p}=0.0000$ ).

[^0]Table WB2
Signrank $d_{4}=d_{12}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 52 | 3618 | 1855 |
| Negative | 1 | 92 | 1855 |
| Zero | 43 | 946 | 946 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros -6858.50
adjusted variance 68025.50
$H_{0}: d_{4}=d_{12}$
$z=6.76$
Prob $>\mathrm{z}=0.0000$

## Table WB3

Signrank $d_{12}=d_{20}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 44 | 3224 | 1690.5 |
| Negative | 2 | 157 | 1690.5 |
| Zero | 50 | 1275 | 1275 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad 0.00$
adjustment for zeros -10731.25
adjusted variance 64152.75
$H_{0}: d_{12}=d_{20}$

$$
\begin{aligned}
z & =6.05 \\
\text { Prob }>z & =0.0000
\end{aligned}
$$

Table WB4
Signrank $d_{20}=d_{28}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 57 | 3875 | 1957.5 |
| Negative | 1 | 40 | 1957.5 |
| Zero | 38 | 741 | 741 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros -4754.75
adjusted variance 70129.25

Table WB5
$\mathrm{H}_{0}: \mathrm{d}_{28}=\mathrm{d}_{36}$

$$
\begin{aligned}
z & =7.24 \\
\operatorname{Prob}>z & =0.0000
\end{aligned}
$$

Signrank $\mathrm{d}_{28}=\mathrm{d}_{36}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 40 | 2916 | 1715.5 |
| Negative | 7 | 515 | 1715.5 |
| Zero | 49 | 1225 | 1225 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad 0.00$
adjustment for zeros -10106.25
adjusted variance 64777.75
$\mathrm{H}_{0}: \quad d_{28}=d_{36}$

$$
z=4.72
$$

Prob $>\mathrm{z}=0.0000$

Table WB6
Signrank $d_{36}=d_{44}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 47 | 3306 | 1855 |
| Negative | 6 | 404 | 1855 |
| Zero | 43 | 946 | 946 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros $\quad-6858.50$
adjusted variance 68025.50
$H_{0}: d_{36}=d_{44}$

$$
z=5.56
$$

Prob $>\mathrm{z}=0.0000$

Table WB7
Signrank $d_{44}=d_{52}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 37 | 2801 | 1612.5 |
| Negative | 6 | 424 | 1612.5 |
| Zero | 53 | 1431 | 1431 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad 0.00$
adjustment for zeros -12759.75
adjusted variance 62124.25
$H_{0}: d_{36}=d_{44}$

$$
z=4.77
$$

Prob $>\mathrm{z}=0.0000$

We next give the statistics showing that the difference between the area under the UM cumulative discount weight function and the area under the diagonal is positive, confirming impatience.

Table WB8
Signrank UM_area $=0$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 96 | 4656 | 2328 |
| Negative | 0 | 0 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-0.13$
adjustment for zeros 0.00
adjusted variance 74883.88
$\mathrm{H}_{0}$ : UM_area $=0$
$z=8.51$
Prob $>|z|=0.0000$

## Online Appendix WC: Further Details in Comparing the DM and the UM

## WC1. Regressions

To see how concavity of the cumulative discount weights is related to individual characteristics, we regress (1) DM_area, (2) UM_area and (3) difference between the two areas on risk preference parameters $(\alpha, \beta, 1-\eta)$ and demographics (gender, age, nationality (Dutch/non-Dutch)). The following table gives the results.

TABLE WC1. LS regression of areas on risk preference parameters and demographics

|  | (1) | (2) | (3) |
| :---: | :---: | :---: | :---: |
| $\alpha$ | -0.63 | 0.24 | -0.88 |
|  | (0.66) | (0.48) | (0.72) |
| Pessimism | 0.13 | $-2.47 * * *$ | 2.60 * |
|  | (1.22) | (0.88) | (1.33) |
| Concavity of Utility | -0.12 | -1.21 *** | 1.09 *** |
|  | (0.28) | (0.21) | (0.31) |
| Nation | 0.28 | -0.15 | 0.43 |
| (1: Dutch; 0: Other) | (0.38) | (0.28) | (0.42) |
| Gender | -0.16 | -0.27 | 0.11 |
| (1: Male; 0: Female) | (0.39) | (0.28) | (0.42) |
| Age | 0.10 | 0.15 *** | -0.05 |
|  | (0.07) | (0.05) | (0.08) |
| Constant | -0.83 | 1.41 | -2.23 |
|  | (1.99) | (1.44) | (2.17) |
| $\mathrm{R}^{2}$ | 0.03 | 0.40 | 0.21 |
| Observations | 96 | 96 | 96 |

