

# High-Earner Lemons

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Chicago, 5 January 2012



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# Outline



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- ▶ Adverse selection is potentially a serious problem in markets for health insurance.
- ▶ The theoretical literature suggests severe welfare losses might occur as a result (Rotschild & Stiglitz, 1976).
- ▶ The empirical literature has mainly been concerned with the identification of adverse selection:
  - ▶ A positive correlation between coverage and risk may be due to moral hazard, or adverse selection, or both.
  - ▶ Risk is not the only source of heterogeneity: other dimensions might give rise to advantageous selection.
  - ▶ Methods are typically simple and results not necessarily useful for policy purposes.
- ▶ Recent contributions use structural estimation to identify underlying preference and risk parameters (Einav et al, 2009).
- ▶ The identification problem remains, but estimates more useful and informative.

**Aim of the paper:** To estimate the distribution of risk and preference parameters among German holders of PHI.

- ▶ The German system is dual: 20 % of population can opt out of public system.
- ▶ Insured individuals may choose coinsurance rate, monetary deductible, and service package.
- ▶ The choice of parameters reveals information on individual risk and preferences.
- ▶ We consider two stages of the decision:
  1. **Ex ante:** The choice of coinsurance reveals information.
  2. **Ex post:** These coinsurance parameters rule out some 'corner solutions'.
- ▶ Theoretical model: Additive CARA utility function.
- ▶ We do not achieve point identification, but the distribution of parameters is identified already from ex ante information – thus not contaminated by moral hazard.

We use a simple additive CARA utility function:

$$U(c, m | n) = -\exp(-\gamma c) - \beta \exp(-\gamma(m - n)) \quad (1)$$

where

- ▶  $m$  is the consumption of medical care services.
- ▶  $c$  is the consumption of other goods and services:  $c = y - p - z(m | \alpha, D)$
- ▶  $z(m | \alpha, D)$  is the out-of-pocket payment for someone with coinsurance rate  $\alpha$  and deductible  $D$ .
- ▶  $\gamma$  is the relative risk aversion.
- ▶  $\beta$  is the preference for consumption of health care.
- ▶  $n$  is the severity of illness (exponentially distributed with parameter  $\theta$ ).
- ▶  $p$  is the insurance premium.



Inserting the budget constraint and solving, we get

$$m_{-}^{*}(n) = \frac{y - p + n - \frac{1}{\gamma} \ln \left( \frac{1+\delta}{\beta} \right)}{2 + \delta}$$
$$m_{+}^{*}(n) = \frac{y - p - \alpha D + n - \frac{1}{\gamma} \ln \left( \frac{1-\alpha+\delta}{\beta} \right)}{2 - \alpha + \delta}$$

...from which we get two ‘corner solutions’:

1. At  $\tilde{n}$ ,  $m_{-}^{*}(n) = 0$ .
2. At  $\bar{n}$ , consumer is indifferent between  $m_{-}^{*}(n)$  and  $m_{+}^{*}(n)$ .

Identifying information:

- ▶ If  $0 < m < D$ , then  $m < m_{-}^{*}(\bar{n})$ .
- ▶ If  $m = 0$ , then  $\tilde{n} \geq 0$ .
- ▶ If  $m > D$ , then  $m \geq m_{+}^{*}(\bar{n})$

# The first stage decision

Assuming individuals know their risk parameter  $\theta$ , we consider first order conditions for the choice of  $\alpha$  and  $D$ .

The ex ante expected utility equals

$$V = - \int_0^{\infty} f_n(n) [\exp(-\gamma c^*(n)) - \beta \exp(-\gamma(m^*(n) - n))] dn. \quad (2)$$

Necessary conditions for an optimum are

$$\frac{\partial V}{\partial \alpha} \geq 0, \frac{\partial V}{\partial D} \geq 0 \quad (3)$$

From these FOC:s, we get partial identification of parameters:

1. **Case 1** ( $\alpha < 1, D > 0$ ): Interval identification of  $\gamma$ , point identification of  $(\theta, \beta)$ .
2. **Case 2** ( $\alpha = 1, D > 0$ ): Interval identification of  $\theta$ , point identification of  $\beta$ .
3. **Case 3** ( $\alpha < 1, D = 0$ ): Interval identification of  $\theta$ , point identification of  $\beta$ .
4. **Case 4** ( $\alpha = 1, D = 0$ ): Interval identification of  $\beta$ .





If we are willing to make assumptions concerning the distribution of  $\gamma$ ,  $\theta$  and  $\beta$ , we may estimate the parameters of this distribution.

## Assumptions

- ▶ *The parameters  $\psi = (\gamma, \theta, \beta)'$  take on a log-normal distribution.*
- ▶ *The logarithm vector  $\ln(\psi)$  has mean vector  $\mu = (\mu_\gamma, \mu_\theta, \mu_\beta)'$  and covariance matrix  $\Sigma$ :  $\ln(\psi) \sim \mathcal{N}(\mu, \Sigma)$*
- ▶ *The parameter  $\delta$ , reflecting the shadow cost of health care consumption, is the same for everyone.*

We model the means  $\mu = (\mu_\gamma, \mu_\theta, \mu_\beta)'$  as linear functions of characteristics  $X$ .  
These characteristics should include any information available to the insurer.  
In that case, the covariance matrix  $\Sigma$  captures the degree of asymmetric information.

