Couples and Singles' Savings After Retirement

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September 15, 2015

Abstract

We model the saving problem of retired couples and singles facing uncertain longevity and medical expenses in presence of means-tested social insurance. Households can save to self-insure against uncertain longevity and medical expenses, and to leave bequests. Individuals in a couple can be altruistic towards their spouse and other heirs and split bequests optimally. Single people can care about leaving bequests to children and others. Using AHEAD data, we first estimate the model and we then evaluate the relative importance of the various savings motives and the risk exposure of couples' vs. singles.

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1 Introduction

In the Assets and Health Dynamics of the Oldest Old (AHEAD) dataset, about 50% of individuals aged 70 or older are in a couple, while about 50% are single. Being in a couple during retirement allows its members to pool their longevity and medical expense risks, but also exposes each member to their spouse's risks, including the income loss that often accompanies a spouse's death.

Much of the previous literature, including our own work, only studies singles. In a previous paper (De Nardi, French, and Jones [20]) we show that post-retirement medical expenses and government-provided insurance are important to explaining the saving patterns of U.S. single retirees at all income levels, including high permanent-income individuals who keep large amounts of assets until very late in life. These savings patterns are due to two important features of out-of-pocket medical expenses. First, out-of-pocket medical and nursing-home expenses can be large. Second, average medical expenditures rise very rapidly with age and permanent income. Medical expenses that rise with age provide the elderly with a strong incentive to save, and medical expenses that rise with permanent income encourage the rich to be more frugal. In other work, we showed that heterogeneous life expectancy is important to matching the savings patterns of retired elderly singles (De Nardi, French and Jones [19]).

In this paper, we build on these previous contributions by studying the determinants of retirement saving for both couples and singles, in a framework that incorporates observed heterogeneity in life expectancy and medical expenses, and that explicitly models means-tested social insurance.

Our first goal is to match important facts about savings, medical expenses, and longevity, for both singles and couples. Our second goal is to estimate couples' bequest motives toward the surviving spouse and other heirs, and compare them to the bequest motives of single people. Our third goal is to evaluate the extent to which medical risk affects retired couples, compared to singles, and whether couples can better insure such risks due to intra-household risk-sharing and economies of scale. Our fourth goal is to evaluate the potentially different responses of the saving of couples, compared to that of singles, to changes in publicly-provided health insurance.

Using data from the AHEAD survey, we begin by documenting asset growth at each age for members of different cohorts, for both couples and singles. We also estimate the data generating process for shocks faced by

post-retirement households. These first-step estimates of annuitized income, mortality, health transitions, and medical expenses provide new evidence on how these risks compare for singles and couples. Making accurate comparisons requires that we control for the retirees' permanent income, which in turn requires a measure of permanent income that is invariant to age and family structure. One contribution of this paper is that we construct such a measure. Our approach is to estimate a model expressing annuitized income as a function of an age polynomial, family structure (households are classified as couples, single men or single women), family structure interacted with an age trend, and a household fixed effect. The fixed effect captures the notion of permanent income, because it measures the component of retirement income not affected by age or changes in household structure. Because annuitized retirement income is mostly from Social Security and private pensions, and income from these sources is monotonically rising in lifetime income, this is a good measure of permanent income (PI). Another important benefit of our methodology is that our model can be used to infer the effects of changing age or family structure on annuitized income for the same household. For example, our estimates imply that couples in which the male spouse dies at age 80 suffer a 40% decline in income, while couples in which the female spouse dies at age 80 suffer a 30% decline. These income losses are consistent with the fact that the spousal benefits associated with Social Security and defined benefit pensions typically replace only a fraction of the deceased spouses income.

We estimate health transitions and mortality rates simultaneously by fitting the transitions observed in the HRS to a multinomial logit model. We allow the transition probabilities to depend on age, sex, current health status, marital status, permanent income, and interactions of these variables. Using the estimated transition probabilities, we simulate demographic histories, beginning at age 70, for different gender-PI-health combinations. We find that rich people, women, married people, and healthy people live much longer than their poor, male, single, and sick counterparts. For example, a single 70-year-old male at the 10th permanent income percentile in a nursing home expects to live only 2.9 more years, while a single female at the 90th percentile in good health expects to live 16.5 more years. A 70-year-old married female at the 90th percentile in good health (married to a 73 year old man in the same health state) expects to live 18.6 more years. These large differences in life expectancy can have a significant effect on asset holdings over the retirement period (De Nardi, French and Jones, 2009).

Despite having shorter lifetimes than people who are part of a couple, people who are singles at age 70 are more likely to end up in a nursing home than their counterparts who are members of a couple. For that reason, singles also have higher medical spending, per person, than people who are part of a couple, at any given age. We also find that the strongest predictor for nursing home entry is gender: men are less likely to end up in a nursing home than women. Single men and women face on average a 21% and 36% chance, respectively, of being in a nursing home for an extended stay. The corresponding odds for married individuals are 19% and 36%.

We also find that assets drop sharply during the period before death. By the time the second spouse dies, a large fraction of the wealth of the original couple has vanished, with wealth falls at the time of death of each spouse explaining most of the decline. Depending on the specification, assets decline \$30,000-\$60,000 at the time of an individual's death. A large share of this drop, but not all of it, is explained by the high medical expenses at the time of death. For example, out of pocket medical spending plus death expenses are approximately \$20,000 during the year of death (whereas medical spending is \$6,000 per year for similarly aged people who do not die).

We then estimate the preference parameters of the model with the method of simulated moments. In particular, we compare the simulated asset profiles generated by the model to the empirical asset profiles generated by the data, and find the parameter vector that yields the closest match. In matching the model to the data, we take particular care to control for cohort effects. Moreover, by explicitly modeling demographic transitions, we account for mortality bias.

Our second-step estimates will allow us to evaluate to what extent the risk sharing and economies of scale of a couple help insure against longevity and medical-expense risk and to what extent couples get a better or worse deal from publicly provided health insurance. They will also allow us to estimate bequest motives towards the surviving spouse, in contrast to bequests to children or others. Finally, it will enable us to study in what ways the responses of a couple will differ from the responses of a single person when, for example, public health insurance becomes more limited, or its quality worsens, or some of its means-testing criteria become tighter.

The rest of the paper is organized as follows. In section 2 we describe the key previous papers on which our paper builds on. In section 3 we introduce our model and in section 4 we discuss our estimation procedure. In section 5 we describe some key features of the data and the estimated shock processes

that households face. We discuss our results in section 6 and we and conclude in section 7.

2 Related Literature

Poterba et al. ([43]) show that relatively little dissaving occurs amongst retirees whose family composition does not change, but that assets fall significantly when households lose a spouse. We find similar results. Furthermore, as in French et al.([26]), we document significant drops in assets when the last member of the household passes away.

Previous literature had shown that high income individuals live longer than low income individuals (see Attanasio and Emmerson [4] and Deaton and Paxon [17]). This means that high income households must save a larger share of their lifetime wealth if they are to smooth consumption over their retirement. Differential mortality rates thus provide a potential explanation for why high income households have higher savings rates than low income households. We extend the analysis along this dimension by explicitly modeling the interaction of life expectancy for individuals in couples and the differential life expectancy for couples and singles.

Even in presence of social insurance such as Medicare and Medicaid, households face potentially large out-of-pocket medical and nursing home expenses (see French and Jones [28, 27], Palumbo [41], Feenberg and Skinner [25], and Marshall et al. [36]). The risk of incurring such expenses might generate precautionary savings, over and above those accumulated against the risk of living a very long life ([35]).

Hubbard, Skinner and Zeldes [32] argue that means-tested social insurance programs such as Supplemental Security Income and Medicaid provide strong incentives for low income individuals not to save. De Nardi et al. [21] finds that these effects extend to singles in higher permanent income quintiles as well. In this paper, to allow for these important effects, we model means-tested social insurance explicitly for both singles and couples.

Bequest motives could be another reason why households, and especially those with high permanent income, retain high levels of assets at very old ages (Dynan, Skinner and Zeldes [23] and Americks et al. [2]). De Nardi [15] and Castañeda et al. [13] argue that bequest motives are necessary to explain why the observed distribution of wealth is more skewed and concentrated than the distribution of income (Quadrini et al. [18]). De Nardi et al [21]

shows that bequest motives help fit both assets and Medicaid recipiency profiles for singles. We allow for a richer structure of bequest motives, in that couples might want to leave resources to the surviving spouse, children and other heirs, while singles might want to leave bequests to children and other heirs.

Previous quantitative papers on savings have used simpler models that omit one or more of these features. Hurd [33] estimates a structural model of bequest behavior in which the time of death is the only source of uncertainty. Palumbo [41] focuses on the effect of medical expenses and uncertain lifetimes, but omits bequests. Dynan, Skinner and Zeldes [23, 24] consider the interaction of mortality risk, medical expense risk and bequests, but use a stylized two-period model. Moreover, none of these papers model household survival dynamics, assuming instead that households (while "alive") always have the same composition. In contrast, we explicitly model household survival dynamics: when the first household member dies, assets are optimally split among the surviving spouse and other heirs. Although Hurd [34] extends his earlier model to include household survival dynamics, he omits medical expense risk, and, in contrast to his earlier work, he does not estimate his model.

Our work also complements the one on retirement behaviour by couples by Blau and Gilleskie [8], Casanova [12], and Gallipoli and Turner [30].

Including couples and simultaneously considering bequest motives, social insurance, uncertain medical expenses, and uncertain life expectancy is important for at least two reasons. First, Dynan, Skinner and Zeldes [24] argue that explaining why the rich have high savings rates requires a model with precautionary motives, bequest motives and social insurance. Second, simultaneously considering multiple savings motives allows us to identify their relative strengths. This is essential for policy analysis. For example, the effects of estate taxes depend critically on whether rich elderly households save mainly for precautionary reasons, or mainly to leave bequests (see for example Gale and Perozek [29]).

3 The Model

Consider a retired household with family structure f_t (either a single person or a couple), seeking to maximize its expected lifetime utility at household head age t, $t = t_r, t_r + 1..., T + 1$, where t_r is the retirement age, while T is

the maximum potential lifespan.

We use w to denote women and h to denote men. Each person's health status, hs^g , $g \in \{h, w\}$, can vary over time. The person is either in a nursing home $(hs^g = 1)$, in bad health $(hs^g = 2)$, or in good health $(hs^g = 3)$.