[^1]Column (1) shows that none of the parameters in risk preference or demographics have impact on DM time preference. Column (2) shows that UM time preference is
related with pessimism in probability weighting and concavity of utility and also age. Column (3) shows that the difference between the two areas is related to concavity of utility. There is no correlation between age and concavity of utility ( $\mathrm{p}=0.16$ ), and also no correlation between gender and concavity of utility ( $p=0.46$ ).

## WC2. Further Details

The discount factors of 48.25 weeks in the DM and that in the UM suggest that the mean (median) of discount factors of 52 weeks $\left(\delta_{52}\right)$ is $0.756(0.839)$ for the DM and 0.716 ( 0.748 ) for the UM. A Wilcoxon test shows that subjects' discounting in the DM and in the UM does not differ significantly ( $\mathrm{p}=0.87$ ).

Table WC2
Signrank DM_d ${ }_{52}=$ UM_d ${ }_{52}$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 46 | 2374 | 2328 |
| Negative | 50 | 2282 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | ---: |
| adjustment for ties | 0.00 |
| adjustment for zeros | 0.00 |

adjusted variance 74884.00
$H_{0}: D M \_d_{52}=U M \_d_{52}$

$$
z=0.17
$$

$$
\text { Prob }>z=0.87
$$

Histograms of discount factors are provided next.

Figure WC1


We calculate annual discount rates r from $\mathrm{e}^{-\mathrm{rt}}=\delta_{52}$. The mean (median) of r is $0.409(0.175)$ for the DM and $0.390(0.291)$ for the UM. The difference is not significant $(\mathrm{p}=0.74)$.

Table WC3
Signrank DM_r ${ }_{52}=U M \_r_{52}$
Wilcoxon signed-rank test

| Sign | Observations | Sum | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 50 | 2418 | 2328 |
| Negative | 46 | 2238 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | ---: |
| adjustment for ties | 0.00 |
| adjustment for zeros | 0.00 |

adjusted variance 74884.00
$H_{0}: D M \_r_{52}=U M \_r_{52}$

$$
z=0.33
$$

$$
\operatorname{Prob}>z=0.74
$$

DM_area and UM_area are the difference between area under the DM/UM cumulative discount weighting functions and area under the diagonal. Here is the output of the test showing that the UM area exceeds the DM area.

Table WC4
signrank UM_area = DM_area
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 55 | 2980 | 2328 |
| Negative | 41 | 1676 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 74884.00
$\mathrm{H}_{0}$ : UM_area = DM_area
$z=2.38$
Prob $>\mathrm{z}=0.02$

Here is the output of the test showing that the power function fitted to the DM area has a power different than 1 , confirming concavity of C .

## Table WC5

signrank DM_power = 1
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 10 | 307 | 2328 |
| Negative | 86 | 4349 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | :---: |
| adjustment for ties | -749.50 |
| adjustment for zeros | 0.00 |

adjusted variance 74134.500
$\mathrm{H}_{0}$ : DM_power = 1

$$
\begin{aligned}
z & =-7.42 \\
\operatorname{Prob}>z & =0.0000
\end{aligned}
$$

Here is the output of the test showing that the power function fitted to the UM area has a power different than 1 , confirming concavity of $\mathrm{C}^{\mathrm{u}}$.

## Table WC6

signrank UM_power = 1
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 0 | 0 | 2328 |
| Negative | 96 | 4656 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-0.13$
adjustment for zeros 0.00
adjusted variance 74883.88
$\mathrm{H}_{0}$ : UM_power = 1

$$
\begin{aligned}
z & =-8.51 \\
\operatorname{Prob}>z & =0.0000
\end{aligned}
$$

Here is the output of the test showing that the power function fitted to the UM area is not significantly different from that fitted to the DM area.