Estimation is done using maximum likelihood, with numerical integration over intervals.

We (will) consider three specifications:

1. Using *ex ante* information only:

$$L_i^1(\mu, \Sigma, \delta | \alpha_i, D_i, X_i) = \Pr(\alpha_i, D_i | \mu, \Sigma, \delta, X_i).$$

These estimates cannot possibly be affected by moral hazard, but identifying information is weak.

2. Combining *ex ante* and *ex post* information:

$$L_i^2(\mu, \Sigma, \delta | m_i, \alpha_i, D_i, X_i) = \Pr(m_i | \alpha_i, D_i, \mu, \Sigma, \delta, X_i) \Pr(\alpha_i, D_i | \mu, \Sigma, \delta, X_i).$$

This approach allows for much more precise estimates, but weaker identification.

3. Using only *ex post* information:

$$L_i^3(\mu, \Sigma, \delta | m_i, \alpha_i, D_i, X_i) = \Pr(m_i | \alpha_i, D_i, \mu, \Sigma, \delta, X_i).$$

May serve as a test whether standard correlation tests deliver biased estimates.



We use the German Socio-Economic Panel for estimation: it is a household survey that is representative for Germany.

The waves 2007 and 2008 contains information on (almost) everything we need:

- ▶ Insurance parameters  $(p, \alpha, D)$ ,
- ▶ Income, age, gender, location.
- ▶ Consumption of medical care: tricky
  - ▶ We have (annual) days spent in hospital and (quarterly) visits to doctors.
  - ▶ Amounts spent had to be imputed using national averages.
- ▶ All information is self-reported.
- ▶  $p$  assumed to be log-linear function of  $\alpha$  and  $D$ .

After deleting individuals with item nonresponse, we were left with a sample of 2,363 individuals.

# Descriptive Statistics 1



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Variable	Mean	Std. Dev.	N
<i>m</i>	1,526.146	3,834.939	2,363
$\alpha$	0.977	0.071	2,363
<i>D</i>	283.667	601.5	2,363
<i>p</i>	4,932.711	2,126.193	2,363
<i>y</i>	31,913	21,507	2,363
year	0.485	0.5	2,363
age	47.058	10.802	2,363
sex	0.34	0.474	2,363
East	0.163	0.369	2,363

Table: Summary statistics of cost-sharing parameters

	D = 0			D > 0		
$\alpha = 1$	N = 1902 (56 per cent)			N = 1037 (31 per cent)		
		D	alpha		D	alpha
	Min	0	1	Min	10	1
	Mean	0	1	Mean	798	1
	Max	0	1	Max	6000	1
	SD	0	0	SD	808	0
$\alpha < 1$	N = 397 (12 per cent)			N = 31 (1 per cent)		
		D	alpha		D	alpha
	Min	0	0.50	Min	40	0.60
	Mean	0	0.79	Mean	668	0.83
	Max	0	0.99	Max	2500	0.95
	SD	0	0.11	SD	663	0.08

# Determinants of insurance premium

	(1)	(2)
	$\ln p_{2007}$	$\ln p_{2008}$
$\alpha$	0.124 (1.01)	0.153 (1.17)
$D$	-0.000153*** (-8.45)	-0.000138*** (-8.04)
age	0.0602*** (12.29)	0.0795*** (16.38)
age2	-0.000452*** (-9.85)	-0.000627*** (-13.74)
female	0.135*** (6.21)	0.144*** (6.74)
East	-0.164*** (-5.29)	-0.127*** (-4.09)
_cons	4.007*** (22.26)	3.467*** (19.38)
$N$	1,592	1,561

*t* statistics in parentheses

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

# Influence of Observable Characteristics



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	(1) $\ln \gamma$	(2) $\ln \theta$	(3) $\ln \beta$
$\delta$	30.799*** (0.516)		
constant	-12.6114*** (0.069)	-10.4343*** (0.072)	2.9244*** (0.038)
year	-0.4015*** (0.022)	-0.4003*** (0.027)	0.0216* (0.012)
age	0.0384 (0.118)	0.013 (0.128)	0.1549*** (0.054)
female	0.0601** (0.024)	0.1589*** (0.027)	0.109*** (0.013)
east	0.0773* (0.046)	0.0839* (0.051)	-0.0074 (0.024)

Standard errors in parentheses

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

# Covariance Matrix



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	(1)	(2)	(3)
	$\ln \gamma$	$\ln \theta$	$\ln \beta$
$\ln \gamma$	0.1834*** (0.01)		
$\ln \theta$	-0.1117*** (0.01)	0.4622*** (0.013)	
$\ln \beta$	-0.1143*** (0.005)	0.1877*** (0.005)	0.1191*** (0.001)

Standard errors in parentheses

\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$





- ▶ The distribution of unobservables amongst privately insured may be detected from choice of coinsurance parameters.
- ▶ Further, these coinsurance parameters introduce non-convexities in the budget set, which also carry identifying information.
- ▶ Based on a simple CARA utility function, we estimated the distribution of unobservables, and their determinants.
- ▶ Combining ex ante and ex post information gives relatively precise information on unobservables, but point identification not achieved.
- ▶ Our estimates suggest there is considerable scope for selection, but the direction not yet clear.
- ▶ Clearly, the quality of the data is one main limitation of this study.