For tractability, we assume a fixed age gap between the husband and the wife in a couple, so that one age is sufficient to characterize the household. To be consistent with the data frequency, and to reduce computation time, our time period is two years long.

3.1 Preferences

Households maximize their utility by choosing savings, bequests and current and future consumption. The annual discount factor is given by β . Each period, the household's utility depends on its total consumption, c, and the health status of each member. The within-period utility function for a single is given by

$$u(c, hs) = (1 + \delta(hs)) \frac{c^{1-\nu}}{1-\nu},$$
 (1)

with $\nu \geq 0$. When $\delta(.) = 0$, health status does not affect utility.

We assume that the preferences of couples can be represented by the following utility function:¹

$$u^{c}(c, hs^{h}, hs^{w}) = [1 + \delta(hs^{h}) + 1 + \delta(hs^{w})] \frac{(c/\eta)^{1-\nu}}{1 - \nu},$$
(2)

where $1 < \eta \le 2$ determines the extent to which couples enjoy economies of scale in the transformation of consumption goods to consumption services.

When a household member dies, the estate can be left to the surviving spouse (if there is one) or to other heirs, including the household's children. Estates are subject to estate taxes, but the exemption level during the time period in our sample is above the actual assets of the vast majority of the households in our sample. For this reason, we abstract from explicitly modeling estate taxation.

We indicate with b the part of the estate, that does *not* go to the surviving spouse, and assume that the deceased member of the household derives utility

¹Mazzocco [37] shows that under full commitment, the behavior of a couple can be characterized by a unique utility function if the husband and wife share identical discount factors, identical beliefs and Harmonic Absolute Risk Aversion utility functions with identical curvature parameters.

 $\theta_j(b)$ from leaving that part of the estate to heirs other than the spouse. The subscript j indicates whether there is a surviving spouse or not, and whether one or two people have just died. In particular, $\theta_0(b)$ gives the utility from bequests for a single person with no surviving spouse, $\theta_1(b)$ gives the utility from bequests when there is a surviving spouse, and that $\theta_2(b)$ gives the utility from bequests when both spouses die at the same time. More specifically, the bequest function takes the form

$$\theta_j(b) = \phi_j \frac{(b+k_j)^{(1-\nu)}}{1-\nu},$$
(3)

where k_j determines the curvature of the bequest function, and ϕ_j determines its intensity. Our formulation can support several interpretations of the "bequest motive": dynastic or "warm glow" altruism (as in Becker and Tomes [6] or Andreoni [3]); strategic motives (as in Bernheim, Schleifer and Summers [7] or Brown [9]); or some form of utility from wealth itself, as in (Carroll [11] and Hurd [33]).

3.2 Technology and Sources of Uncertainty

We assume that non-asset income at time t, y_t , is a deterministic function of the household's permanent income, I, age, family structure, and gender if single.

$$y_t(\cdot) = y(I, t, f_t, g_t). \tag{4}$$

There are several sources of uncertainty:

1) Health status uncertainty. The transition probabilities for the health status of a person depend on one's current health status, permanent income, age, and gender and marital status. Hence the elements of the health status transition matrix for a person of gender g are given by

$$\pi_t^g(\cdot) = \Pr(hs_{t+1}^g | I, t, g, hs_t^g, f_t).$$
 (5)

- 2) Survival uncertainty. Let $s_t^g(\cdot) = s(I, t, g, hs_t^g, f_t)$ denote the probability that an individual of gender g is alive at age t + 1, conditional on being alive at age t, having time-t health status hs^g , enjoying household permanent income I, and having family structure f_t .
- 3) Medical expense uncertainty at the household level. We define m_t as the sum of all out-of-pocket medical expenses, including insurance premia, and medical expenses covered by the consumption floor. We assume that

medical expenses depend upon the health status of each family member, household permanent income, family structure, gender if single, age, and an idiosyncratic component, ψ_t :

$$\ln m_t = m(hs_t^h, hs_t^w, I, q, t, f_t, f_{t-1}) + \sigma(hs_t^h, hs_t^w, I, q, t, f_t, f_{t-1}) \times \psi_t.$$
 (6)

For medical spending, we also include last period's household status, to capture the jump in medical spending that occurs in the period a family member dies.

Following Feenberg and Skinner [25] and French and Jones [27], we assume that ψ_t can be decomposed as

$$\psi_t = \zeta_t + \xi_t, \quad \xi_t \sim N(0, \sigma_{\varepsilon}^2), \tag{7}$$

$$\zeta_t = \rho_m \zeta_{t-1} + \epsilon_t, \quad \epsilon_t \sim N(0, \sigma_{\epsilon}^2),$$
 (8)

where ξ_t and ϵ_t are serially and mutually independent. In practice, we discretize ξ and ζ , using quadrature methods described in Tauchen and Hussey [46].

The timing is the following: at the beginning of the period the health shock and the medical cost shocks are realized, income is received, and if the household qualifies, means-tested transfers are also received. Then the household consumes and saves. Finally the survival shock hits. Household members who die leave assets to their heirs. Bequests are included in the heirs' assets at the beginning of next period.

Let us denote assets at the beginning of the period with a_t . Assets have to satisfy a borrowing constraint $a_t \geq 0$. Let us indicate the constant and risk-free, rate of return with r, and total post-tax income with $y(r a_t + y_t(\cdot), \tau)$, with the vector τ describing the tax structure.

3.3 Recursive Formulation

To save on state variables we follow Deaton [16] and redefine the problem in terms of cash-on-hand:

$$x_t = a_t + y(r a_t + y_t(\cdot), \tau) - m_t + tr_t(\cdot),$$
 (9)

The law of motion for cash on hand next period is given by

$$x_{t+1} = x_t - c_t - b_t + y(r(x_t - c_t) + y_{t+1}(\cdot), \tau) - m_{t+1} + tr_t(\cdot)$$
(10)

where $b_t \geq 0$ is positive only when one spouse from a couple dies during the current period and leaves bequests to other heirs (e.g., children). We do not include received bequests as a source of income, because very few households aged 65 or older receive them. When all household members die their assets are bequeathed to the remaining heirs.

Following Hubbard et al. [31, 32], we assume that the government provides means-tested transfers, $tr_t(\cdot)$, that bridge the gap between a minimum consumption floor and the household's resources, net of an asset disregard amount. Define the resources available next period *before* government transfers with

$$\widetilde{x}_{t+1} = x_t - c_t - b_t + y(r(x_t - c_t) + y_{t+1}(\cdot), \tau) - m_{t+1},$$
 (11)

Consistently with the main Medicaid and SSI rules, we can express government transfers next period as

$$tr_{t+1}(\widetilde{x}_{t+1}, hs_{t+1}) = \max\{0, c_{min}(f_{t+1}) - \max\{0, \widetilde{x}_{t+1} - a_d(f_{t+1})\}\}, \quad (12)$$

We allow both the guaranteed consumption level c_{min} and the asset disregard a_d to vary with family structure. We impose that if transfers are positive, $c_t = c_{min}(f_t)$.

The law of motion for cash on hand next period can thus be rewritten as

$$x_{t+1} = \widetilde{x}_{t+1} + tr_{t+1}(\widetilde{x}_{t+1}, hs_{t+1}). \tag{13}$$

To ensure that cash on hand is always non-negative, we require

$$c_t \le x_t, \quad \forall t.$$
 (14)

Using the definition of cash-on-hand, the value function for a single individual of gender g can be written as

$$V_t^g(x_t, hs_t, I, \zeta_t) = \max_{c_t, x_{t+1}} \left\{ u(c_t, hs_t) + \beta s(I, t, g, hs_t^g, f_t) E_t \Big(V_{t+1}^g(x_{t+1}, hs_{t+1}, I, \zeta_{t+1}) \Big) + \beta (1 - s(I, t, g, hs_t^g, f_t) \theta_0(x_t - c_t) \right\},$$
(15)

subject to equations (4)-(8) and (11)-(14).

The value function for couples can be written as

$$V_{t}^{c}(x_{t}, hs_{t}^{h}, hs_{t}^{w}, I, \zeta_{t}) = \max_{c_{t}, x_{t+1}, b^{w}, b^{h}} \left\{ u^{c}(c_{t}, hs_{t}^{h}, hs_{t}^{w}) + \beta s(I, t, w, hs_{t}^{g}, 1) s(I, t, h, hs_{t}^{g}, 1) E_{t} \left(V_{t+1}^{c}(x_{t+1}, hs_{t+1}^{h}, hs_{t+1}^{w}, I, \zeta_{t+1}) \right) + \beta s(I, t, w, hs_{t}^{g}, 1) (1 - s(I, t, h, hs_{t}^{g}, 1)) \left[E_{t} \left(V_{t+1}^{w}(x_{t+1}^{w}, hs_{t+1}^{w}, I, \zeta_{t+1}) \right) + \theta_{1}(b_{t}^{h}) \right] + \beta (1 - s(I, t, w, hs_{t}^{g}, 1)) s(I, t, h, hs_{t}^{g}, 1) \left[E_{t} \left(V_{t+1}^{h}(x_{t+1}^{h}, hs_{t+1}^{h}, I, \zeta_{t+1}) \right) + \theta_{1}(b_{t}^{w}) \right] + \beta (1 - s(I, t, w, hs_{t}^{g}, 1)) (1 - s(I, t, h, hs_{t}^{g}, 1) \theta_{2}(x_{t} - c_{t}) \right\},$$

$$(16)$$

where the value function is subject to equations subject to equations (4)-(8) and (11)-(17), with $f_t = 1$ since we are referring to couples, and bequests are constrained by

$$b_t \le x_t - c_t. \tag{17}$$

4 Estimation Procedure

We adopt a two-step strategy to estimate the model. In the first step, we estimate or calibrate those parameters that, given our assumptions, can be cleanly identified outside our model. In particular, we estimate health transitions, out-of-pocket medical expenses, and mortality rates from raw demographic data. We calibrate the household economies of scale parameter and the minimum consumption floor for singles and couples based on previous work.

In the second step, we estimate the rest of the model's parameters (discount factor, risk aversion, health preference shifter, and bequest parameters)

$$\Delta = (\beta, \nu, \delta, \omega, \phi_0, \phi_1, \phi_2, k_0, k_1, k_2)$$

with the method of simulated moments (MSM), taking as given the parameters that were estimated in the first step. In particular, we find the parameter values that allow simulated life-cycle decision profiles to "best match" (as measured by a GMM criterion function) the profiles from the data.