Table WC7
signrank UM_power = DM_power
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 50 | 2140 | 2328 |
| Negative | 46 | 2516 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad 0.00$
adjustment for zeros 0.00
adjusted variance 74884.00
$H_{0}$ : UM_power = DM_power

$$
z=-0.69
$$

Prob $>z=0.492$

The following table shows the correlation $\rho$ between discount rate $r$,
DM_area/UM_area, and concavity of C. Capital P designates p-value.

Table WC8

|  | r(DM) | area(DM) | concavity(DM) | r(UM) | area(UM) | concavity(UM) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r(DM) |  | $\mathrm{P}=0.000$ | $\mathrm{P}=0.000$ | $\mathrm{P}=0.008$ | $\mathrm{P}=0.01$ | $\mathrm{P}=0.03$ |
|  |  | $\rho=0.96$ | $\rho=-0.90$ | $\rho=0.27$ | $\rho=0.26$ | $\rho=-0.21$ |
| area(DM) | ----- | ----- | $\mathrm{P}=0.000$ | $\mathrm{P}=0.02$ | $\mathrm{P}=0.02$ | $\mathrm{P}=0.046$ |
|  |  |  | $\rho=-0.90$ | $\rho=0.25$ | $\rho=0.24$ | $\rho=-0.20$ |
| concavity(DM) | ----- | ----- | ----- | $\mathrm{P}=0.007$ | $\mathrm{P}=0.001$ | $\mathrm{P}=0.004$ |
|  |  |  |  | $\rho=-0.34$ | $\rho=-0.32$ | $\rho=0.29$ |
| r(UM) | ----- | ----- | ----- |  | $\mathrm{P}=0.000$ | $\mathrm{P}=0.000$ |
|  |  |  |  |  | $\rho=0.99$ | $\rho=-0.96$ |
| area(UM) | ----- | ----- | ----- | ----- | ----- | $\mathrm{P}=0.000$ |
|  |  |  |  |  |  | $\rho=-0.95$ |
| concavity(UM) | ----- | ----- | ----- | ----- | ----- | ----- |

## Online Appendix WD: Statistics for Parametric Fittings

The following table gives descriptives of parametric fittings of discounting on the individual level.

Table WD1

| Variable | Mean | Min | Median | Max | SD |
| ---: | ---: | ---: | ---: | ---: | ---: |
| r (exponential; UM) | 0.009 | 0.000 | 0.006 | 0.046 | 0.009 |
| $\alpha$ (hyperbolic; UM) | 1.876 | 0.000 | 1.214 | 8.222 | 2.139 |
| $\beta$ (hyperbolic; UM) | 0.249 | 0.000 | 0.055 | 3.981 | 0.557 |
| d (unit invariance; UM) | 0.576 | -9.401 | 0.938 | 3.719 | 1.352 |
| r (unit invariance; UM) | 2.190 | 0.000 | 0.692 | 18.193 | 3.411 |
| r (exponential; DM) | 0.005 | -0.012 | 0.002 | 0.037 | 0.008 |
| $\alpha$ (hyperbolic; DM) | 1.663 | 0.000 | 1.297 | 9.770 | 2.497 |
| $\beta$ (hyperbolic; DM) | 0.139 | -0.012 | 0.049 | 1.650 | 0.261 |
| d (unit invariance; DM) | 0.801 | -1.281 | 0.893 | 1.954 | 0.490 |
| r (unit invariance; DM) | 1.858 | 0.000 | 0.246 | 19.982 | 2.970 |

We next present tests for heteroskedasticity. We fitted three models for both UM data and DM data. The following figure displays the error term of the exponential model for UM data.

Figure WD1


Levene's test of equality of variances rejects the null hypothesis that absolute deviations from the medians are the same across time ( $p<0.01$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_exponential_UM
Test Statistic $=5.28, \mathrm{p}=2.46 \mathrm{e}-05$

We now present the error term of the hyperbolic model for the UM.