Because our underlying motivations are to explain why elderly individuals retain so many assets and to explain why individuals with high income save

at a higher rate, we match median assets by cohort, age, and permanent income. Because we wish to study differences in savings patterns of couples and singles, we match profiles for the singles and couples separately. Finally, to help identify bequest motives towards' one spouse, we also match the fraction of assets (net worth) left to the surviving spouse in a couple affected by death.

In particular, the moment conditions that comprise our estimator are given by

- 1. Median asset holdings by PI-cohort-year for the singles who are still alive when observed.
- 2. Median asset holdings by PI-cohort-year for those who were initially couples with both members currently alive.
 - When there is a death in a couple, the surviving spouse is included in the singles' profile of the appropriate age, cohort, and permanent income cell; in keeping with our assumption that all singles differ only in their state variables.
- 3. For estates of positive value, the median fraction of the estate left to the surviving spouse by PI and age. We do not condition this moment by cohort for two reasons. First, the sample size is too small, and second there does not seem to be a discernible cohort effect in this moment.

The cells are computed as follows.² Household i has family structure f_t ; which indexes households that are initially couples and those that either are initially singles (both men and women), or become singles through death of their spouse. We sort type-f households in cohort c by their permanent income levels, separating them into Q = 5 quintiles. Suppose that household i's permanent income level falls in the qth permanent income interval of households in its cohort and family structure.

Let $a_{cfqt}(\Delta, \chi)$ be the model-predicted median observed asset level in calendar year t for a household that was in the qth permanent income interval of cohort c. Assuming that observed assets have a continuous density, at the "true" parameter vector (Δ_0, χ_0) exactly half of the households in group

²As was done when constructing the figures from the HRS data, we drop cells with less than 10 observations from the moment conditions. Simulated agents are endowed with asset levels drawn from the 1996 data distribution, and thus we only match asset data 1998-2010.

cfqt will have asset levels of $a_{cfqt}(\Delta_0, \chi_0)$ or less. This leads to the following moment condition:

$$E(1\{\tilde{a}_{it} \le a_{cfat}(\Delta_0, \chi_0)\} - 1/2 | c, f, q, t, \text{household alive at } t) = 0, \quad (18)$$

for all c, f, q and t. In other words, for each permanent income-family structure-cohort grouping, the model and the data have the same median asset levels.

The mechanics of our MSM approach are as follows. We compute life-cycle histories for a large number of artificial households. Each of these households is endowed with a value of the state vector $(t, f_t, x_t, I, hs_t^h, hs_t^w, \zeta_t)$ drawn from the data distribution for 1996, and each is assigned the entire health and mortality history realized by the household in the AHEAD data with the same initial conditions. This way we generate attrition in our simulations that mimics precisely the attrition relationships in the data (including the relationship between initial wealth and mortality).

We discretize the asset grid and, using value function iteration, we solve the model numerically. This yields a set of decision rules, which, in combination with the simulated endowments and shocks, allows us to simulate each individual's assets, medical expenditures, health, and mortality. We compute assets from the artificial histories in the same way as we compute them from the real data. We use these profiles to construct moment conditions, and evaluate the match using our GMM criterion. We search over the parameter space for the values that minimize the criterion. Appendix E contains a detailed description of our moment conditions, the weighting matrix in our GMM criterion function, and the asymptotic distribution of our parameter estimates.

When estimating the life-cycle profiles, and subsequently fitting the model to those profiles, we face two well-known problems. First, in a cross-section, older households were born in an earlier year than younger households and thus have different lifetime incomes. Because lifetime incomes of households in older cohorts will likely be lower than the lifetime incomes of younger cohorts, the asset levels of households in older cohorts will likely be lower also. Therefore, comparing older households born in earlier years to younger households in later years leads to understate asset growth. Second, households with lower income and wealth tend to die at younger ages than richer households. Therefore, the average survivor in a cohort has higher lifetime income than the average deceased member of the cohort. As a result, "mortality bias" leads the econometrician to overstate the average lifetime income

of members of a cohort. This bias is more severe at older ages, when a greater share of the cohort members are dead. Therefore, "mortality bias" leads to overstate asset growth.

We use panel data to overcome these first two problems. Because we are tracking the same households over time, we are obviously tracking members of the same cohort over time. Similarly, we do separate sets of simulations for each cohort, so that the (initial) wealth and income endowments behind the simulated profiles are consistent with the endowments behind the empirical profiles. As for the second problem, we explicitly simulate demographic transitions so that the simulated profiles incorporate mortality effects in the same way as the data, both for couples and singles.

5 Data

We use data from the Asset and Health Dynamics Among the Oldest Old (AHEAD) dataset. The AHEAD is a sample of non-institutionalized individuals, aged 70 or older in 1993. These individuals were interviewed in late 1993/early 1994, and again in 1996, 1998, 2000, 2002, 2004, 2006, 2008, and 2010. We do not use 1994 assets, nor medical expenses, due to underreporting (Rohwedder et al. [45]).

We only consider retired households to abstract from the retirement decisions and focus on the determinants of savings and consumption. Because we only allow for household composition changes through death, we drop households where an individual enters a household or an individual leaves the household for reasons other than death. Fortunately, attrition for reasons other than death is a minor concern in our data.

To keep the dynamic programming problem manageable, we assume a fixed difference in age between spouses, and we take the average age difference from our data. In our sample, husbands are on average 3 years older than their wives. To keep the data consistent with this assumption, we drop all households where the wife is more than 4 years older or 10 years younger than her husband.

We begin with 6047 households. After dropping 401 households who get married, divorced, were same sex couples, or who report making other transitions not consistent with the model, 753 households who report earning at least \$3,000 in any period, 171 households with a large difference in the age of husband and wife, and 87 households with no information on the spouse

in a household, we are left with 4,634 households, of whom 1,388 are couples and 3,246 are singles. This represents 24,274 household-year observations where at least one household member was alive.

We break the data into 5 cohorts. The first cohort consists of individuals that were ages 72-76 in 1996; the second cohort contains ages 77-81; the third ages 82-86; the fourth ages 87-91; and the final cohort, for sample size reasons, contains ages 92-102. Even with the longer age interval, the final cohort contains relatively few observations. In the interest of clarity, we exclude this cohort from our graphs, but we use all cells with at least 10 observations when estimating the model.

We use data for 8 different years; 1996, 1998, 2000, 2002, 2004, 2006, 2008, and 2010. We calculate summary statistics (e.g., medians), cohort-by-cohort, for surviving individuals in each calendar year—we use an unbalanced panel. We then construct life-cycle profiles by ordering the summary statistics by cohort and age at each year of observation. Moving from the left-hand-side to the right-hand-side of our graphs, we thus show data for four cohorts, with each cohort's data starting out at the cohort's average age in 1996.

Since we want to understand the role of income, we further stratify the data by post-retirement permanent income (PI). Hence, for each cohort our graphs usually display several horizontal lines showing, for example, median assets in each PI group in each calendar year. These lines also identify the moment conditions we use when estimating the model.

Our PI measure can be thought of as the level of income if there were two people in the household at age 70. We measure post-retirement PI using non-asset non-social insurance annuitized income and the methods described in appendix A . The method maps the relationship between current income and PI, adjusted for age and household structure. The income measure includes the value of Social Security benefits, defined benefit pension benefits, veterans benefits and annuities. Since we model means-tested social insurance from SSI and Medicaid explicitly through our consumption floor, we do not include SSI transfers. Because there is a roughly monotonic relationship between lifetime earnings and the income variables that we use, our measure of post-retirement PI is also a good measure of lifetime permanent income.

The AHEAD has information on the value of housing and real estate, autos, liquid assets (which include money market accounts, savings accounts, T-bills, etc.), IRAs, Keoghs, stocks, the value of a farm or business, mutual funds, bonds, "other" assets and investment trusts less mortgages and other debts.

We do not include pension and Social Security wealth for four reasons. First, we wish to to maintain comparability with other studies (Hurd [33], Attanasio and Hoynes [5] for example). Second, because it is illegal to borrow against Social security wealth pension and difficult to borrow against most forms of pension wealth, Social Security and pension wealth are much more illiquid than other assets. Third, their tax treatment is different from other assets. Finally, differences in Social Security and pension are captured in our model by differences in the permanent income measure we use to predict annual income.

One important problem with our asset data is that the wealthy tend to underreport their wealth in virtually all household surveys (Davies and Shorrocks [14]). This will lead us to understate asset levels at all ages. However, Juster et al. (1999) show that the wealth distribution of the AHEAD matches up well with aggregate values for all but the richest 1 % of households. Given that we match medians (conditional on permanent income), underreporting at the very top of the wealth distribution should not seriously affect our results.

6 Results

6.1 Health and Mortality

We estimate health transitions and mortality rates simultaneously by fitting the transitions observed in the HRS to a multinomial logit model. We allow the transition probabilities to depend on age, sex, current health status, marital status, permanent income, as well as polynomials and interactions of these variables.

Using the estimated transition probabilities, we simulate demographic histories, beginning at age 70, for different gender-PI-health combinations. Tables 1 and 2 show life expectancies for singles and couples at age 70, respectively. All tables use the appropriate distribution of people over state variables to compute the number which is object of interest. We find that rich people, women, married people, and healthy people live much longer than their poor, male, single, and sick counterparts.

Table 1 shows that a single male at the 10th permanent income percentile in a nursing home expects to live only 2.9 more years, while a single female at the 90th percentile in good health expects to live 16.5 more years. The

	Males Females						
Income	Nursing	Bad	Good	Nursing	Bad	Good	
Percentile	Home	Health	Health	Home	Health	Health	All
10	2.86	6.72	8.45	3.79	11.13	13.21	11.46
30	2.86	7.30	9.36	3.78	11.78	14.03	12.20
50	2.86	7.99	10.34	3.78	12.48	14.89	13.01
70	2.88	8.83	11.37	3.78	13.33	15.76	13.85
90	2.90	9.76	12.44	3.85	14.14	16.54	14.73
By gender:							
Men							9.97
Women							13.72
By health status:							
Bad Heal							11.11
Good Hea	alth						14.20

Table 1: Life expectancy in years for singles, conditional on reaching age 70.

far right column shows average life expectancy conditional on permanent income, averaging over both genders all health states. It shows that singles at the 10th percentile of the permanent income distribution live on average 11.5 years, whereas singles at the 90th percentile live on average 14.7 years.

Table 2 shows that a 70 year old male married to a 67 year old woman with the same health as himself, at the 10th permanent income percentile in a nursing home expects to live only 2.7 more years, while a 70 year old married female at the 90th percentile in good health (married to a 73 year old man in the same health state as herself) expects to live 18.6 more years. Averaging over both genders and all health states, married 70 year old people at the 10th percentile of the income distribution live on average 10.5 years, while those at the 90th percentile live 15.7 years. Singles at the 10th percentile live longer than members of couples at the same percentile. The reason

		Males			Females		
Income	Nursing	Bad	Good	Nursing	Bad	Good	
Percentile	Home	Health	Health	Home	Health	Health	All
10	2.65	6.88	8.46	3.59	11.47	13.49	10.48
30	2.69	7.77	9.74	3.67	12.46	14.68	11.59
50	2.76	8.87	11.12	3.76	13.55	15.98	12.86
70	2.85	10.19	12.62	3.90	14.89	17.29	14.23
90	2.98	11.69	14.22	4.06	16.26	18.55	15.67
By gender:							
Men							12.24
Women							16.93
By health status:							
Bad Health							11.88
Good Hea	alth						15.60
Oldest Survivor							18.78
Prob Oldest Survivor is Woman						67.5%	

Table 2: Life expectancy in years for couples, conditional on reaching age 70.

for this is that singles at the 10th percentile of the income distribution are are overwhelmingly women who live longer, whereas 50% of the members of couples are male. Conditional on gender, those in either good or bad health at the 10th percentile live longer if in a couple. Conditional only on gender, members of couples live almost 3 years longer than singles: single 70 year old women live on average 13.8 years versus 16.9 for married women But a comparison of tables 1 and 2 reveals that, conditional on PI and health, the differences in longevity are much smaller. Married people live longer than singles, but much of the difference is explained by the fact that married people tend to have higher PI.

	Mε	Males		Females		
Income	Bad	Good	Bad	Good		
Percentile	Health	Health	Health	Health	All	
10	20.8	21.5	34.0	35.6	32.2	
30	20.5	21.6	34.1	36.1	32.7	
50	20.3	21.7	34.1	36.8	32.8	
70	20.1	21.6	34.1	36.9	33.1	
90	19.5	21.5	33.9	36.9	33.0	
By gender:						
Men					21.0	
Women					35.7	
By health status:						
Bad Heal					31.2	
Good Hea	alth				33.2	

Table 3: Probability of ever entering a nursing home, singles alive at age 70.

The bottom part of table 2 shows the number of years of remaining life of the oldest survivor in a household when the man is 70 and the woman is 67. On overage the last survivor lives and additional 18.8 years. The woman is the oldest survivor 68% of the time.

The strongest predictor for nursing home entry is gender: men are less likely to end up in a nursing home than women. Although married people tend to live longer than singles, they are slightly less likely to end up in a nursing home.

Table 3 shows that single men and women face on average a 21% and 36% chance of being in a nursing home for an extended stay, respectively. Table 4 shows that married men and women face on average a 19% and 36% chance of being in a nursing home for an extended stay. Married people are much less likely to transition into a nursing home at any age , but married

	Mε	Males		Females		
Income	Bad	Good	Bad	Good		
Percentile	Health	Health	Health	Health	All	
10	16.1	16.6	31.8	33.0	24.6	
30	16.6	17.5	32.3	34.3	25.7	
50	17.3	18.6	33.0	35.7	26.5	
70	17.8	19.4	34.0	36.4	27.5	
90	18.5	20.6	34.9	37.3	28.3	
By gender:						
Men					19.0	
Women					36.3	
By health status:						
Bad Health				25.6		
Good Hea	alth				28.4	

Table 4: Probability of ever entering a nursing home, married alive at age 70.

people often become single as their partner dies and a they age. Furthermore, married people tend to live longer than singles, so they have more years of life to potentially enter a nursing home. Permanent income has only a small effect on ever being in a nursing home. Those with a high permanent income are less likely to be in a nursing home at each age, but they tend to live longer.

6.2 Income

We model income as a function of a third order polynomial in age, dummies for family structure, family structure interacted with an age trend, and a fifth order polynomial in permanent income. The estimates use a fixed effects estimation procedures, where the fixed effect is a transformation of

initial permanent income. Hence the regression results can be interpreted as the effect of changing age or family structure for the same household: see appendix A for details of the procedure.

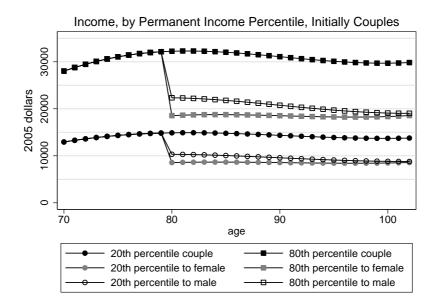


Figure 1: Income, conditional on permanent income and family structure. Figure assumes all households begin as couples, then potentially change to a single male or single female at age 80.

Figure 1 presents predicted income profiles for those at the 20th and 80th percentiles of the permanent income distribution. For each permanent income level, we display three scenarios, all commencing from the income of a couple. Under the first scenario, the household remains a couple until age 100. Under the second one, the man dies at age 80. Under the third one, the woman dies at age 80.

Figure 1 shows that average annual income ranges from about \$14,000 per year for couples in the 20th percentile of the PI distribution to over \$30,000 for couples in the 80th percentile of the PI distribution. As a point of comparison, median wealth holdings for the two groups are \$70,000 and \$330,000 at age 74, respectively. Our estimates suggest that couples in which the male spouse dies at age 80 suffer a 40% decline in income, while couples in which the female spouse dies at 80 suffer a 30% decline in income.

These income losses at the death of a spouse reflect the fact that although both Social Security and defined benefit pensions have spousal benefits, these benefits replace only a fraction of the deceased spouse's income. More specifically, people can receive benefits either based on their own history of Social security contributions (in which case they are a "retired worker"), or based on their spouse's or former spouse's history (in which case they receive the "spouse's" or "widows" benefit).

A married person who never worked can receive 50% of their spouse's benefit if their spouse is alive and is a "retired worker". The same person can receive up to 100% of their spouse's benefit if their "retired worker" spouse has died. Thus the household benefit can receive 100%+50%=150% of the former worker spouse's benefit when alive and 100% of the former worker spouse's benefit when either spouse has died. Thus, after the death of a household member the household would maintain (100%/150%)=67% of the original Social Security benefit and would experience a 33% drop in benefits.

In contrast, a person who earned the same amount as their spouse will not receive a spousal or widow's benefit. In this case, both spouses in the couple will receive 100% of their own "retired worker" benefit, which is based off of their own earnings history. After the death of a spouse, the household benefit will be (100%/(100%+100%)=50% of its level when both were alive.

To perform our calculations, we make several assumptions, including that both spouses begin receiving benefits at the normal retirement age. In practice, there are many modifications to this rule, including those to account for the age at which the beneficiary and spouse begin drawing benefits.³ Our regression estimates capture the average drop in income at the time of death of a spouse, averaging over those who retire at different ages and have different claiming histories.

6.3 Medical Spending

One drawback of the AHEAD data is that it contains information only on out of pocket medical spending and not on the portion of medical spending covered by Medicaid. To be consistent with the model, in which the consumption floor is explicitly modeled, we need to include both Medicaid

³See https://socialsecurity.gov/planners/retire/yourspouse.html for more details of calculation of spousal benefits.

payments and out of pocket medical spending in our measure of out-of-pocket medical spending.

Fortunately, the Medicare Current Beneficiary Survey (MCBS) has extremely high quality information on Medicaid payments and out of pocket medical spending. It uses a mixture of both administrative and survey data. One drawback of the MCBS, however, is that although it has information on marital status and household income, but does not have information on the medical spending or health of the spouse. To exploit the best of both datasets, we use the procedures described in Appendix C to obtain our measured out-of-pocket medical expenditures, including those paid for by Medicaid.

We model the logarithm of medical spending as a fourth order polynomial in age, dummies for family structure, the health of each family member (including whether that family member just died), family structure interacted with an age trend, and a fifth order polynomial in permanent income. As with the income estimate, we use fixed effects estimation procedures, so the regression results can be interpreted as the effect of changing age or family structure for the same household.

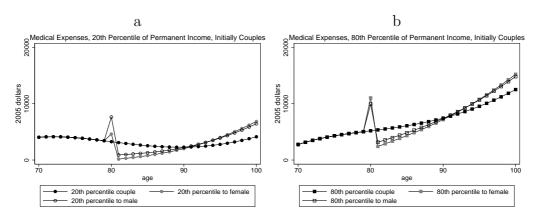


Figure 2: Mean out-of-pocket medical expenditures by age, conditional on permanent income and family structure. Figure assumes all households begin as couples, then potentially change to a single male or single female at age 80.

Figure 2 displays our predicted medical expense profiles for those at the 20th (left panel) and 80th (right panel) percentiles of the permanent income distribution for those in bad health. For each permanent income level, we

present three scenarios, all of which start out with a couple. Under the first scenario, the household remains a couple until age 100. Under the second one, the man dies at age 80. Under the third one, the woman dies at age 80. The jump in medical spending shown at age 80 represents the elevated medical spending during the year of death of a family member and amounts to almost \$5,000 on average. Both average medical spending and the jump at time of death are larger for those with higher permanent income.

The figure shows that, before age 80, average annual medical spending hoover around \$4,000 per year for the couples in both income groups. For those at the 20th percentile of the PI distribution, medical expenses change little with age. However, for couples in the 80th percentile, medical expenses rise to well over \$10,000 per year by age 95.

In order to estimate the variability of medical spending, we take medical expense residuals (the difference between actual and predicted medical spending) and we regress the squared residuals on the same covariates we used for the regression for the logarithm of medical spending.

6.4 Life Cycle Asset Profiles

The following figures display median assets, conditional on birth cohort and income quintile, for couples and singles that are classified by permanent income quintile based on the permanent incomes of that same subpopulation (couples of singles). We choose to classify profiles in this fashion because couples are richer than singles and classifying a subpopulation according to the permanent income of the entire population would create cells that in some cases contain a large fraction of the population, while in other they generate a much smaller cell. The graphs based on the classification of permanent income by the whole population are in appendix B and display similar patterns.