Figure WD2


For the hyperbolic discounting model, Levene's test cannot reject the null that absolute deviations from the medians are the same across time ( $p>0.05$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_hyperbolic_UM
Test Statistic $=2.00, \mathrm{p}=0.06$

The following figure shows the error term of the unit invariance model for the UM.

Figure WD3


Levene's test cannot reject the null that absolute deviations from the medians are the same ( $p>0.05$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_unit.invariance_UM
Test Statistic $=1.98, \mathrm{p}=0.07$

The following figure shows the error term of the exponential discounting model for the DM .

Figure WD4


Levene's test cannot reject the null. Hence, deviations from the medians are constant ( $\mathrm{p}>0.05$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_exponential_DM
Test Statistic $=1.67, \mathrm{p}=0.16$

The following figure shows the error term of the hyperbolic discounting model for the DM.

Figure WD5


Visual inspection suggests that the error terms in each column have different variances. Levene's test confirms this ( $\mathrm{p}<0.01$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_hyperbolic_DM
Test Statistic $=104.59, \mathrm{p}<2.2 \mathrm{e}-16$

The following figure gives the error term of the unit invariance discounting model for the DM .

Figure WD6


Leneve's test cannot reject the null that the variances are the same ( $p>0.1$ ).

Modified robust Brown-Forsythe Levene-type test based on the absolute deviations from the median
data: error_unit.invariance_DM
Test Statistic $=1.61, \mathrm{p}=0.17$

The following output shows that the discount rate r of exponential discounting of the UM exceeds that of the DM.

TAbLE WD2
signrank $r($ exponential, $U M)=r($ exponential, DM $)$
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 60 | 3344 | 2328 |
| Negative | 36 | 1312 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | ---: |
| adjustment for ties | 0.00 |
| adjustment for zeros | 0.00 |

adjusted variance 74884.00
$H_{0}$ : $r($ exponential, $U M)=r($ exponential, DM)
$z=3.71$
Prob $>\mathrm{z}=0.0002$

The following output shows that the $\alpha$ parameter of hyperbolic discounting of the DM is not significantly different from that of the UM.

## Table WD3

Signrank $\alpha$ (hyperbolic, DM) $=\alpha$ (hyperbolic, UM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 40 | 1998 | 2328 |
| Negative | 56 | 2658 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 74884.00
$\mathrm{H}_{0}: \alpha$ (hyperbolic, DM) $=\alpha$ (hyperbolic, UM)

$$
\begin{aligned}
z & =-1.21 \\
\text { Prob }>z & =0.23
\end{aligned}
$$

The following output shows that the $\beta$ parameter of hyperbolic discounting of the UM is not significantly different from that of the DM.

Table WD4
Signrank $\beta$ (hyperbolic, DM) = $\beta$ (hyperbolic, UM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 41 | 2049 | 2328 |
| Negative | 55 | 2607 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | ---: |
| adjustment for ties | 0.00 |
| adjustment for zeros | 0.00 |

adjusted variance 74884.00
$H_{0}: \beta$ (hyperbolic, DM) $=\beta$ (hyperbolic, UM)

$$
\begin{aligned}
z & =-1.02 \\
\operatorname{Prob}>z & =0.31
\end{aligned}
$$

The following output shows that the d parameter of unit invariance of the DM tends to exceed that of the UM but not significantly so.

## Table WD5

Signrank d (unit invariance, UM) = d (unit invariance, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 45 | 2026 | 2328 |
| Negative | 51 | 2630 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 74884.00
$H_{0}$ : d (unit invariance, UM) = d (unit invariance, DM)

$$
\begin{aligned}
z & =-1.10 \\
\operatorname{Prob}>z & =0.27
\end{aligned}
$$

The following output shows that the r parameter of unit invariance of the DM is not significantly different from that of the UM.

## Table WD6

Signrank r (unit invariance, UM) = r (unit invariance, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 48 | 2424 | 2328 |
| Negative | 48 | 2232 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-1.25$
adjustment for zeros 0.00
adjusted variance 74882.75
$H_{0}$ : $r$ (unit invariance, $U M$ ) $=r$ (unit invariance, $D M$ )

$$
\begin{aligned}
z & =0.35 \\
\operatorname{Prob}>z & =0.73
\end{aligned}
$$

The following output gives descriptive statistics of the Akaike information criterion (AIC).

Table WD7

| Variable | Mean | Min | Median | Max | SD |
| ---: | ---: | ---: | ---: | ---: | ---: |
| Exponential_UM | -3.026 | -6.708 | -3.261 | 0.452 | 1.229 |
| Exponential_DM | -3.559 | -3.990 | -3.676 | -2.147 | 0.475 |
| Hyperbolic_UM | -1.552 | -4.916 | -1.684 | 1.943 | 1.025 |
| Hyperbolic_DM | -1.659 | -2.184 | -1.799 | -0.017 | 0.440 |
| Unit invariance_UM | -1.628 | -5.084 | -1.699 | 1.931 | 0.953 |
| Unit invariance_DM | -1.647 | -2.269 | -1.779 | -0.017 | 0.462 |

The following output shows that AIC for exponential discounting of the UM exceeds that of the DM, implying that the DM has a better fit.

## Table WD8

Signrank AIC (exponential, UM) = AIC (exponential, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 72 | 3577 | 2328 |
| Negative | 24 | 1079 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |


| unadjusted variance | 74884.00 |
| :--- | ---: |
| adjustment for ties | 0.00 |
| adjustment for zeros | 0.00 |

adjusted variance 74884.00
$\mathrm{H}_{0}$ : AIC (exponential, UM) = AIC (exponential, DM)

$$
\begin{aligned}
z & =4.56 \\
\operatorname{Prob}>z & =0.0000
\end{aligned}
$$

The following output shows that AIC for hyperbolic discounting of the UM tends to exceed that of the DM (suggesting that the DM has a better fit), but not significantly so.

Table WD9
Signrank AIC (hyperbolic, UM) = AIC (hyperbolic, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 53 | 2753 | 2328 |
| Negative | 43 | 1903 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 74884.00
$\mathrm{H}_{0}$ : AIC (hyperbolic, UM) = AIC (hyperbolic, DM)
$z=1.55$
Prob $>\mathrm{z}=0.12$

The following output shows that AIC for unit invariance discounting of the DM and the UM do not differ significantly.

Table WD10
Signrank AIC (unit.invariance, UM) = AIC (unit.invariance, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 52 | 2582 | 2328 |
| Negative | 44 | 2074 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 74884.00
$H_{0}$ : AIC (unit.invariance, UM) = AIC (unit.invariance, DM)

$$
\begin{aligned}
z & =0.93 \\
\operatorname{Prob}>z & =0.35
\end{aligned}
$$

The following output shows, for the UM, that the AIC for unit invariance discounting exceeds that of exponential discounting (so that exponential has a better fit).

Table WD11
Signrank AIC (unit.invariance, UM) = AIC (exponential, UM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 95 | 4639 | 2328 |
| Negative | 1 | 17 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-0.13$
adjustment for zeros 0.00
adjusted variance 74883.88
$H_{0}$ : AIC (unit.invariance, UM) = AIC (exponential, UM)
$z=8.44$
Prob $>\mathrm{z}=0.0000$

The following output shows, for the UM, that the AIC for hyperbolic discounting exceeds that of unit invariance (so that unit invariance has a better fit).

TABLE WD12
Signrank AIC (unit.invariance, UM) = AIC (hyperbolic, UM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 17 | 634 | 2328 |
| Negative | 79 | 4019 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-0.13$
adjustment for zeros 0.00
adjusted variance 74883.88
$\mathrm{H}_{0}$ : AIC (unit.invariance, UM) = AIC (hyperbolic, UM)
$z=-6.18$
Prob $>\mathrm{z}=0.0000$

The following output shows, for the UM, that the AIC for hyperbolic discounting exceeds that of exponential discounting (so that exponential discounting has a better fit).

Table WD13
Signrank AIC (hyperbolic, UM) = AIC (exponential, UM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 88 | 4394 | 2328 |
| Negative | 8 | 262 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 68114.75
adjustment for ties 0.00
adjustment for zeros 0.00
adjusted variance 68114.75
$\mathrm{H}_{0}$ : AIC (hyperbolic, UM) = AIC (exponential, UM)
$z=7.37$
Prob $>\mathrm{z}=0.0000$

The following output shows, for the DM, that the AIC for hyperbolic discounting tends to exceed that of unit invariance (so that unit invariance has a better fit), but not significantly so.