Figure 3 displays the asset profiles for the unbalanced panel of singles, classified according to the PI of the singles. Median assets are increasing in permanent income, with the 74-year-olds in the highest PI income of the singles holding about \$200,000 in median assets, while those at the lowest PI quintiles holding essentially no assets. Over time, those with the highest PI tend to hold onto significant wealth well into their nineties, those with the lower PIs never save much, while those in the middle PIs display quite some asset decumulation as they age.

Figure 4 reports median assets for the population of those who are ini-

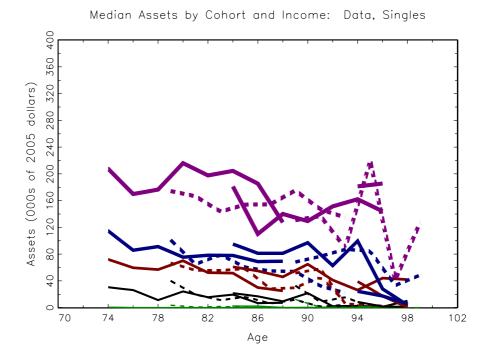


Figure 3: Median assets for singles, PI percentiles computed using singles only. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

tially in a couple. The first thing to notice is that couples are richer than singles. The younger couples in the highest PI quintile for couples hold over \$340,000, compared to \$200,000 for singles, and even the couples in the lowest PI quintile bin hold over \$60,000 in the earlier years of their retirement, compared to zero for the singles. As for the singles, the couples in the highest PI quintile hold on to large amount of assets well into their nineties, while those in the lowest income PIs display more asset decumulation. Some of these couples lose one spouse during the period in which we observe them, in which case we report the assets of the surviving spouse, hence some of the decumulation that we observe in this graph is due to the death of one spouse and consequent disappearance of some of the couple's assets.

Figure 5 Displays median assets for those who initially are in couples

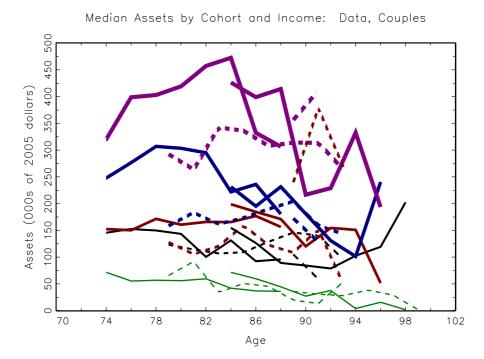


Figure 4: Median assets for initially couples, PI percentiles computed using couples only. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

and remain in a couple during our sample period. That is, they do not experience the death of a partner. Interestingly, these graphs display flat to increasing asset profiles, going from low to high permanent income. This is consistent with the observation that much of the asset decumulation for a couple happens at death of one spouse.

To formalize and quantify this observation, we perform regression analysis. We regress assets on a household fixed effect, dummies for household status (couple, single man, single woman, everyone dead), a polynomial in age, and interactions between these and permanent income. Including the household specific fixed effect means that we can track wealth of the same households, when one member of the household dies. The fixed effect includes all time invariant factors, including permanent income, so we cannot

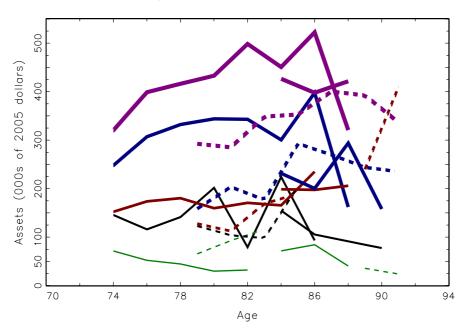


Figure 5: Median assets for intact couples, PI percentiles computed using couples only. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

include permanent income directly. To include permanent income directly, we then regress the estimated fixed effect on the permanent income of that household.

Figure 6 reports the predicted assets of a couple starting out, respectively, in the top PI income quintile, and in the bottom one, and display the assets under three scenarios. Under the first one, the couple remains intact until age 90. Under the second one, the male dies at age 80, while under the third one, the female dies at age 80. For both PI levels, assets stay roughly constant if both partners are alive. In contrast, assets display a significant drop at death of one of the spouses for the higher PI couples. The results show that on average, wealth declines approximately \$60,000 at the time of death of a household member. Interestingly, assets experience a large drop

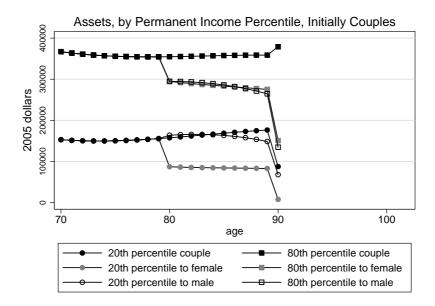


Figure 6: Assets, conditional on permanent income and family structure. Figure assumes all households begin as couples, then potentially change to a single male or single female at age 80, then everyone dies at age 90.

when the male dies also for the lowest PI quintile, but not much of a drop when the female dies first.

A simpler exercise of merely tabulating the wealth decline when one member of the household dies suggests smaller estimates of the wealth decline at the time of death of a spouse. This procedure suggests a decline of wealth of \$30,000 at the death of a spouse. A large share of this drop, but not all of it, is explained by the high medical expenses at the time of death. For example, out of pocket medical spending plus death expenses are approximately \$20,000 during the year of death (whereas medical spending is \$6,000 per year for similarly aged people who do not die).

To measure the decline in wealth at the time of death of the final member of the family, we exploit the exit surveys, which include information on the heirs' reports of the value of the estate. In addition, we also use data from post-exit interviews, which are follow up surveys of heirs, to better measure wealth held in the estate. The results suggest even larger declines in wealth when the final member of the household dies. For those at the top of the income distribution, the death of a single person results in a wealth decline

of approximately \$110,000, whereas the decline is closer to \$70,000 for those at the bottom of the income distribution.

One should take the wealth increase when both members of the household die for those at the top of the income distribution with some caution, since very few households have both members die at exactly the same time.

7 Conclusions

Over one-third of total wealth in the United States is held by households over age 65. This wealth is an important determinant of their consumption and welfare. As the U.S. population continues to age, the elderlys savings will only grow in importance.

Retired U.S. households, especially those who are part of a couple and have high income, decumulate their assets at a slow rate and often die with large amounts of assets, raising the questions of what drives their savings behavior and how their savings would respond to policy reforms.

We develop a model of optimal lifetime decision making and estimate key properties of the model. We find that singles live less long than people who are part of a couple, but are more likely to end up in a nursing home in any given year. For that reason, singles also have higher medical spending, per person, than people who are part of a couple. We also find that assets drop sharply with the death of a spouse. By the time the second spouse dies, a large fraction of the wealth of the original couple has vanished, with the wealth falls at the time of death of each spouse explaining most of the decline. A large share of these drops in assets is explained by the high medical expenses at the time of death. This suggests that a large fraction of all assets held in retirement are used to insure oneself against the risk of high medical and death expenses.

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Appendix A: Inferring Permanent Income

We assume that log income follows the process

$$ln y_{it} = \kappa_1(t, f_{it}) + h(I_i) + \omega_{it}$$
(19)

where $\kappa_1(t, f_{it})$ is a flexible functional form of age t and family structure f_{it} (i.e., couple, single male, or single female) and ω_{it} represents measurement error. The variable I_i is the household's percentile rank in the permanent income distribution. Since it is a summary measure of lifetime income at retirement, it should not change during retirement and is thus a fixed effect over our sample period. However, income could change as households age and potentially lose a family member. Our procedure to estimate equation (19) is to first estimate the fixed effects model

$$ln y_{it} = \kappa_1(t, f_{it}) + \alpha_i + \omega_{it}$$
(20)

which allows us to obtain a consistent estimate of the function $\kappa_1(t, f_{it})$. Next, note that as the number of time periods over which we can measure income and other variables for individual i (denoted T_i) becomes large,

$$plim_{T_i \to \infty} \frac{1}{T_i} \sum_{t=1}^{T_i} [\ln y_{it} - \kappa_1(t, f_{it}) - \omega_{it}] = \frac{1}{T_i} \sum_{t=1}^{T_i} [\ln y_{it} - \kappa_1(t, f_{it})] = h(I_i).$$
(21)

Thus we calculate the percentile ranking of permanent income I_i for every household in our sample by taking the percentile ranking of $\frac{1}{T_i}\sum_{t=1}^{T_i}[\ln y_{it} - \widehat{\kappa}_1(t, f_{it})]$, where $\widehat{\kappa}_1(t, f_{it})$ is the estimated value of $\kappa_1(t, f_{it})$ from equation (20). Put differently, we take the mean residual per person from the fixed effects regression (where the residual includes the estimated fixed effect), then take the percentile rank of the mean residual per person to construct I_i . This gives us a measure of the percentile ranking of permanent income I_i . However, we also need to estimate the function $h(I_i)$, which gives a mapping from the estimated index I_i back to a predicted level of income that can be used in the dynamic programming model. To do this we estimate the function

$$[\ln y_{it} - \widehat{\kappa}_1(t, f_{it})] = h(I_i) + \omega_{it}$$
(22)

where the function $h(I_i)$ is a flexible functional form.

In practice we model $\kappa_1(t, f_{it})$ as a third order polynomial in age, dummies for family structure, and family structure interacted with an age trend. We

model $h(I_i)$ as a fifth order polynomial in our measure of permanent income percentile.

Given that we have for every member of our sample t, f_{it} , and estimates of I_i and the functions $\kappa_1(.,.), h(.)$, we can calculate the predicted value of $\ln \hat{y}_{it} = \hat{\kappa}_1(t, f_{it}) + \hat{h}(\hat{I}_i)$. It is $\ln \hat{y}_{it}$ that we use when simulating the model for each household. A regression of $\ln y_{it}$ on $\ln \hat{y}_{it}$ yields a R^2 statistic of .74, suggesting that our predictions are accurate.

Appendix B: Asset Profiles Based on PI percentiles computed on whole population rather than on the subpopulation of interest.

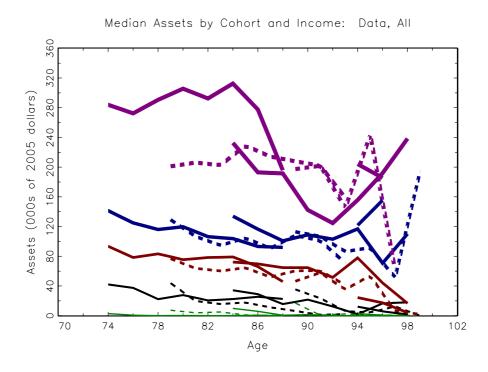


Figure 7: Median assets, whole sample. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

Appendix C: Imputing Medicaid plus Out of Pocket Medical Expenses



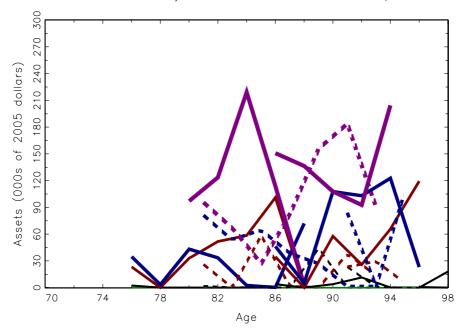


Figure 8: Bequests, whole sample. Each line represents the median bequest for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

Our goal is to measure the data generating process of the sum of Medicaid payments plus out of pocket expenses: this is the variable $\ln(m_{it})$ in equation (6) of the main text. If the household is drawing Medicaid benefits, then the household will spend less than $\ln(m_{it})$ on out of pocket medical spending (Medicaid picking up the remainder).

The AHEAD data contains information on out of pocket medical spending, but not on Medicaid payments. Fortunately, the Medicare Current Beneficiary Survey (MCBS) has extremely high quality information on Medicaid payments plus out of pocket medical spending. One drawback of the MCBS, however, is that although it has information on marital status and household income, it does not have information on the medical spending or health of the spouse. Here we explain how to exploit the best of both datasets.

We use a two step estimation procedure. First, we estimate the process

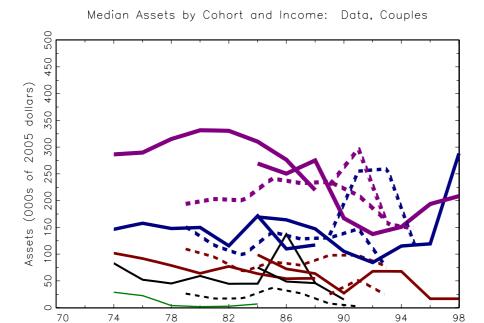


Figure 9: Median assets for couples, PI percentiles computed using whole population. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

Age

for household out of pocket medical spending using the AHEAD. Second, we estimate the process for Medicaid payments plus out of pocket medical spending as a function of out of pocket medical spending and other state variables using the MCBS. Because the MCBS lacks information on spouse's medical spending, and because most elderly Medicaid recipients are singles, we employ the second step estimation procedure only for singles. For couples we use only the first stage estimates estimated using the AHEAD data.

First Step Estimation Procedure: Define $\ln(oop_{it})$ as the log of out of pocket medical expenses and $X_{it} = (hs_t^h, hs_t^w, I, g, t, f_t, f_{t-1})$. Using AHEAD data, we first use fixed effects estimation procedures to estimate

$$\ln(oop_{it}) = \kappa_2(X_{it}) + \epsilon_{it}. \tag{23}$$

Median Assets by Cohort and Income: Data, Intact Couples

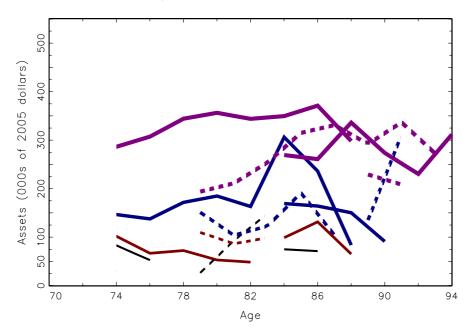


Figure 10: Median assets for intact couples, PI percentiles computed using whole population. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

Next we construct the estimated residuals $\hat{\epsilon_{it}} = \ln(oop_{it}) - \hat{g}(X_{it})$ and estimate the regression (using OLS and no fixed effects):

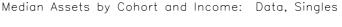
$$\hat{\epsilon_{it}}^2 = h(X_{it}) + \zeta_{it}. \tag{24}$$

This allows us to recover the variance of ϵ_{it} conditional on X_{it} .

Second Step Estimation Procedure: Once we estimate equations (23) and (24) on the AHEAD data, we use the MCBS to estimate the link between $\ln(m_{it})$ and $\ln(oop_{it})$ for singles using OLS with no fixed effects:

$$\ln(m_{it}) = \alpha \ln(oop_{it}) + k(X_{it}) + u_{it}, \tag{25}$$

so we can construct $\hat{u}_{it} = \ln(m_{it}) - (\hat{\alpha} \ln(oop_{it}) + \hat{k}(X_{it}))$ and estimate the



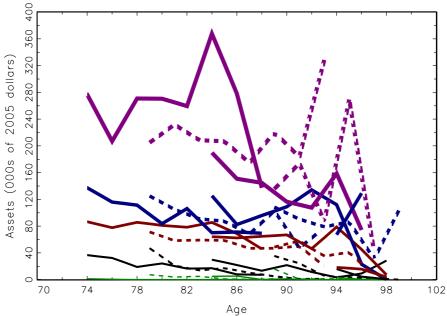


Figure 11: Median assets for singles, PI percentiles computed using whole population. Each line represents median assets for a cohort-income cell, traced over the time period 1996-2010. Thicker lines refer to higher permanent income groups. Solid lines: cohorts ages 72-76 and 82-86 in 1996. Dashed lines: ages 82-86 and 92-96 in 1996.

conditional variance of this:

$$\hat{u_{it}}^2 = \hat{l}(X_{it}) + \xi_{it} \tag{26}$$

Combining equations (23) and (25) yields

$$\ln(m_{it}) = \alpha \kappa_2(X_{it}) + k(X_{it}) + (\alpha \epsilon_{it} + u_{it}). \tag{27}$$

Recall that equation (6) of the main text is given by $\ln(m_{it}) = m(X_{it}) + \sigma(X_{it}) \times \psi_t$. Equation (27) then implies that $m(X_{it}) = \alpha g(X_{it}) + k(X_{it})$.

In order to infer the variance of medical expenditures conditional on X_{it} , note that from equations (6) and (27)

$$\sigma(X_{it}) \times \psi_{it} = \ln(m_{it}) - m(X_{it}) = (\alpha \epsilon_{it} + u_{it}). \tag{28}$$

so we can obtain the conditional variance by noting that $E[\psi_{it}^2]=1$ and assuming that $E[\epsilon_{it}u_{it}]=0$

$$[\sigma(X_{it})]^2 = E[(\alpha \epsilon_{it} + u_{it})^2 | X_{it}] = \alpha^2 E[\epsilon_{it}^2 | X_{it}] + E[u_{it}^2 | X_{it}]$$
 (29)

where we estimate $E[\epsilon_{it}^2|X_{it}] = h(X_{it})$ in equation (24) and $E[u_{it}^2|X_{it}]$ in equation (26).

Appendix D: Outline of the computation of the value functions and optimal decision rules

We compute the value functions by backward induction. We start from the singles, find their time T value function and decision rules by maximizing equation (15) subject to the relevant constraints, and $V_{T+1}^g = \theta_0(x_t - c_t)$, g = h, w. This yields the value function V_T^g and the decision rules for time T. We then find the decision rules at time T-1 by solving equation (15) with V_T^g . Continuing this backward induction yields decision rules for time T-2, T-3, ..., 1.

We find the decisions for couples by maximizing equation (16), subject to the relevant constraints and the value function for the singles, and setting V_{T+1}^c to the appropriate bequest motive value. This yields the value function V_T^c and the decision rules for time T. We then find the decision rules at time T-1 by solving equation (16) using $V_T^c, V_T^g, g = h, w$. Continuing this backward induction yields decision rules for time T-2, T-3, ..., 1.

We discretize the persistent component and the transitory components of the health shock, and interest rate into Markov Chain following Tauchen and Hussey (1991). We assume a finite number of permanent income categories. We take cash-on-hand to lay into a finite number of grid points.

Given each level of permanent income of the household, we solve for decision rules for each possible combination of cash-on-hand, income, health status, and persistent component of the health shock. We use linear interpolation within the grid and linear extrapolation outside of the grid to evaluate the value function at points that we do not directly compute.

For the singles, for simplicity of notation, here for the most part we drop any reference to the missing spousal variables everywhere, and just use similar notation to the one for couples (except for the number of arguments in the function). In the code, we have different names, say for example for the survival of single people and couples.

The value function for the singles, g = h, w and $f_t = 0$ is given by:

$$\begin{split} V_{t}^{g}(x_{t}, hs_{t}, I, \zeta_{t}) &= \max_{c_{t}, x_{t+1}} \left\{ u(c_{t}, hs_{t}) + \beta \Big(1 - s(hs_{t}, I, g, t, 0) \Big) \theta_{0} \Big(x_{t} - c_{t} \Big) + \\ \beta s(hs_{t}, I, g, t, 0) \Big[\sum_{k=1}^{d_{m}} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\xi}} Pr(hs_{t+1} = hs_{k} | hs_{t}, I, g, t, 0) Pr(\zeta_{t+1} = \zeta_{l} | \zeta_{t}) Pr(\xi_{t+1} = \xi_{n}) \\ V_{t+1}^{g} \Big(x_{t+1}(k, l, n), hs_{t+1}(k), I, \zeta_{t+1}(l) \Big) \Big] \right\}. \end{split}$$

Subject to:

$$z_{t+1} = x_t - c_t + y \Big(r(x_t - c_t) + y_{t+1}(I, 0), \tau \Big)$$

$$x_t > c_{min}(g), \quad c_t \le x_t, \quad \forall t,$$

$$\ln(m_{t+1}(k, l, n)) = m^g (hs_{t+1}(k), I, t+1) + \sigma^g (hs_{t+1}(k), I, t+1) \psi_{t+1}(l, n)$$

$$\psi_{t+1}(l, n) = \zeta_{t+1}(l) + \xi_{t+1}(n),$$

$$s_{t+1}(k, l, n) = z_{t+1} - m_{t+1}(k, l, n)$$

$$tr_{t+1}(k, l, n) = \max \Big\{ 0, c_{\min}(f_t) - \max(0, s_{t+1} - a_d(i)) \Big\}$$

$$x_{t+1}(k, l, n) = s_{t+1}(k, l, n) + tr_{t+1}(k, l, n)$$

$$\forall x_t \text{ COH level, determine maximum consumption (and hence savings)}$$

$$\forall c_t \in (c_{\min}, x_t), \text{ compute } u^g(c, m) \text{ and } \theta_0(x_t - c_t).$$