## Table WD14

Signrank AIC (unit.invariance, DM) = AIC (hyperbolic, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 31 | 1995 | 2326.5 |
| Negative | 63 | 2658 | 2326.5 |
| Zero | 2 | 3 | 3 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-370.75$
adjustment for zeros $\quad-1.25$
adjusted variance 74512.00
$H_{0}$ : AIC (unit.invariance, DM) = AIC (hyperbolic, UM)

$$
z=-1.21
$$

$$
\operatorname{Prob}>z=0.22
$$

The following output shows, for the DM, that the AIC for hyperbolic discounting exceeds that of exponential discounting (so that exponential discounting has a better fit).

Table WD15
Signrank AIC (exponential, DM) = AIC (hyperbolic, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 0 | 0 | 2328 |
| Negative | 96 | 4656 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-771.00$
adjustment for zeros 0.00
adjusted variance 74113.00
$\mathrm{H}_{0}$ : AIC (exponential, DM) = AIC (hyperbolic, DM)

$$
z=-8.55
$$

$$
\text { Prob }>z=0.0000
$$

The following output shows, for the DM, that the AIC for unit invariance exceeds that of exponential discounting (so that exponential discounting has a better fit).

Table WD16
Signrank AIC (exponential, DM) = AIC (unit.invariance, DM)
Wilcoxon signed-rank test

| Sign | Observations | Sum Ranks | Expected |
| ---: | ---: | ---: | ---: |
| Positive | 0 | 0 | 2328 |
| Negative | 96 | 4656 | 2328 |
| Zero | 0 | 0 | 0 |
| All | 96 | 4656 | 4656 |

unadjusted variance 74884.00
adjustment for ties $\quad-370.75$
adjustment for zeros 0.00
adjusted variance 74513.25
$\mathrm{H}_{0}$ : AIC (exponential, DM) = AIC (unit.invariance, DM)
$z=-8.53$
Prob $>\mathrm{z}=0.0000$

## Online Appendix WE: Theoretical Possibility to Manipulate in the Adaptive Experiment

As explained in the main text (Section V ), the possibility for subjects to manipulate in the experiment is only a theoretical problem because in reality it is impossible for subjects to see through the design without knowing it beforehand. Even readers who have studied the design will need considerable time before being able to specify how to benefit from manipulation. We now consider the theoretical case where someone knows the entire design and has used considerable time to think about manipulations, which is our case as authors of this paper. We assume that all answers are equally likely to be implemented for real, and that the prize to be won is fixed.

A wrong answer in the measurement of $\mathrm{c}_{1 / 2}$ will bring no net gain in the measurements of $\mathrm{c}_{1 / 4}$ and $\mathrm{c}_{3 / 4}$ because the time period gained for one of these two is the time period lost for the other. It will neither bring net gains in the measurements of $\mathrm{c}_{1 / 8}$, and $\mathrm{c}_{1 / 8}$ because, again, the duration gained for one is the duration lost for the other. The only benefit possible is from making $\mathrm{c}_{1 / 4}$ too large (or, similarly, making $\mathrm{c}_{3 / 4}$ too small). Then in some followup questions for $\mathrm{c}_{1 / 8}$ there is a gain, always less than half the loss suffered due to the preceding wrong answer (but in some there is a loss). But there are more, usually around 12 , choice questions in the choice list for $\mathrm{c}_{1 / 8}$. Hence in expectation one gains about $\mathrm{p} \times(8 / 2-1)$ times the error made, where p is the probability of the question being selected for real. Given that $\mathrm{p} \approx 0.01$, this is a moderate gain.


[^0]:    ${ }^{1}$ Although we have the discount factor $\mathrm{d}_{52}^{\mathrm{u}}$ of 52 weeks, we do not show it in Figure 5. Instead, for the end point of the UM, we used the last midpoint of the DM, to allow direct comparisons between the UM and the DM.

[^1]:    *0.05; ** $0.01 ;{ }^{* * *} 0.001$