 $\forall (g, t, I)$ For each gender, age, PI, compute savings $= z_{t+1}$

 $\forall hs_t, \zeta_t$ For each health state and pers. medex shock TODAY

 $\forall h s_{t+1}(k), \zeta_{t+1}(l), \xi(n) \text{ tomorrow's shocks}$

 $x_{t+1}(k,l,n)$ compute tomorrow's COH for each state

Interpolate and extrapolate $V_{t+1}^g(x_{t+1}(k,l,n),hs_{t+1}(k),I,\zeta_{t+1}(l))$

$$\beta s(hs_t, I, t) \sum_{k=1}^{d_m} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\xi}} \Pi(k, l, n) V_{t+1}^g(x_{t+1}(k, l, n), hs_{t+1}(k), I, \zeta_{t+1}(l)) \beta(1 - s(hs_t, I, t)) \phi_0(x_t - c_t) + u^g(c_t, hs_t)$$

 $W(c_t, x_t, I, hs_t, \zeta_t) = \text{sum of the two lines just above}$

 $\max_{c_t} W(c_t, x_t, I, hs_t, \zeta_t)$

 $c_t^g(x_t, I, hs_t, \zeta_t) = \text{maximizer}$

 $V_t^g(x_t, I, hs_t, \zeta_t) = \text{maximum}$

The value function for the couples is given by:

$$V_{t}^{c}(x_{t}, hs_{t}^{w}, hs_{t}^{h}, I, \zeta_{t}) = \max_{c_{t}, x_{t+1}, b_{t}^{w}, b_{t}^{h}} \left\{ u^{c}(c_{t}, hs_{t}^{h}, hs_{t}^{w}) + \right. \\ \left. + \beta \left(1 - s(hs^{w}, I, w, t, 1) \right) \left(1 - s(hs^{h}, I, h, t, 1) \right) \theta_{2}(x_{t} - c_{t}) + \\ \left. \beta s(hs^{w}, I, w, t, 1) (1 - s(hs^{h}, I, h, t, 1)) \left(\theta_{1}(b_{t}^{h}) + \omega \sum_{k=1}^{d_{m}} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\zeta}} Pr(\zeta_{t+1} = \zeta_{l} | \zeta_{t}) \right. \\ \left. Pr(\xi_{t+1} = \xi_{n}) Pr(hs_{t+1}^{w} = hs_{k} | hs_{t}^{w}, I, w, t, 1) V_{t+1}^{w}(x_{t+1}^{w}(k, l, n), hs_{t+1}^{w}(k), I, \zeta_{t+1}(l)) \right) + \\ \left. \beta (1 - s(hs^{w}, I, w, t, 1)) s(hs^{h}, I, h, t, 1) \left(\theta_{1}(b_{t}^{w}) + \omega \sum_{k=1}^{d_{m}} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\zeta}} Pr(\zeta_{t+1} = \zeta_{l} | \zeta_{t}) \right. \\ \left. Pr(\xi_{t+1} = \xi_{n}) Pr(hs_{t+1}^{h} = hs_{kh} | hs_{t}^{h}, I, h, t, 1) V_{t+1}^{h}(x_{t+1}^{h}(k, l, n), hs_{t+1}^{h}(k), I, \zeta_{t+1}(l)) \right) + \\ \left. \beta s(hs^{w}, I, w, t, 1) s(hs^{h}, I, h, t, 1) \left. \left(\sum_{kh=1}^{d_{m}} \sum_{kw=1}^{d_{\zeta}} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\zeta}} V_{t+1}^{c}(x_{t+1}(k_{h}, k_{w}, l, n), hs_{t+1}^{w}, hs_{t+1}^{h}, I, \zeta_{t+1}(l)) \right. \right. \\ \left. \left. \left(\sum_{kh=1}^{d_{m}} \sum_{kw=1}^{d_{\zeta}} \sum_{l=1}^{d_{\zeta}} \sum_{n=1}^{d_{\zeta}} V_{t+1}^{c}(x_{t+1}(k_{h}, k_{w}, l, n), hs_{t+1}^{w}, hs_{t+1}^{h}, I, \zeta_{t+1}(l)) \right. \right) \right. \right.$$

$$\left. \left(30 \right) \right.$$

subject to

$$x_{t} > c_{min}(c), \quad c_{t} \leq x_{t}, \quad \forall t$$

$$0 < b_{t} \leq x_{t} - c_{t}, \quad \forall t, \quad i = h, w,$$

$$y_{t+1}^{c} = y(c, I, t+1)$$

$$y_{t+1}^{i} = y(i, I, t+1)$$

$$z_{t+1}^{c} = \{x_{t} - c_{t} + y(r(x_{t} - c_{t}) + y_{t+1}^{c}, \tau)\}$$

$$z_{t+1}^{i} = \{x_{t} - c_{t} + y(r(x_{t} - c_{t}) + y_{t+1}^{i}, \tau)\}$$

$$\ln m_{t+1}^{c}(k_{h}, k_{w}, l, n) = m^{c}(hs_{t+1}^{h}(k_{h}), hs_{t+1}^{w}(k_{w}), t+1, I)$$

$$+\sigma^{c}(hs_{t+1}^{h}(k_{h}), hs_{t+1}^{w}(k_{w}), I, t+1)\psi_{t+1}(l, n)$$

```
\ln m_{t+1}^g(k,l,n) = m^g(g,hs_{t+1}^i(k),t+1,I) + \sigma^g(g,hs_{t+1}^g(k),I,t+1)\psi_{t+1}(l,n)
                                        \psi_{t+1}(l,n) = \zeta_{t+1}(l) + \xi_{t+1}(n),
                 x_{t+1}^{c}(k_h, k_w, l, n) = \max\{z_{t+1}^{c} - m_{t+1}^{c}(k_h, k_w, l, n), c_{\min}(c)\}
                   x_{t+1}^{g}(j, k, l, n) = \max\{z_{t+1}^{i} - m_{t+1}^{i}(k, l, n) - b_{t}, c_{\min}(i)\}
      Computation
     \forall (x_t)
              \forall c_t \in (c_{\min}, x_t)
                  \theta_2 (x_t - c_t)
                  \forall (b_t^i \in (0, x_t))
                  \theta_1(b_t)
                  \forall (m_t^h, m_t^w)
                  u\left(c_t,m_t^h,m_t^w\right)
                       sumC: expected value next period in case both survive
                       sumH: expected value next period in case husband dies
                       sumW: expected value next period in case wife dies
                       bequestUCM: utility from bequests when both die
              W(c_t, x_t, I, m_t^h, m_t^w, \zeta_t) = u\left(c_t, m_t^h, m_t^w\right) + \beta s_{m,I,t}^w s_{m,I,t}^h \text{ sumC} + \beta s_{m,I,t}^w (1 - s_{m,I,t}^h) \text{ sumH} + \beta (1 - s_{m,I,t}^w) s_{m,I,t}^h \text{ sumW} + \beta (1 - s_{m,I,t}^w) (1 - s_{m,I,t}^h) + \beta (1 - s_{m,I,t}^w) (1 - s_{m,I,t}^h) \text{ bequestUCM}
\max_{c_t} W(c_t, x_t, I, m_t^h, m_t^w, \zeta_t)
              c_t^c(x_t, I, m_t^h, m_t^w, \zeta_t) = \text{maximizer}
              V_t^c(x_t, I, m_t^h, m_t^w, \zeta_t) = \text{maximum}
```

In the calculation of next period's expected value in the case in which one spouse dies (sumH and sumW), we compute the optimal decision rule for bequests, conditional on each consumption choice. In the end when we get the decision rule for consumption, we automatically get the optimal decision rule of bequest corresponding to each state $b_t^c(x_t, I, m_t^h, m_t^w, \zeta_t)$

Appendix E: Moment Conditions and the Asymptotic Distribution of Parameter Estimates

Our estimate, $\hat{\Delta}$, of the "true" preference vector Δ_0 is the value of Δ that minimizes the (weighted) distance between the estimated life cycle profiles for assets found in the data and the simulated profiles generated by the model. For each calendar year $t \in \{1, ..., T\}$, we match median assets for 5 permanent income quintiles in 5 birth year cohorts, both for singles and couples, leading to a total of 50T moment conditions. Sorting households into quintiles also requires us to estimate the 1/5th, 2/5th, 3/5th and 4/5th permanent income quantiles for each birth year cohort and initial family type. This produces a total of 40 nuisance parameters, which we collect into the vector γ . Each of these parameters has its own moment condition.

The way in which we construct these moment conditions builds on the approach described in French and Jones [28]. Useful references include Buchinsky [10] and Powell [44]. Consider first the permanent income quantiles. Let $q \in \{1, 2, ..., Q - 1\}$ index the quantiles. Assuming that the permanent income distribution is continuous, the π_q -th quantile of permanent income for initial family type f of cohort c, $g_{\pi_q}(c, f)$, is defined as

$$\Pr\left(I_i \le g_{\pi_q}(c, f) | c, f\right) = \pi_q. \tag{31}$$

In other words, the fraction of households with less than g_{π_j} in permanent income is π_j . Using the indicator function, the definition of π_j -th conditional quantile can be rewritten as

$$E([1\{I_i \le g_{\pi_q}(c, f)\} - \pi_j] \times 1\{c_i = c\} \times 1\{f_i = f\}) = 0,$$
 (32)

for $c \in \{1, 2, ..., C\}$, $f \in \{\text{single, couple}\}$, $q \in \{1, 2, ..., Q - 1\}$.

The more important set of moment conditions involves the permanent income-conditional age-asset profiles. Suppose that household i's permanent income level falls in the qth permanent income interval of households in its cohort, i.e.,

$$g_{\pi_{q-1}}(c,f) \le I_i \le g_{\pi_q}(c,f).$$
 (33)

We assume that $\pi_0 = 0$ and $\pi_Q = 1$, so that $g_{\pi_0}(c, f) \equiv -\infty$ and $g_{\pi_Q}(c, f) \equiv \infty$. Let $a_{cfqt}(\Delta, \chi)$ be the model-predicted median observed asset level for group cfqt. Recall that the median is just the 1/2 quantile. Assuming that observed assets have a continuous conditional density, we arrive at the following moment condition:

$$E(1{\{\tilde{a}_{it} \leq a_{cfqt}(\Delta_0, \chi_0)\}} - 1/2 | c, f, q, t, \text{household observed at } t) = 0.$$
 (34)

Equation (34) is merely equation (18) in the main text, adjusted to allow for "missing" as well as deceased households, as in French and Jones [27]. Using indicator function notation, we can convert this conditional moment equation into an unconditional one:

$$E\Big([1\{\tilde{a}_{it} \le a_{cfqt}(\Delta_0, \chi_0)\} - 1/2] \times 1\{c_i = c\} \times 1\{f_i = f\}$$

$$\times 1\{g_{\pi_{q-1}}(c, f) \le I_i \le g_{\pi_q}(c, f)\} \times 1\{\text{household observed at } t\} \mid t\Big) = 0,$$
(35)

for $c \in \{1, 2, ..., C\}$, $f \in \{\text{single, couple}\}$, $q \in \{1, 2, ..., Q\}$, $t \in \{t_1, t_2, ..., t_T\}$.

Suppose we have a data set of I independent households that are each observed at T separate calendar years. Let $\varphi(\Delta, \gamma; \chi_0)$ denote the (50T+40)-element vector of moment conditions described immediately above, and let $\hat{\varphi}_I(.)$ denote its sample analog. Letting $\widehat{\mathbf{W}}_I$ denote a $(50T+40)\times(50T+40)$ weighting matrix, the MSM estimator $(\hat{\Delta}', \hat{\gamma}')'$ is given by

$$\underset{\{\Delta,\gamma\}}{\operatorname{arg\,min}} \frac{I}{1+\tau} \, \hat{\varphi}_I(\Delta,\gamma;\chi_0)' \widehat{\mathbf{W}}_I \hat{\varphi}_I(\Delta,\gamma;\chi_0),$$

where τ is the ratio of the number of observations to the number of simulated observations.

In practice, we estimate χ_0 as well, using the approach described in the main text. Computational concerns, however, compel us to treat χ_0 as known in the analysis that follows. Under regularity conditions stated in Pakes and Pollard [40] and Duffie and Singleton [22], the MSM estimator $\hat{\theta}$ is both consistent and asymptotically normally distributed:

$$\sqrt{I}\left(\left(\begin{array}{c}\hat{\Delta}\\\hat{\gamma}\end{array}\right)-\left(\begin{array}{c}\Delta_0\\\gamma_0\end{array}\right)\right)\rightsquigarrow N(0,\mathbf{V}),$$

with the variance-covariance matrix \mathbf{V} given by

$$\mathbf{V} = (1+\tau)(\mathbf{D}'\mathbf{W}\mathbf{D})^{-1}\mathbf{D}'\mathbf{W}\mathbf{S}\mathbf{W}\mathbf{D}(\mathbf{D}'\mathbf{W}\mathbf{D})^{-1},$$

where: **S** is the variance-covariance matrix of the data;

$$\mathbf{D} = \left[\frac{\partial \varphi(\Delta, \gamma; \chi_0)}{\partial \Delta'} \bigg|_{\Delta = \Delta_0} \quad \frac{\partial \varphi(\Delta, \gamma; \chi_0)}{\partial \gamma'} \bigg|_{\gamma = \gamma_0} \right]$$
(36)

is the $(50T+40) \times (9+40)$ gradient matrix of the population moment vector; and $\mathbf{W} = \text{plim}_{\to \infty} \{\widehat{\mathbf{W}}_I\}$. Moreover, Newey [38] shows that if the model is properly specified,

$$\frac{I}{1+\tau}\hat{\varphi}_I(\hat{\Delta},\hat{\gamma};\chi_0)'\mathbf{R}^{-1}\hat{\varphi}_I(\hat{\Delta},\hat{\gamma};\chi_0) \leadsto \chi^2_{50T-9},$$

where \mathbf{R}^{-1} is the generalized inverse of

$$\begin{split} \mathbf{R} &= \mathbf{PSP}, \\ \mathbf{P} &= \mathbf{I} - \mathbf{D} (\mathbf{D'WD})^{-1} \mathbf{D'W}. \end{split}$$

The asymptotically efficient weighting matrix arises when $\widehat{\mathbf{W}}_I$ converges to \mathbf{S}^{-1} , the inverse of the variance-covariance matrix of the data. When $\mathbf{W} = \mathbf{S}^{-1}$, \mathbf{V} simplifies to $(1+\tau)(\mathbf{D}'\mathbf{S}^{-1}\mathbf{D})^{-1}$, and \mathbf{R} is replaced with \mathbf{S} . But even though the optimal weighting matrix is asymptotically efficient, it can be severely biased in small samples. (See, for example, Altonji and Segal [1].) We thus use a "diagonal" weighting matrix, as suggested by Pischke [42]. The diagonal weighting scheme uses the inverse of the matrix that is the same as \mathbf{S} along the diagonal and has zeros off the diagonal of the matrix.

We estimate \mathbf{D} , \mathbf{S} and \mathbf{W} with their sample analogs. For example, our estimate of \mathbf{S} is the $(50T+40)\times(50T+40)$ estimated variance-covariance matrix of the sample data. When estimating preferences, we use sample statistics, so that $a_{cfqt}(\Delta, \chi)$ is replaced with the sample median for group cfqt. When computing the chi-square statistic and the standard errors, we use model predictions, so that the sample medians for group cfqt is replaced with its simulated counterpart, $a_{cfqt}(\hat{\Delta}, \hat{\chi})$.

One complication in estimating the gradient matrix \mathbf{D} is that the functions inside the moment condition $\varphi(\Delta, \gamma; \chi)$ are non-differentiable at certain data points; see equations (32) and (35). This means that we cannot consistently estimate \mathbf{D} as the numerical derivative of $\hat{\varphi}_I(.)$. Our asymptotic results therefore do not follow from the standard GMM approach, but rather the approach for non-smooth functions described in Pakes and Pollard [40], Newey and McFadden [39] (section 7) and Powell [44].

In finding **D**, it proves useful to partition $\varphi(.)$ into the 50*T*-element vector $\varphi_{\Delta}(.)$, corresponding to the moment conditions described by equation (35) and the 40 - element vector $\varphi_{\gamma}(.)$, corresponding to the moment conditions described by equation (32). Using this notation, we can rewrite equation

(36) as

$$\mathbf{D} = \begin{bmatrix} \frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'} & \frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'} \\ \frac{\partial \varphi_{\gamma}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'} & \frac{\partial \varphi_{\gamma}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'} \end{bmatrix}, \tag{37}$$

and proceed element-by-element.

It immediately follows from equation (32) that

$$\frac{\partial \varphi_{\gamma}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'} = \mathbf{0}. \tag{38}$$

To find $\frac{\partial \varphi_{\gamma}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'}$, we rewrite equation (32) as

$$\Pr(c_i = c \& f_i = f) \times \left[F\left(g_{\pi_q}(c, f) | c, f \right) - \pi_j \right] = 0, \tag{39}$$

where $F\left(g_{\pi_q}(c,f)|c,f\right)$ is the c.d.f. of permanent income for family typef members of cohort c evaluated at the π_j -th quantile. Differentiating this equation shows that $\frac{\partial \varphi_{\gamma}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'}$ is a diagonal matrix whose diagonal elements are given by

$$\Pr\left(c_i = c \& f_i = f\right) \times f\left(g_{\pi_q}(c, f)|c, f\right). \tag{40}$$

In practice we find $f(g_{\pi_q}(c,f)|c,f)$, the conditional p.d.f. of permanent

income evaluated at the π_j -th quantile, with a kernel density estimator. To find $\frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'}$ and $\frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'}$, it is helpful to rewrite equation (35) as

 $\Pr\left(c_i = c \& f_i = f \& \text{ household observed at } t\right) \times$

$$\int_{g_{\pi_{q-1}}(c,f)}^{g_{\pi_q}(c,f)} \left[\int_{-\infty}^{a_{cfqt}(\Delta_0,\chi_0)} f(\tilde{a}_{it}|c,f,I_i,t) d\tilde{a}_{it} - \frac{1}{2} \right] f(I_i|c,f) dI_i = 0, \quad (41)$$

It follows that the rows of $\frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'}$ are given by

 $\Pr\left(c_i = c \ \& \ f_i = f \ \& \ g_{\pi_{q-1}}(c,f) \le I_i \le g_{\pi_q}(c,f) \ \& \ \text{household observed at } t\right) \times$

$$f(a_{cfqt}|c, f, g_{\pi_{q-1}}(c, f) \le I_i \le g_{\pi_q}(c, f), t) \times \frac{\partial a_{cfqt}(\Delta_0, \gamma_0; \chi_0)}{\partial \Delta'}.$$
 (42)

Proceeding similarly, it can be shown that each row of $\frac{\partial \varphi_{\Delta}(\Delta_0, \gamma_0; \chi_0)}{\partial \gamma'}$ has the following two non-zero elements:

 $\Pr\left(c_i = c \& f_i = f \& \text{ household observed at } t\right) \times$

$$\begin{pmatrix} -f(g_{\pi_{q-1}}(c,f)|c,f) \left[F(a_{cfqt}|c,f,g_{\pi_{q-1}}(c,f),t) - 1/2 \right] \\ f(g_{\pi_q}(c,f)|c,f) \left[F(a_{cfqt}|c,f,g_{\pi_q}(c,f),t) - 1/2 \right] \end{pmatrix}', \tag{43}$$

with

$$f(g_{\pi_0}(c,f)|c,f) \left[F(a_{cfqt}|c,f,g_{\pi_0}(c,f),t) - 1/2 \right] \equiv 0, \qquad (44)$$

$$f(g_{\pi_Q}(c,f)|c,f) \left[F(a_{cfqt}|c,f,g_{\pi_Q}(c,f),t) - 1/2 \right] \equiv 0. \qquad (45)$$

$$f\left(g_{\pi_Q}(c,f)|c,f\right)\left[F\left(a_{cfqt}|c,f,g_{\pi_Q}(c,f),t\right)-1/2\right] \equiv 0. \tag{45}$$

In practice, we find $F\left(a_{cfqt}|c,f,I,t\right)$, the conditional c.d.f. of assets evaluated at the median a_{cfqt} by finding kernel estimates of the mean regression of $1\{a_{it} \leq a_{cfqt}\}$ on I (holding c,f and, t fixed).